



# Dynamical mixing of multiple populations in globular clusters

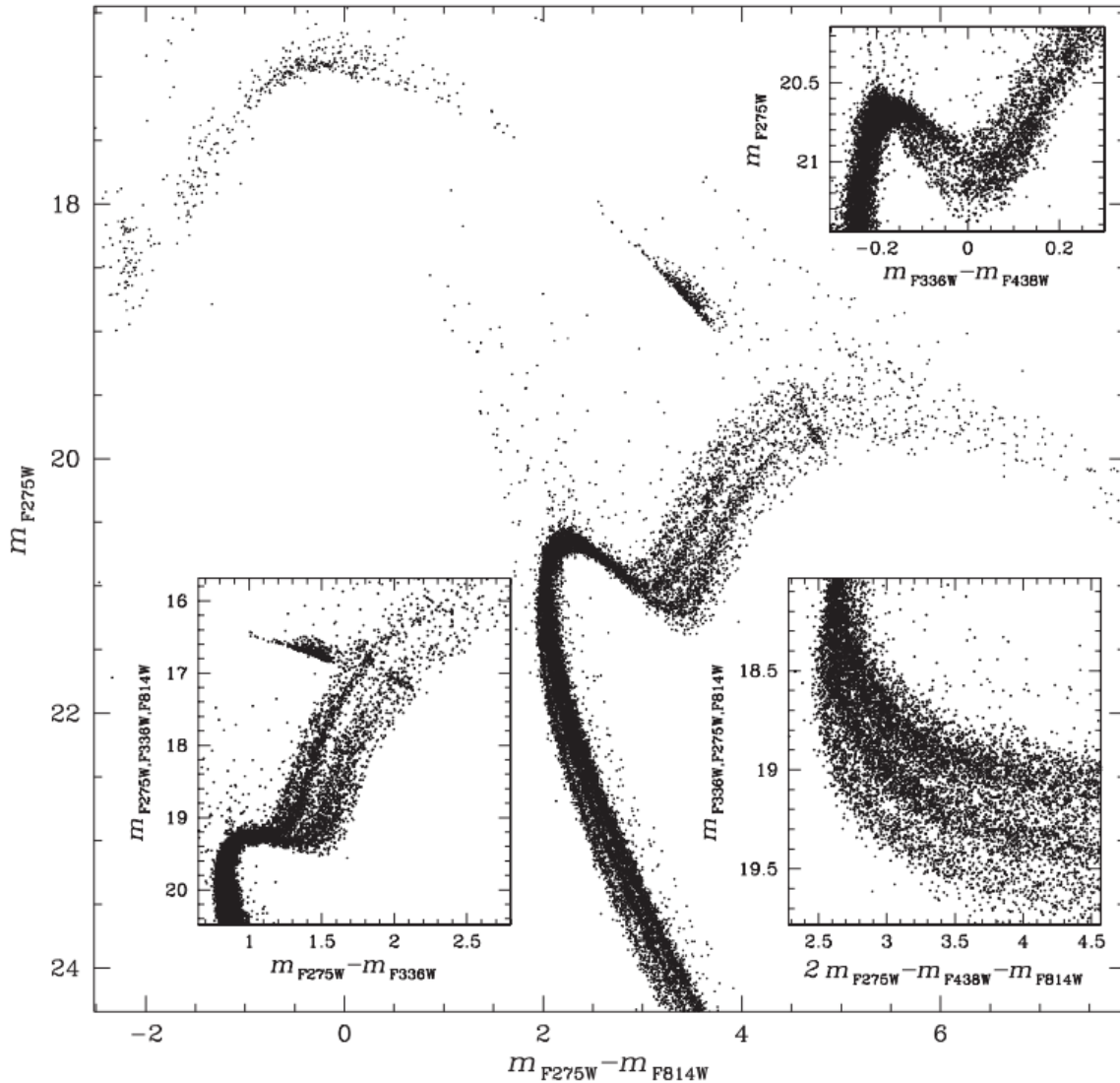
Francisco I. Aros

In collaboration with Enrico Vesperini, Alexander Livernois, Emanuele Dalessandro & Tuila Ziliotto

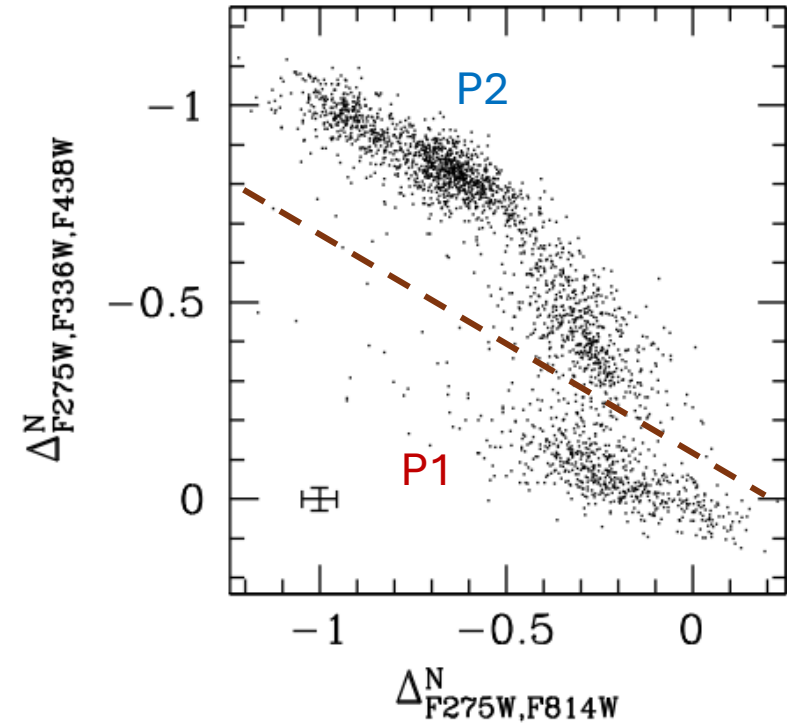


# Multiple populations in GCs

NGC 2808 – Milone et al. (2015)



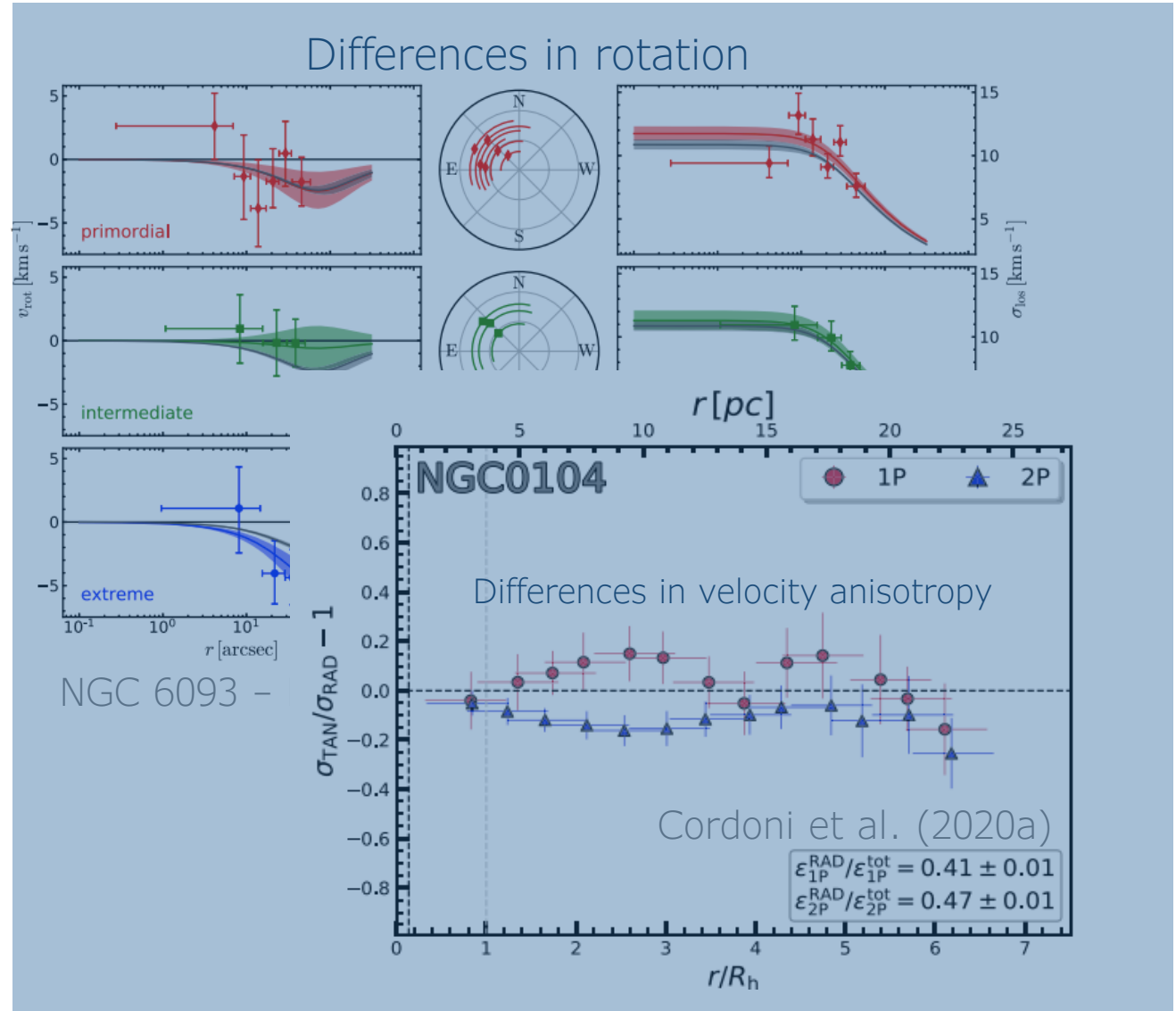
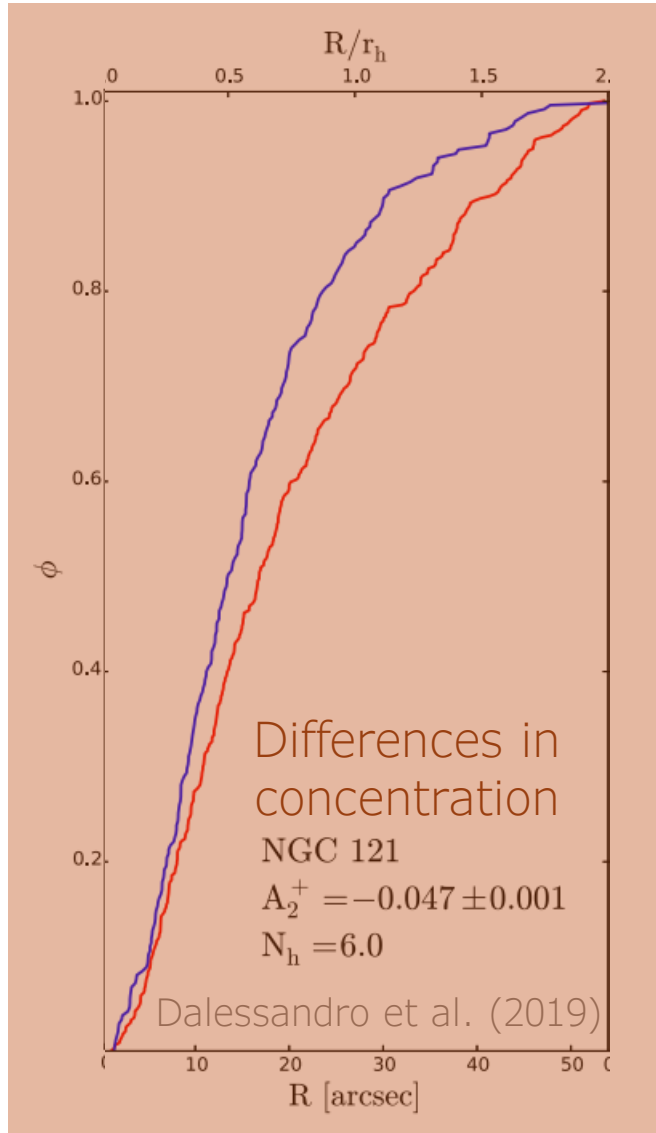
Milone et al. (2015)



See reviews by Gratton, Sneden & Carreta (2014); Bastian & Lardo (2018). Works by Piotto et al (2015); Milone et al. (2015); Milone et al. (2017)

# Structural & Kinematic differences of MPOP in GCs

SPATIAL MIXING



KINEMATIC MIXING

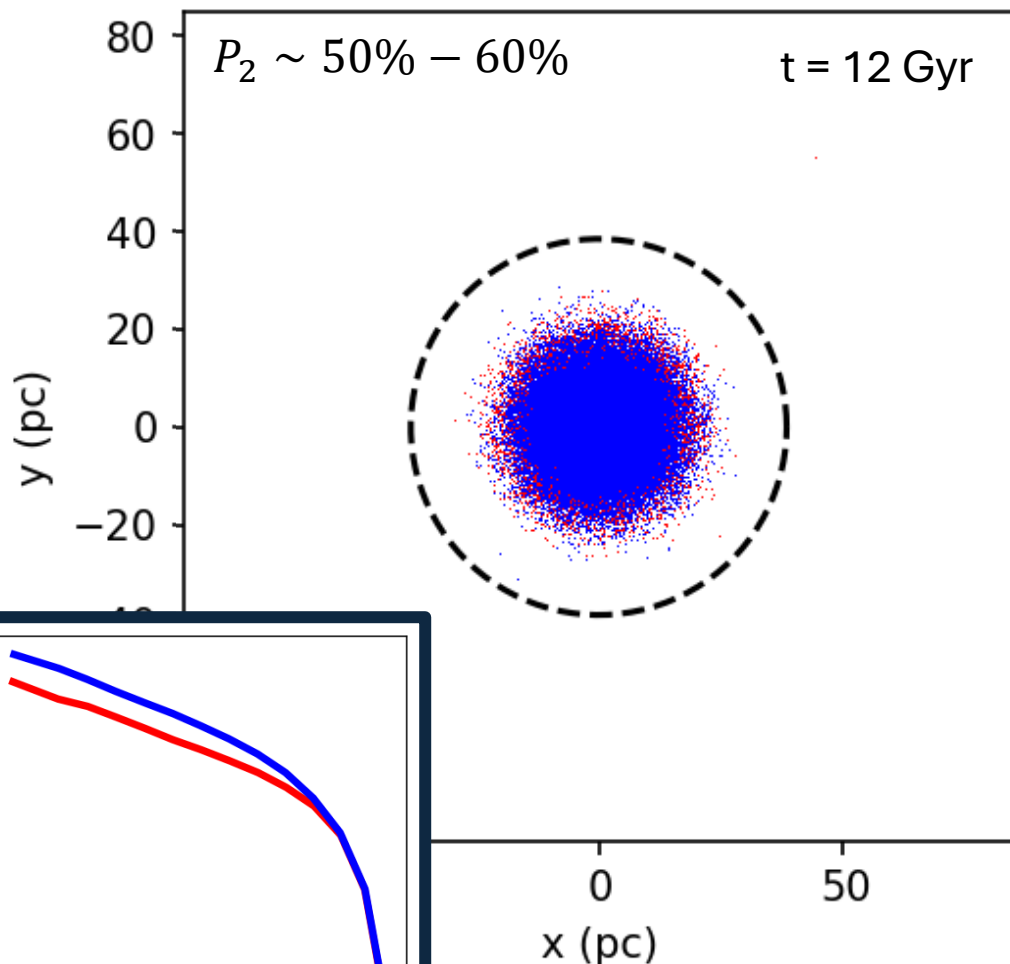
see also Richer et al. (2013); Bellini et al. (2015,2018); Cordero et al. (2017); Milone et al. (2018); Libralato et al.(2019); Cordoni et al. (2020a,b); Dalessandro et al. (2021); Leitinger et al. (2023)

# Numerical simulations

see Vesperini et al. (2021), Livernois et al. (submitted) , Aros et al. (in prep)



Giersz et al. (2013); Hypki et al. (2013)

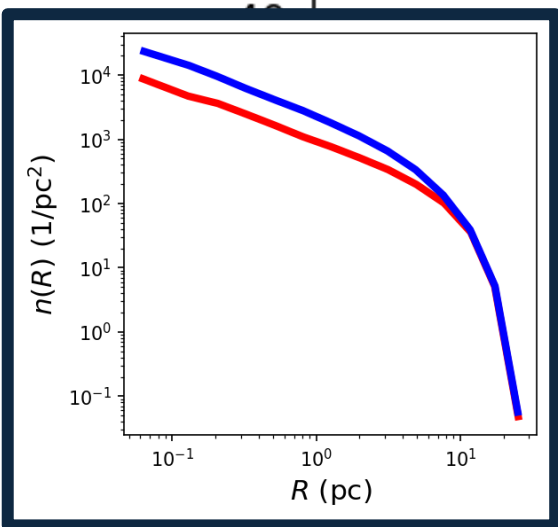


Initial concentration  $> r_{h,P1}/r_{h,P2} = 20,10$

Number of stars  $> 2M, 1M, 500K$

Tidal field  $> \text{strong, weak}$

Primordial anisotropy  $> \text{isotropic, O-M anisotropy}$

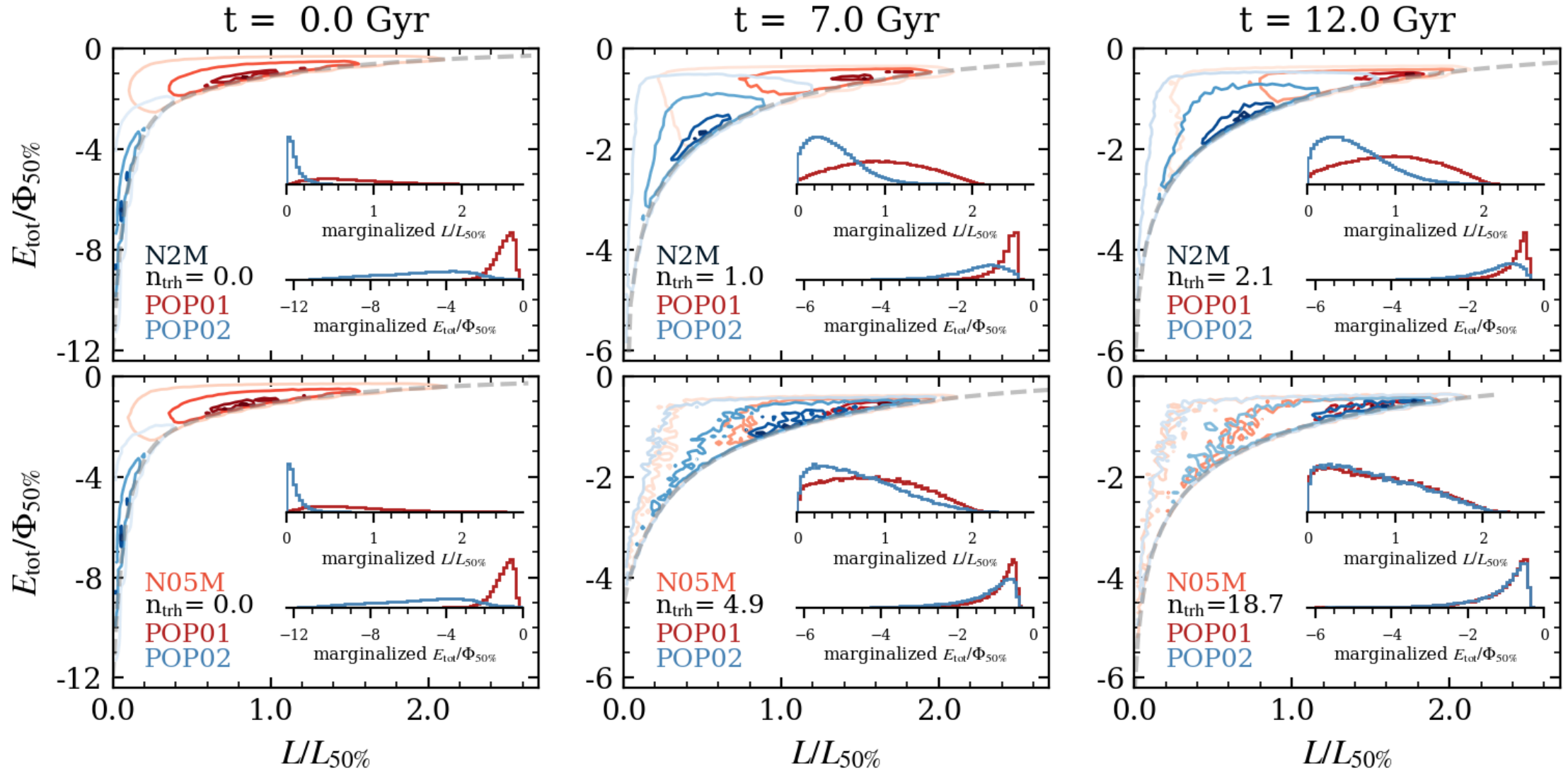


**Non-rotating!**  
For the effects of rotation in GCs with MPOP see the virtual poster presentation by Ethan White!

see also D'Ercole et al. (2008); Bekki (2011); Bekki et al. (2017); Calura et al. (2019); Lacchin et al. (2021, 2022) and Mastrobuono-Battisti & Perets (2013, 2016); Hénault-Brunet et al. (2015); Tiongco et al. (2019); Vesperini et al. (2021); Sollima (2021).

# Mixing in phase-space

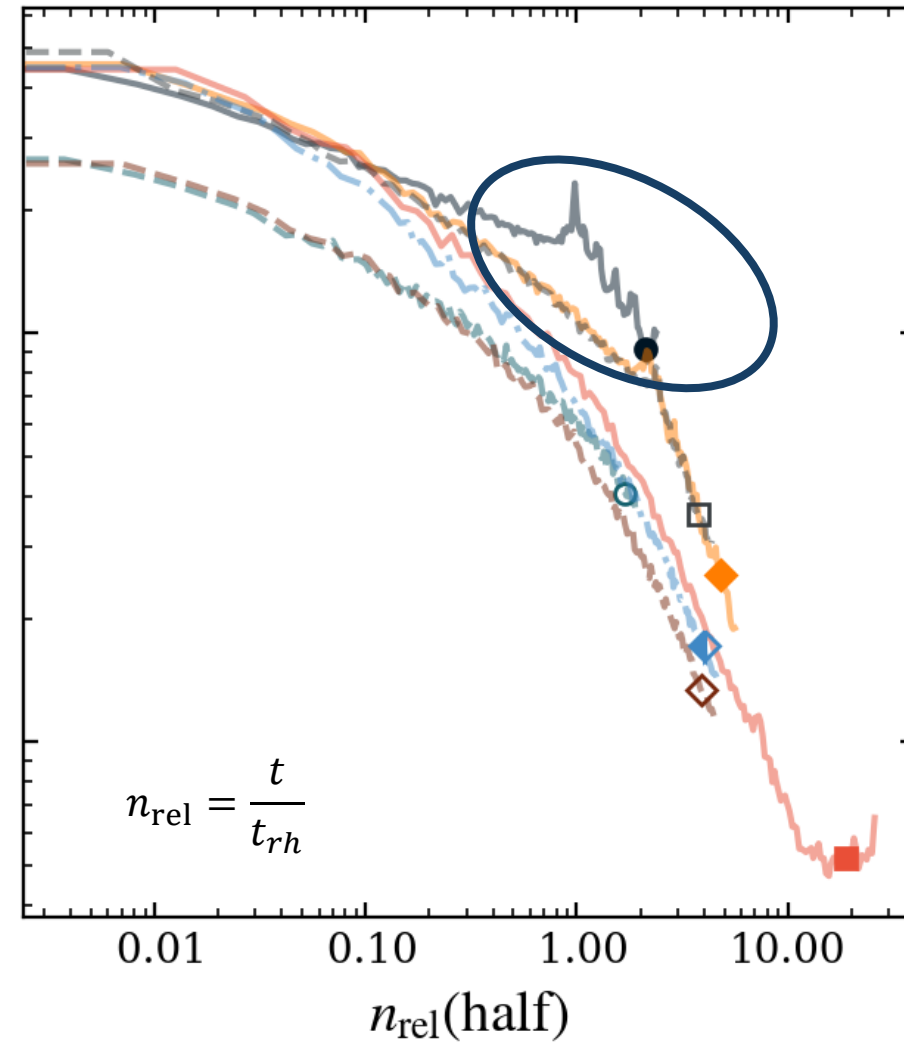
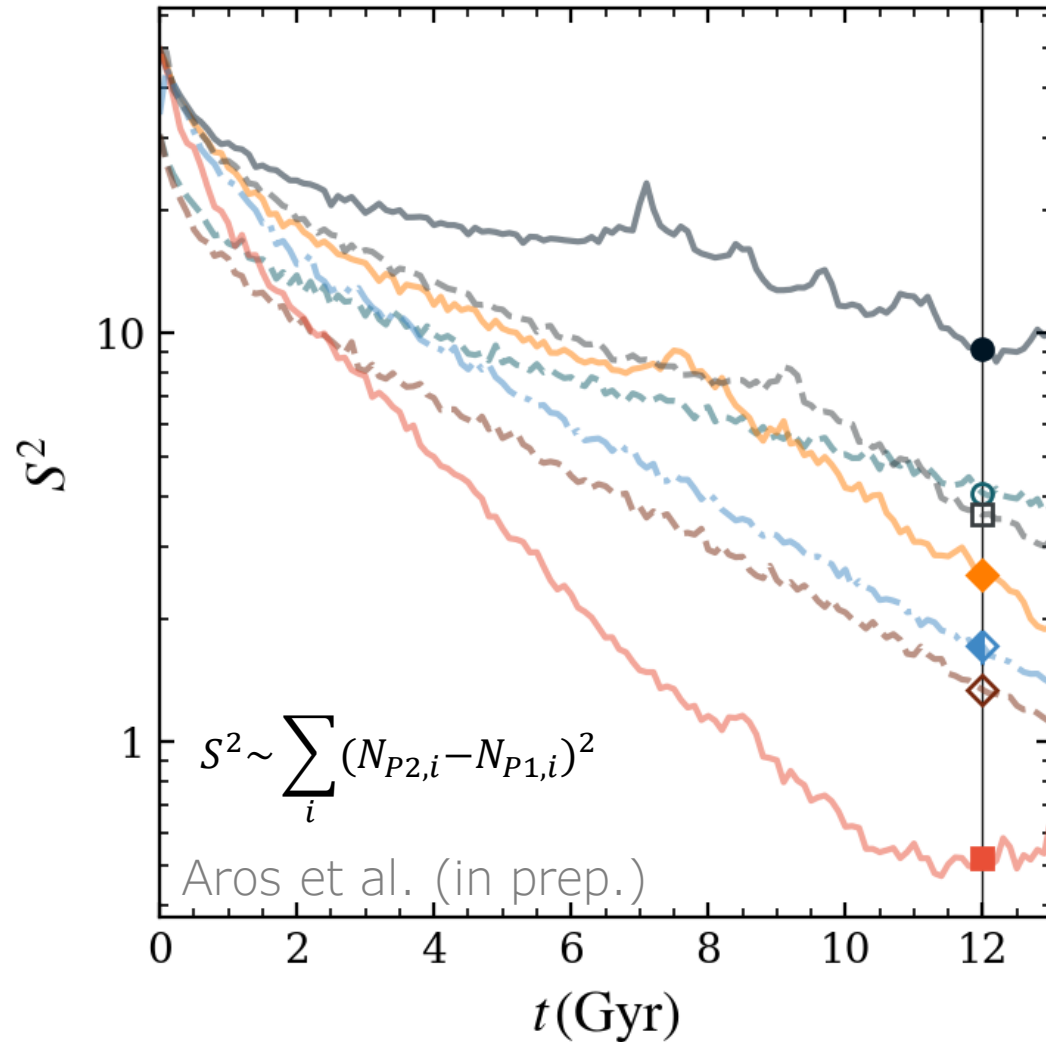
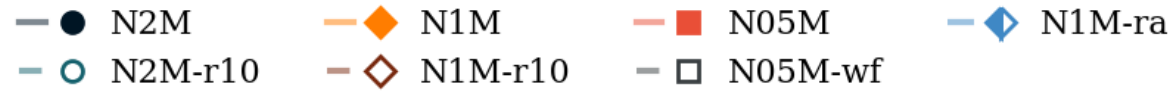
Aros et al. (in prep)



\*the talk included the animated version.

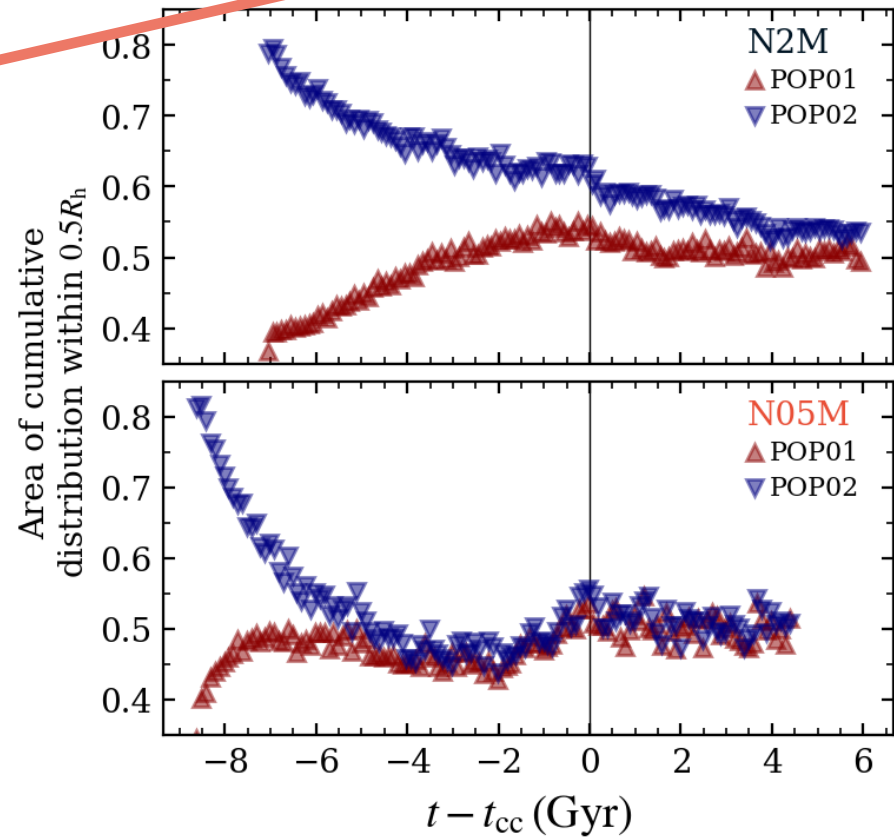
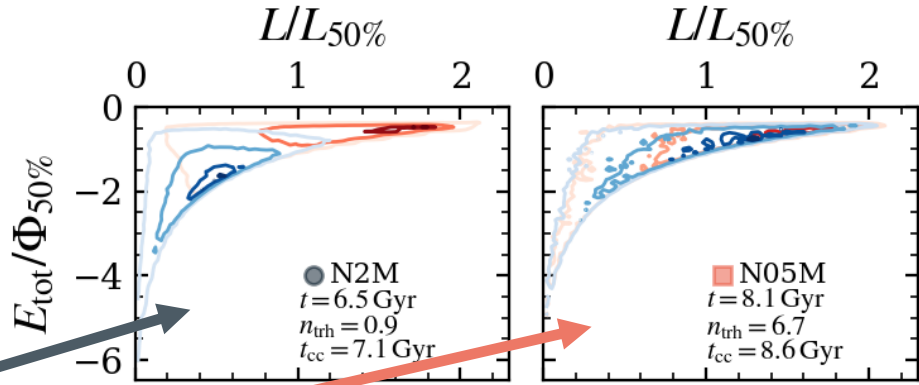
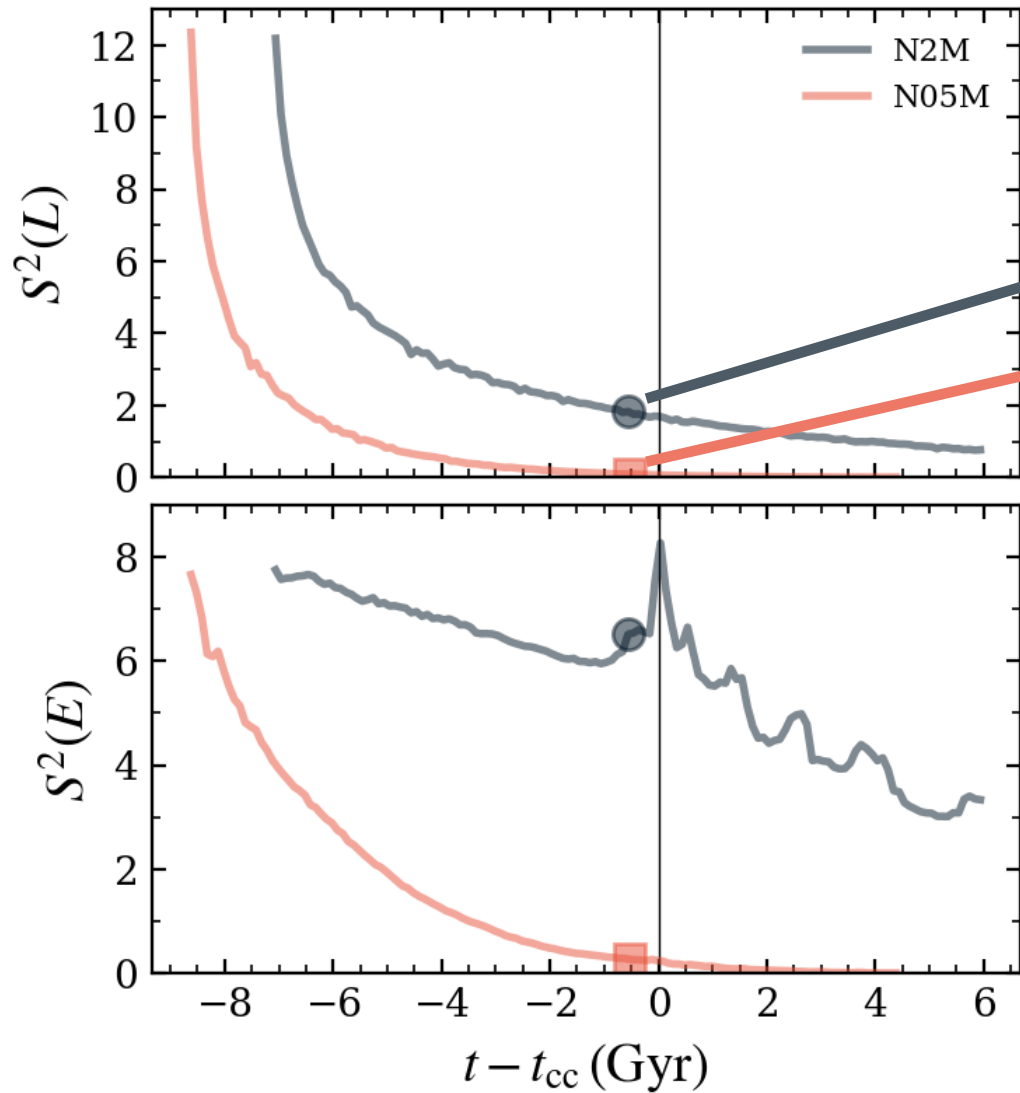
# Quantifying the degree of mixing

Aros et al. (in prep)



# Mixing in energy-space and **spatial mixing**

Aros et al. (in prep)



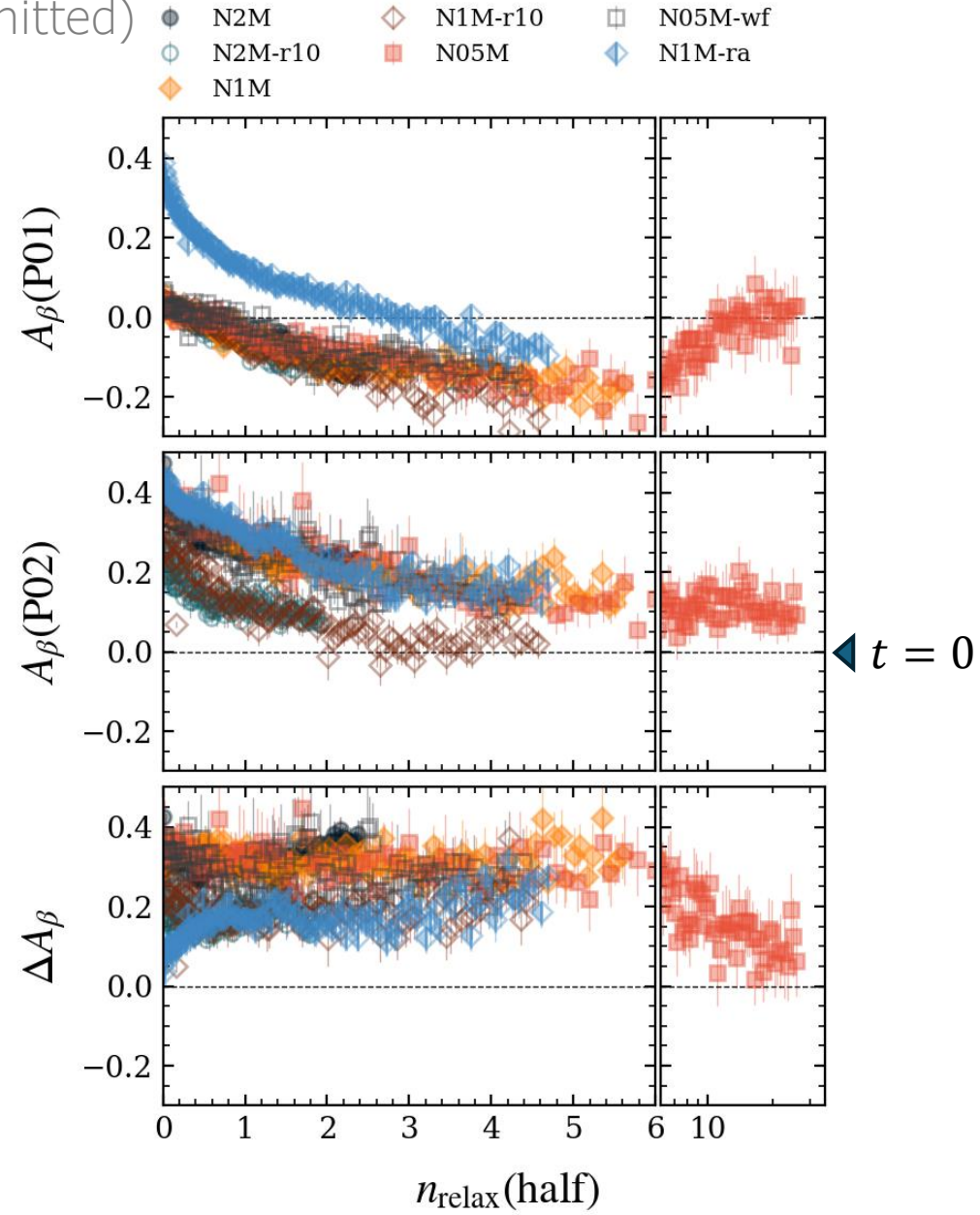
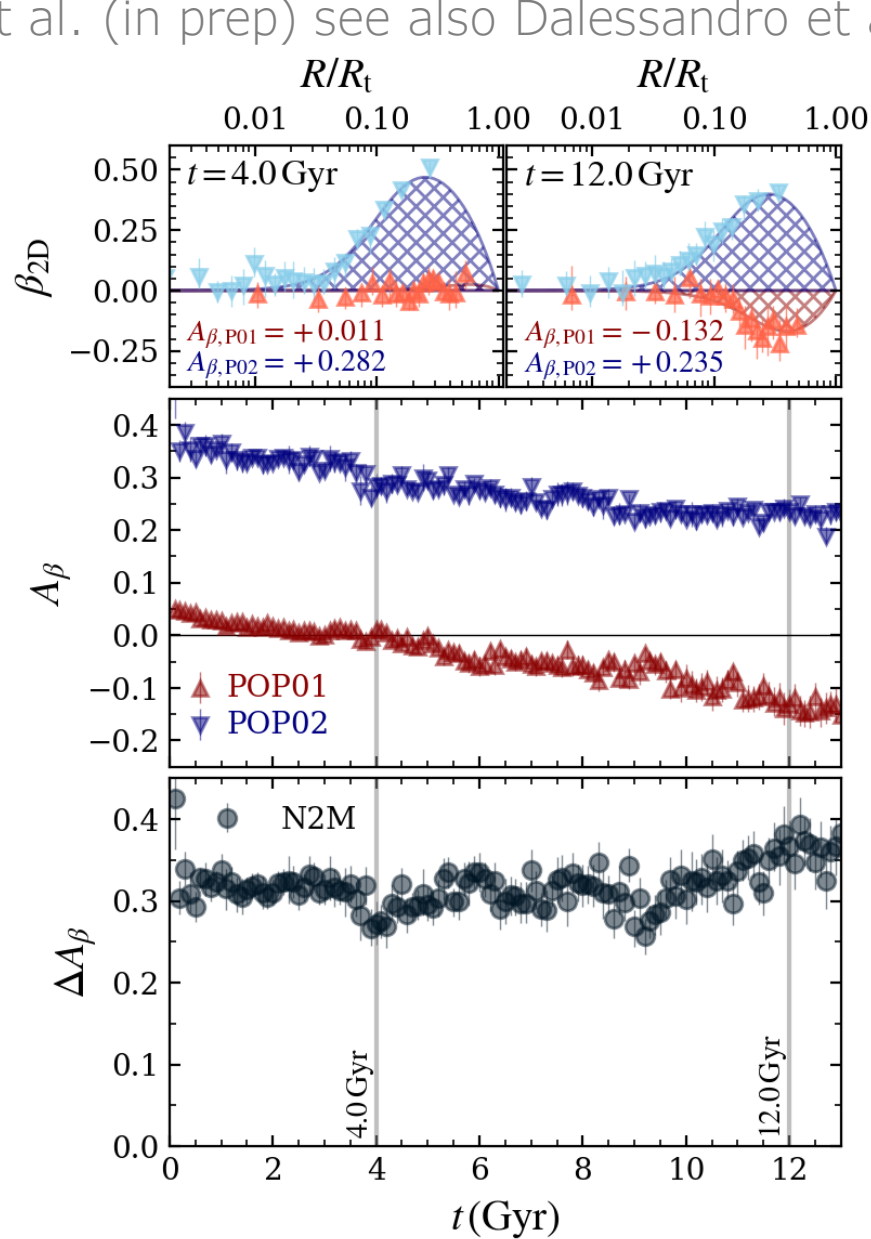
$$f_{P2}(r_{1\%}) = 0.87 (0.52)$$

$$f_{P2}(r_{1\%}) = 0.63 (0.60)$$



# Tracing mixing with the velocity anisotropy

Aros et al. (in prep) see also Dalessandro et al. (submitted)

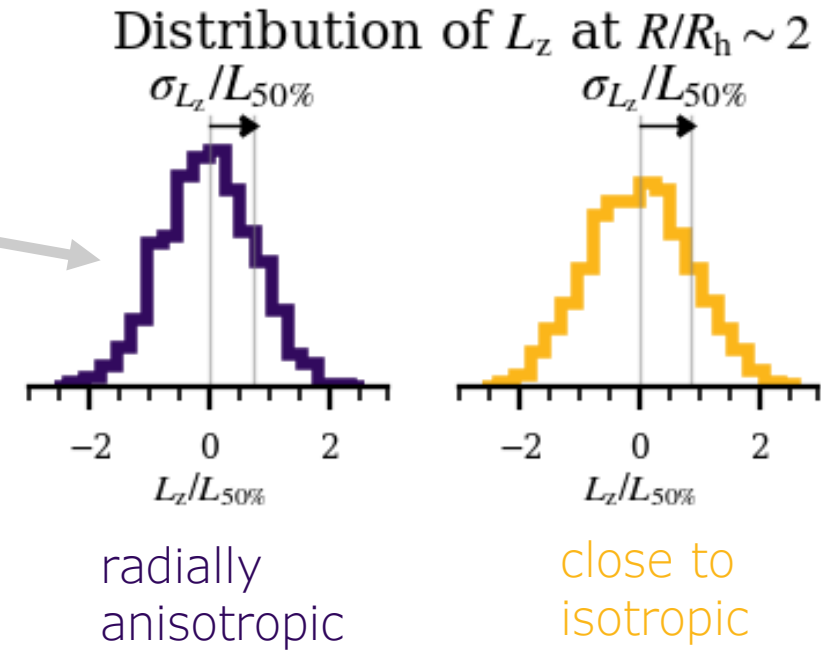
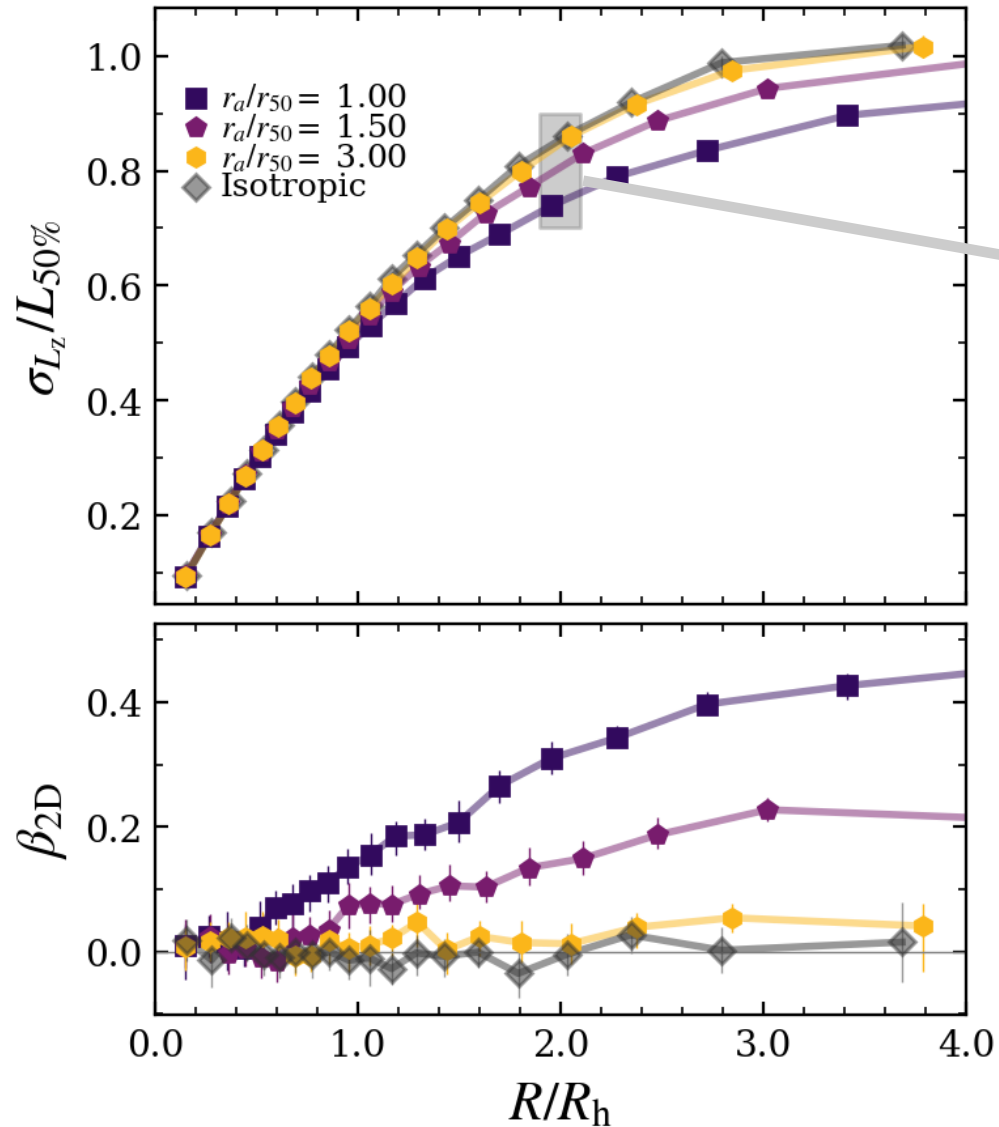


Kinematic mixing



# Velocity anisotropy and angular momentum

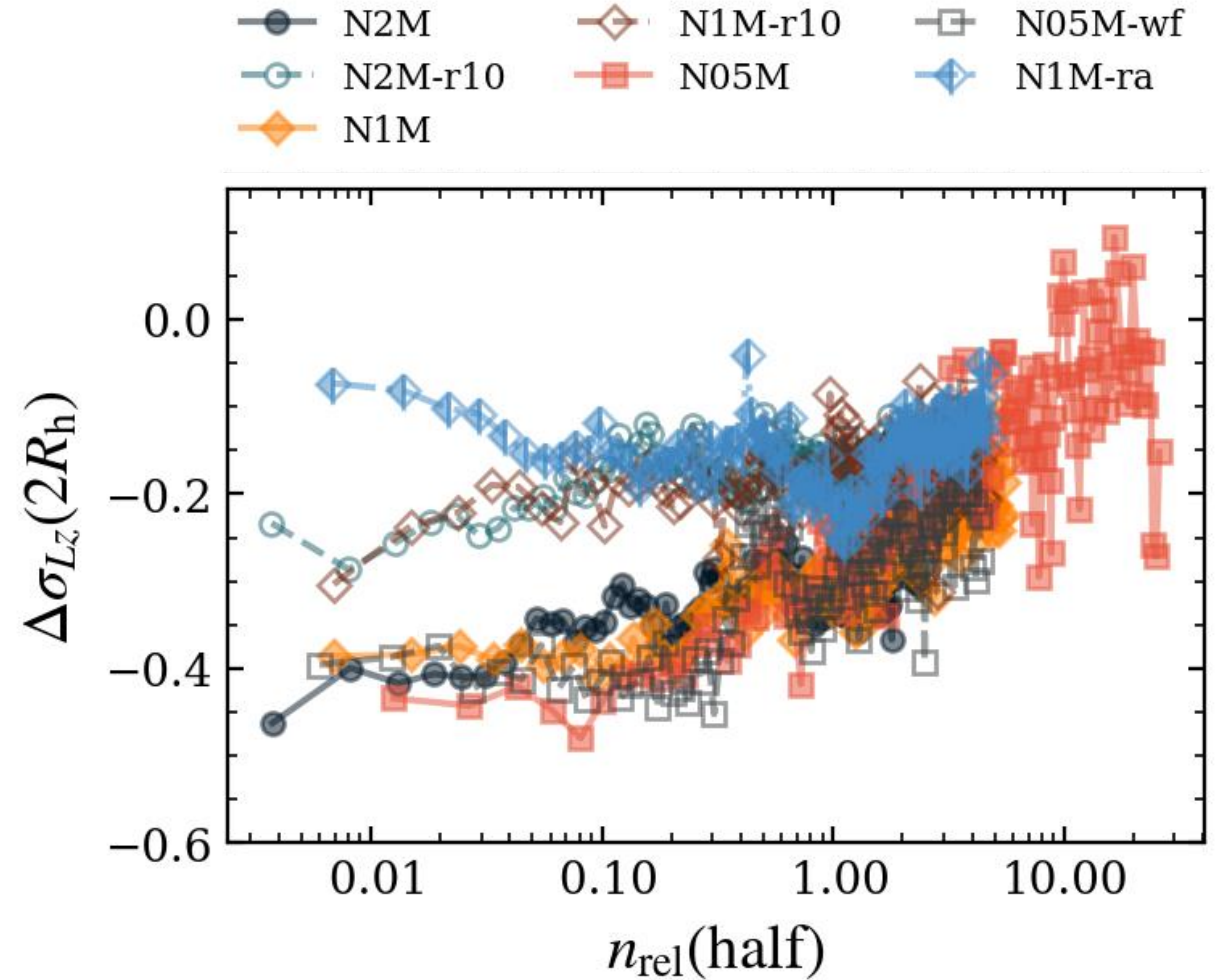
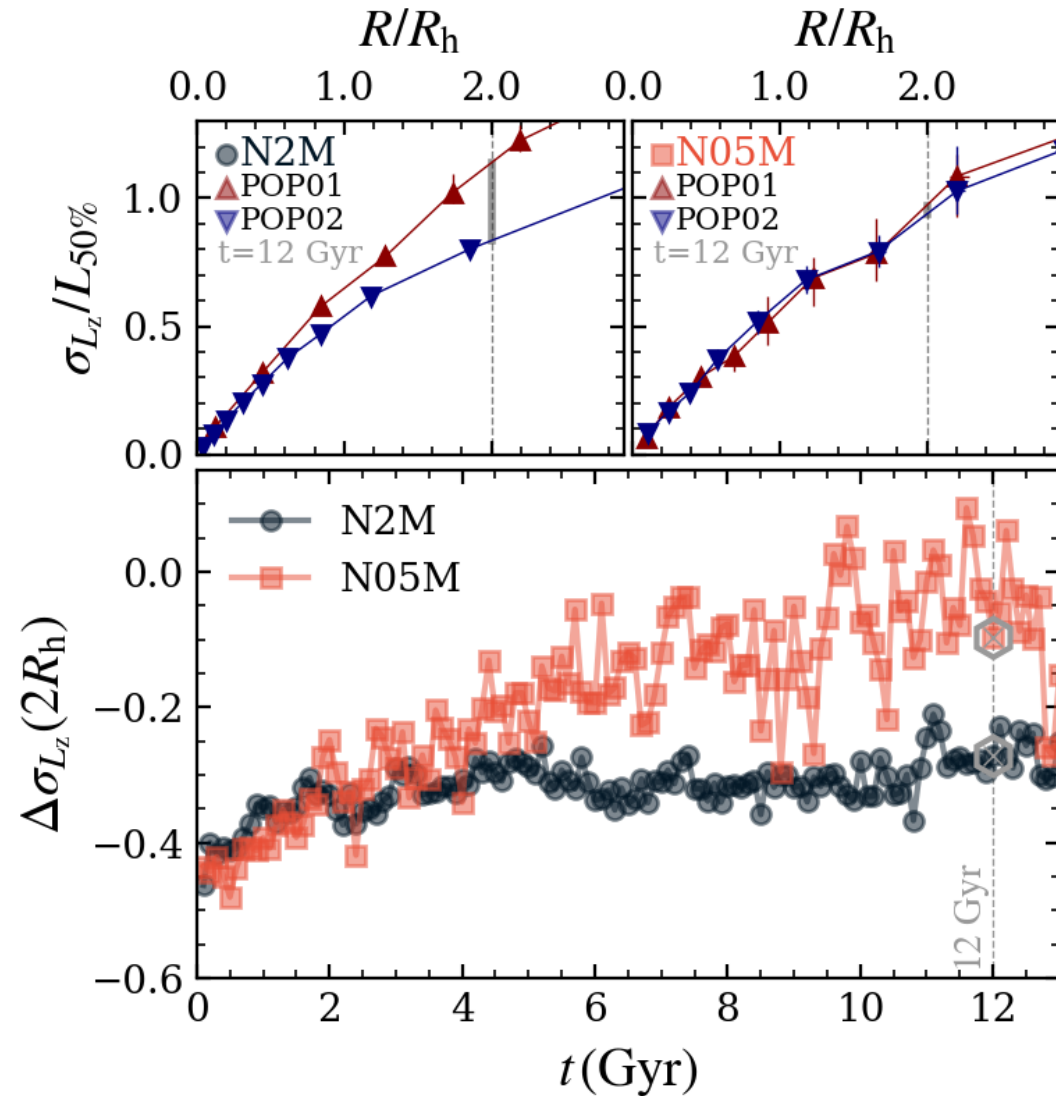
Aros et al. (in prep)



Isotropic and radially anisotropic King models built with `limepy`; see Gieles & Zocchi (2015)

# Tracing mixing with angular momentum

Aros et al. (in prep)



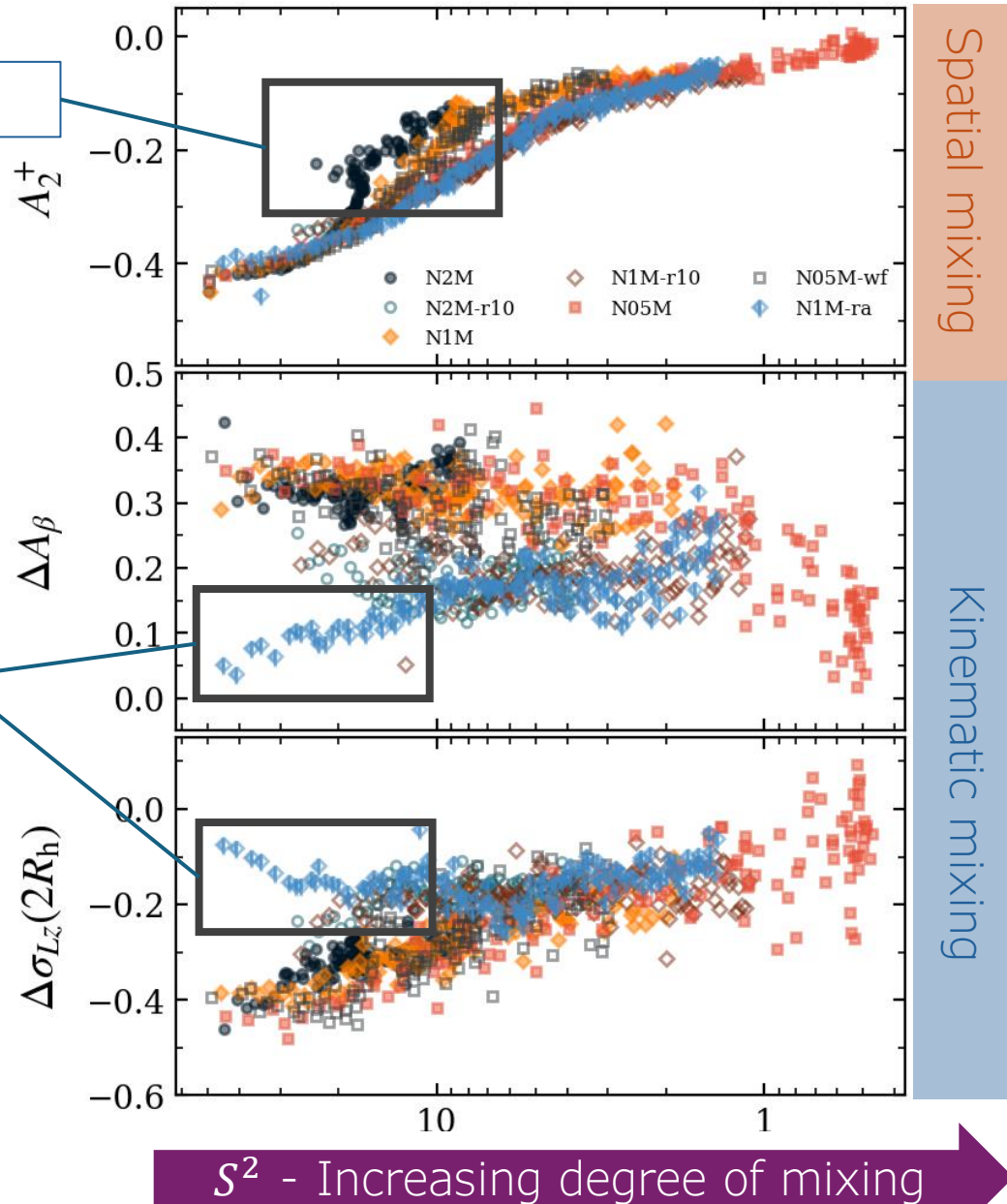
Kinematic mixing

# Phase-space mixing and projected quantities

Aros et al. (in prep)

Core-collapse

Primordial anisotropy



## Summary

> We have a general view of population mixing by looking at the energy-angular momentum space.

> Differences in velocity anisotropy follow the same overall evolution, but they might conserve differences in initial conditions.

> These differences are less apparent on the projected angular momentum distribution (effects of rotation in follow-up work).

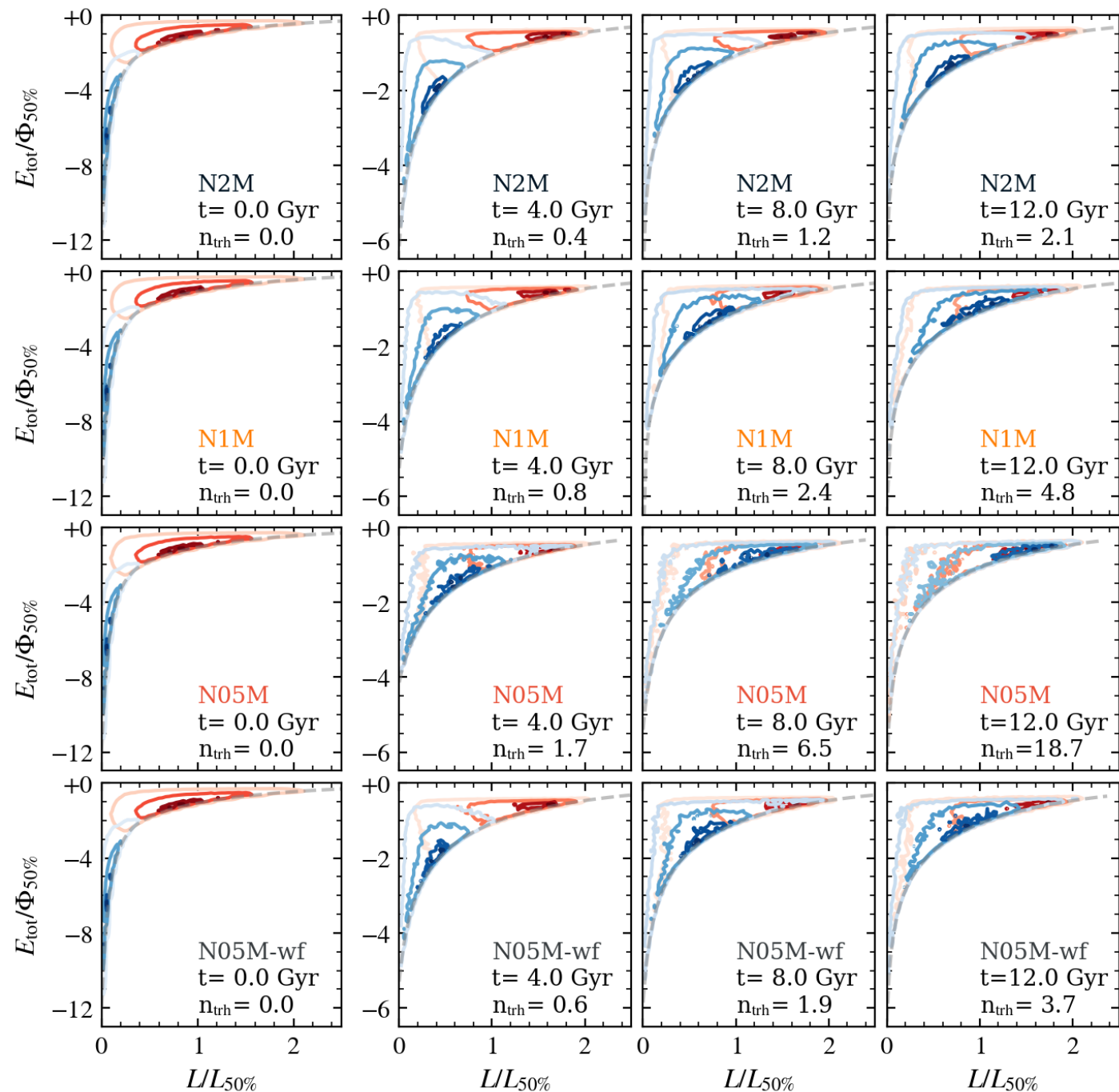
> Spatial and kinematic mixing happens at different rates. We do not see any clear signature of the initial POP02 concentration in the  $A_2^+$  parameter after one relaxation time. Kinematic differences persist for a longer time.



Extra slides

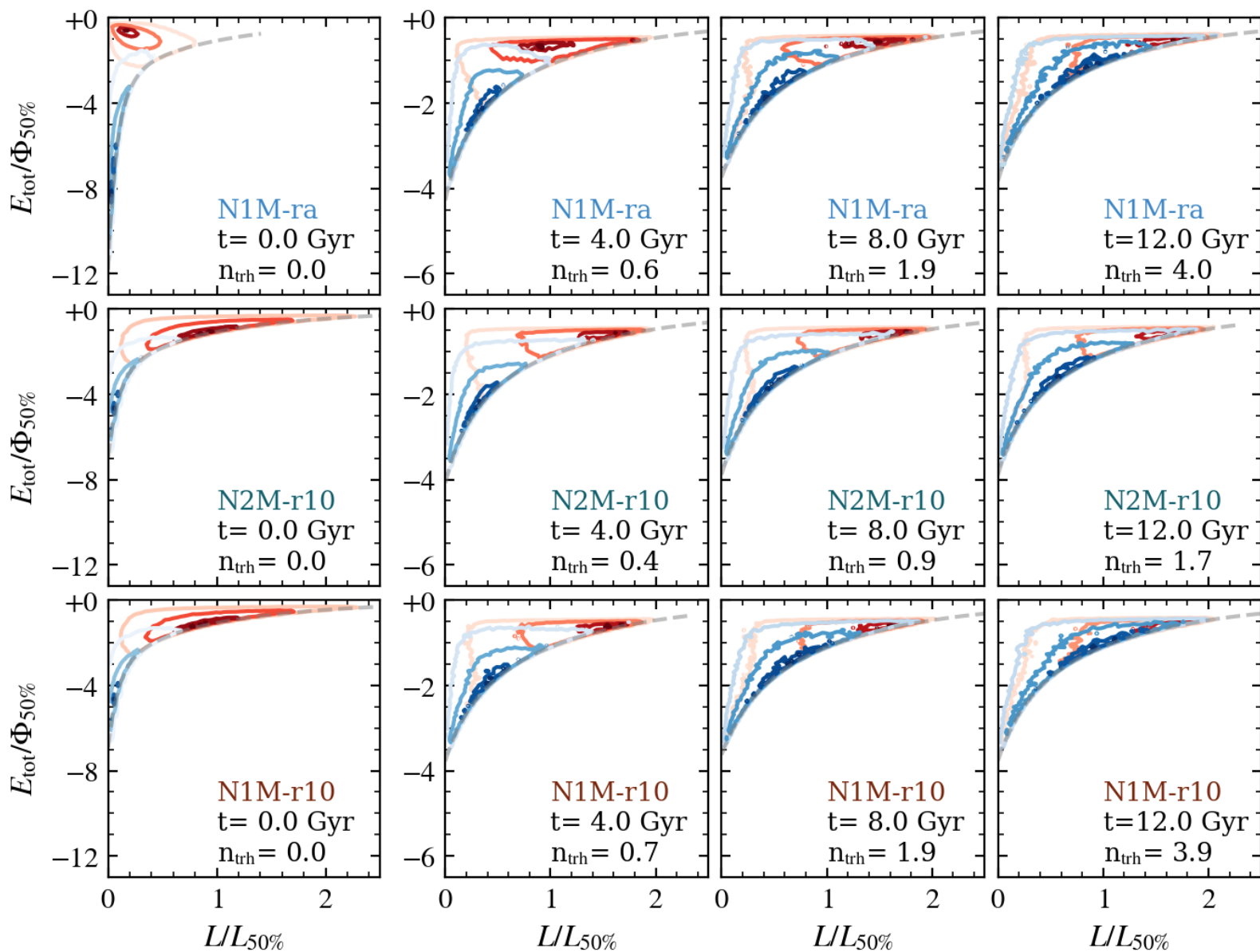
# Phase-space distributions: N2M, N1M, N05M and N05M-wf

Aros et al. (in prep)



# Phase-space distributions: N1M-ra , N2M-r10, N1M-r10

Aros et al. (in prep)





# Evolution of $A_2^+$ Parameter

Aros et al. (in prep)

