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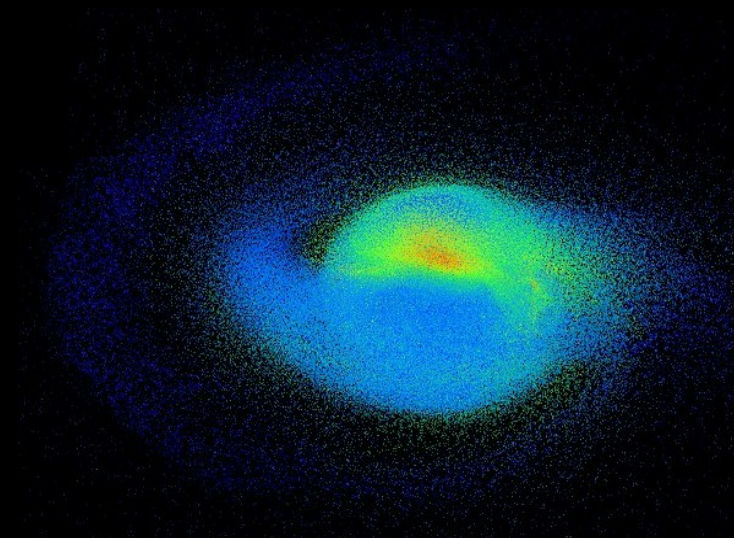
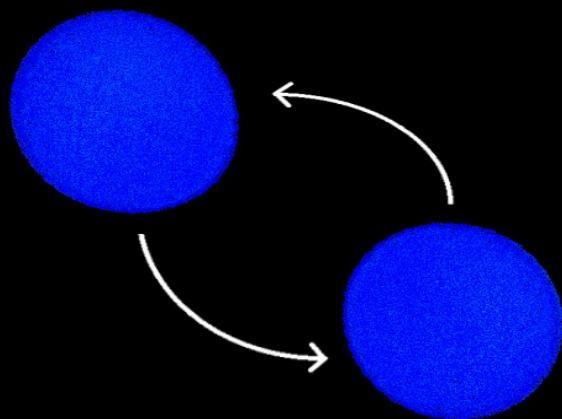
# Neutron star mergers and the high-density equation of state

Astrophysics with GW detections

Warsaw, 07/09/2019

Andreas Bauswein

(GSI Darmstadt)



# Outline

- ▶ Motivation and overview
- ▶ Multi-messenger interpretation of GW170817 → lower limit on NS radii  
→ Collapse behavior (EoS dependence of BH formation)
- ▶ Postmerger GW emission
- ▶ Signatures of the QCD phase transition

# Motivation: Neutron stars and the EoS

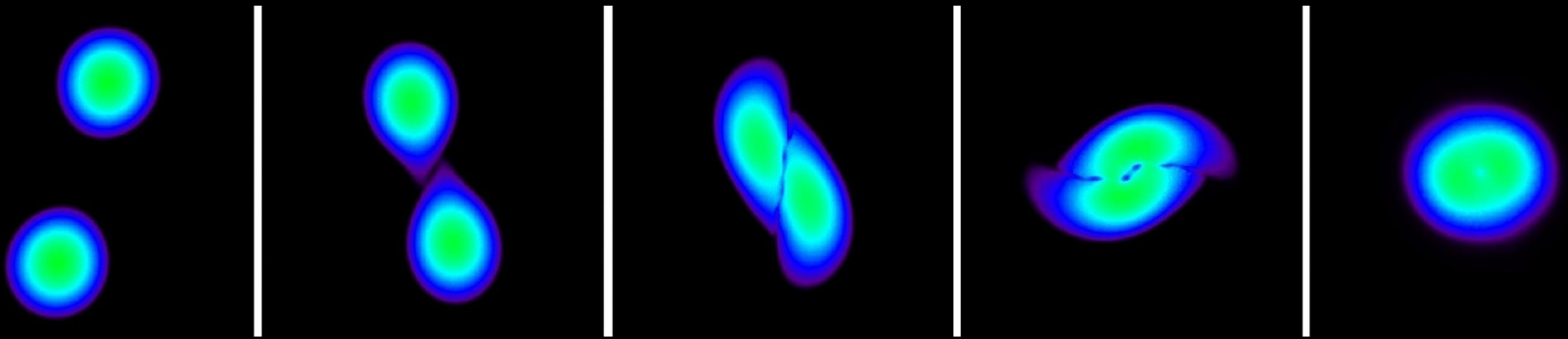
- ▶ Nuclear many-body problem hard to solve (some approximations required)
- ▶ Nuclear interactions not precisely known, especially at higher densities
- ▶ Fundamental constituents of NSs not known: pure nuclear matter, hyperons, ..., possibly phase transition to deconfined quark matter

→ high-density EoS not precisely known

↔ stellar structure of NSs not precisely known - density profile, radii, tidal deformability, maximum mass ???

→ relevant for nuclear/high-density matter physics and astrophysics of NS (NS cooling, SN explosions, NS mass distribution, mass gap, ...)

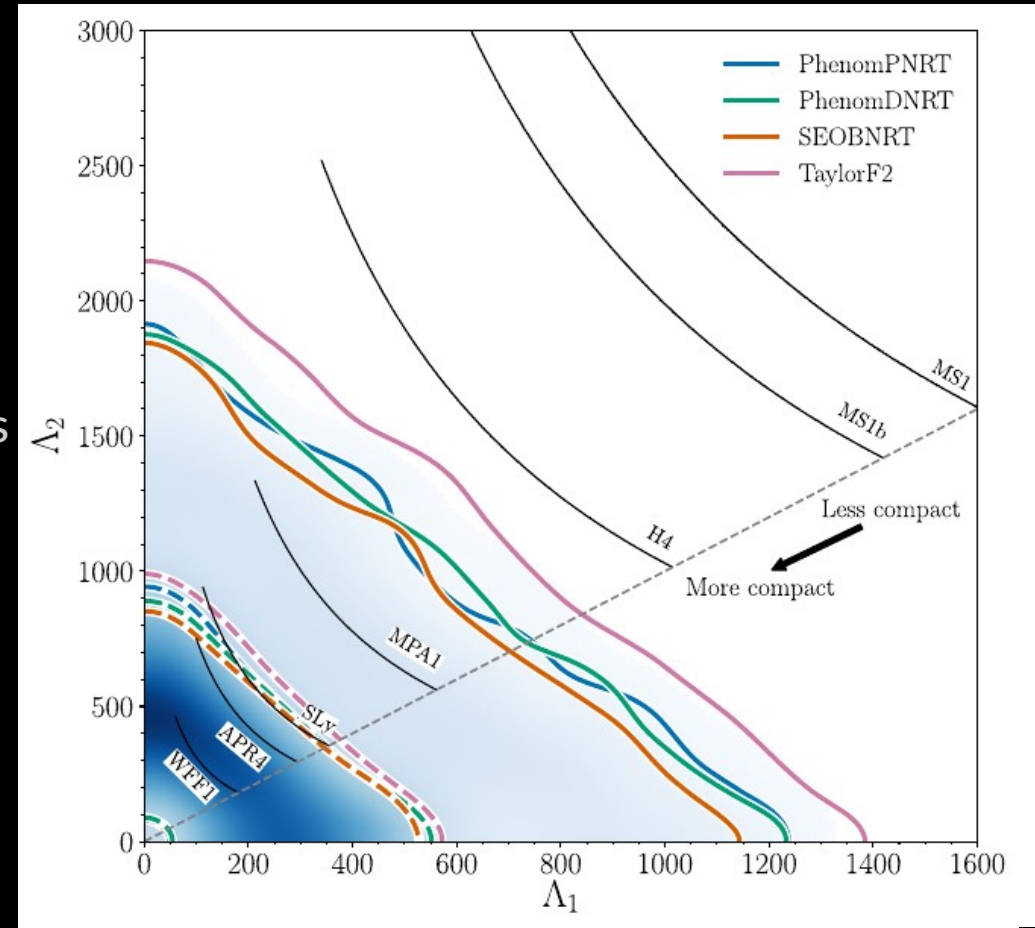
## Finite-size effects during late inspiral



# Measurement

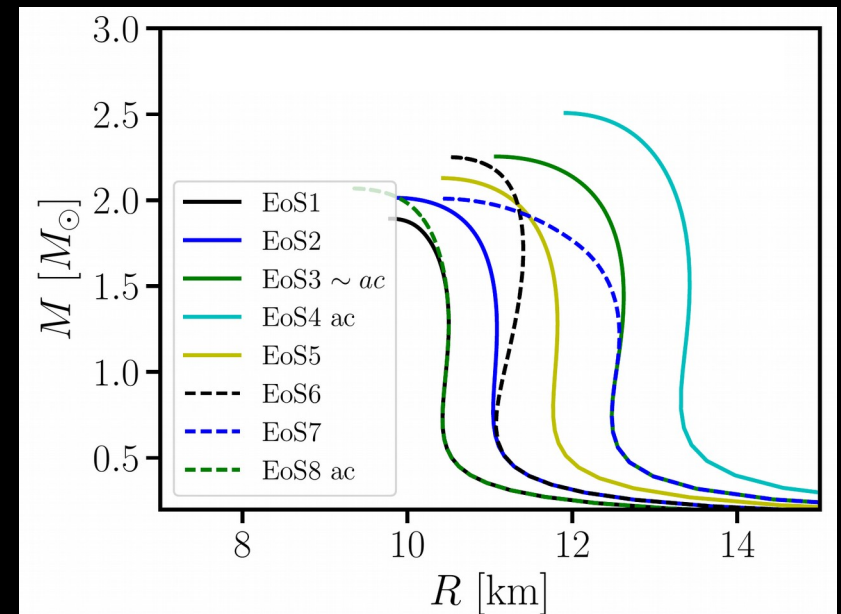
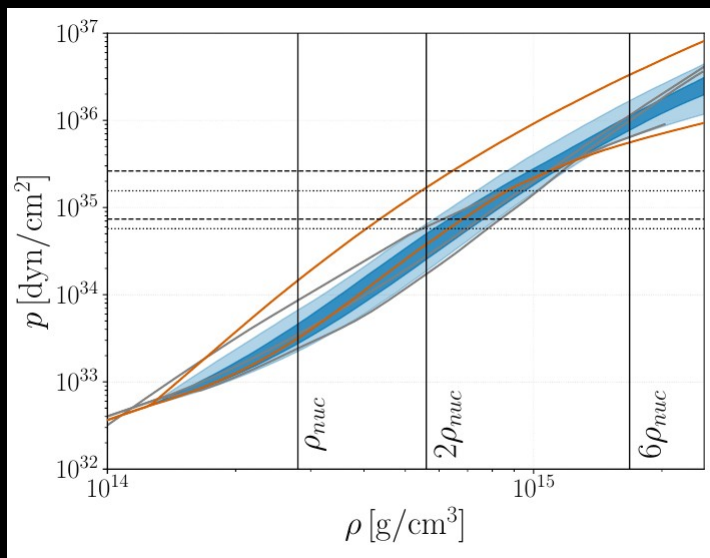
- ▶  $\Lambda < \sim 650$   
→ Means that very stiff EoSs are excluded
- ▶ Somewhat model-dependent
- ▶ Better constraints expected in future as sensitivity increases

$$\tilde{\Lambda} = \frac{16(m_1 + 12m_2)m_1^4\Lambda_1 + (m_2 + 12m_1)m_2^4\Lambda_2}{(m_1 + m_2)^5}$$



Abbott et al. 2017, 2019  
see also later publications by Ligo/Virgo  
collaboration, De et al. 2018

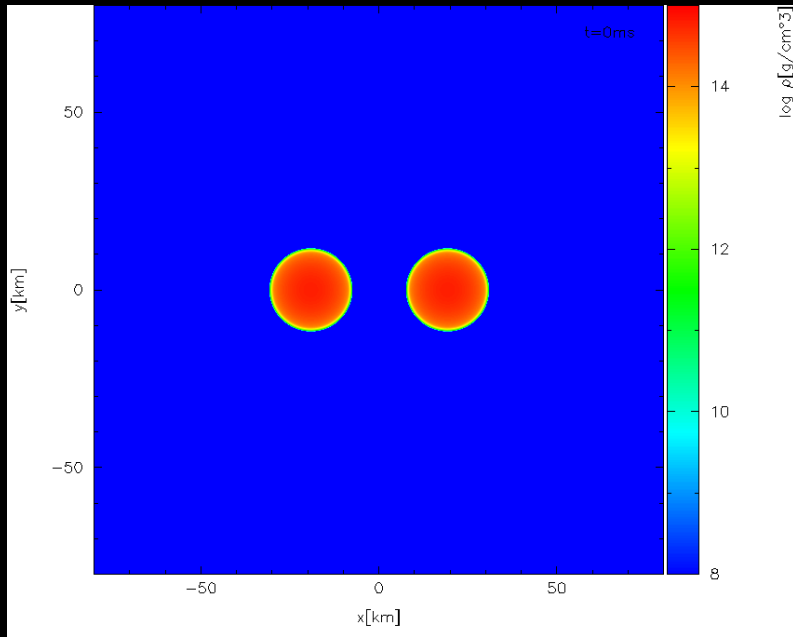
- ▶ Current constraints from LIGO/Virgo through tidal effects during inspiral
- ▶ Recall strong correlation between tidal deformability and NS radius
- ▶ Current constraints roughly compatible with current knowledge from chiral EFT (depending on cut off, e.g. Tews et al 2018)



Ligo/Virgo collaboration 2018

Torres-Riva et al 2019

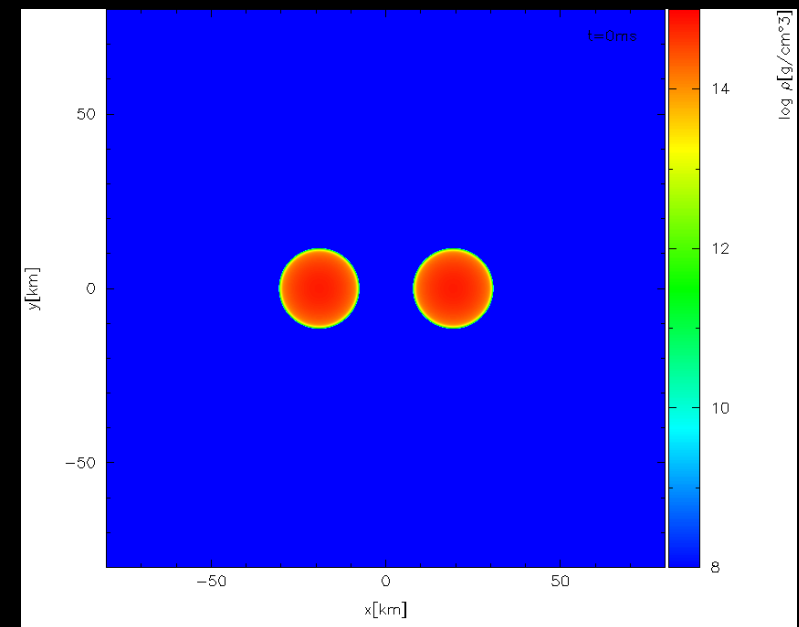
# Collapse behavior and multi-messenger EoS constraints



$$M_{\text{tot}} = 3.4 M_{\odot}$$



$$M_{\text{tot}} = 3.5 M_{\odot}$$



Shen EoS

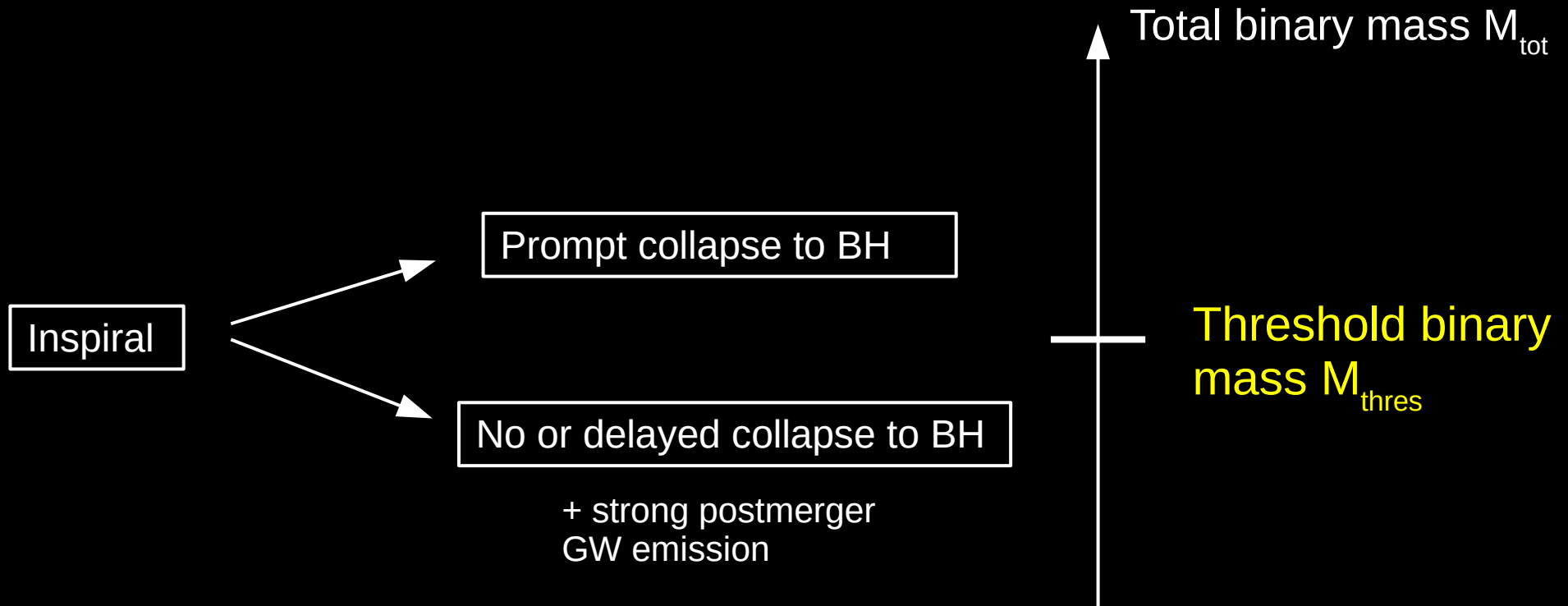
$$\longrightarrow M_{\text{thres}} = (3.45 \pm 0.05) M_{\odot} \quad (\text{for this particular EoS})$$

## Collapse behavior: Prompt vs. delayed (/no) BH formation

Relevant for: EoS constraints through  $M_{\text{max}}$  measurement, Conditions for short GRBs, Mass ejection, Electromagnetic counterparts powered by thermal emission, NS radius constraints !!!



# Collapse behavior



EoS dependent - somehow  $M_{\text{max}}$  should play a role

# Simulations reveal $M_{\text{thres}}$

TOV properties of nonrotating  
stars, i.e. EoS characteristics

Merger property from  
simulations

EoS	$M_{\text{max}}$ ( $M_{\odot}$ )	$R_{\text{max}}$ (km)	$C_{\text{max}}$	$R_{1.6}$ (km)	$M_{\text{thres}}$ ( $M_{\odot}$ )
NL3 [37,38]	2.79	13.43	0.307	14.81	3.85
GS1 [39]	2.75	13.27	0.306	14.79	3.85
LS375 [40]	2.71	12.34	0.325	13.71	3.65
DD2 [38,41]	2.42	11.90	0.300	13.26	3.35
Shen [42]	2.22	13.12	0.250	14.46	3.45
TM1 [43,44]	2.21	12.57	0.260	14.36	3.45
SFHX [45]	2.13	10.76	0.292	11.98	3.05
GS2 [46]	2.09	11.78	0.262	13.31	3.25
SFHO [45]	2.06	10.32	0.294	11.76	2.95
LS220 [40]	2.04	10.62	0.284	12.43	3.05
TMA [44,47]	2.02	12.09	0.247	13.73	3.25
IUF [38,48]	1.95	11.31	0.255	12.57	3.05

Bauswein et al. 2013

Smooth particle hydrodynamics + conformal flatness

# Threshold binary mass

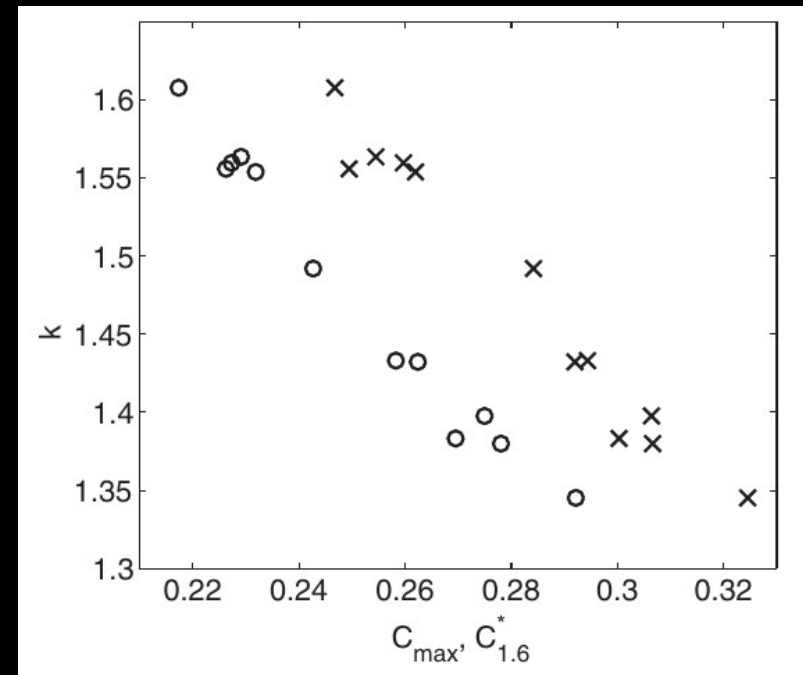
- ▶ Empirical relation from simulations with different  $M_{\text{tot}}$  and EoS
- ▶ Fits (to good accuracy):

$$M_{\text{thres}} = M_{\text{thres}}(M_{\text{max}}, R_{\text{max}}) = \left( -3.38 \frac{GM_{\text{max}}}{c^2 R_{\text{max}}} + 2.43 \right) M_{\text{max}}$$

$$M_{\text{thres}} = M_{\text{thres}}(M_{\text{max}}, R_{1.6}) = \left( -3.6 \frac{G M_{\text{max}}}{c^2 R_{1.6}} + 2.38 \right) M_{\text{max}}$$

- ▶ Both better than  $0.06 M_{\text{sun}}$ ,  
(meanwhile more ~20 models)

$$k = M_{\text{thres}}/M_{\text{max}}$$



# EoS constraints from GW170817\*

→ lower bound on NS radii

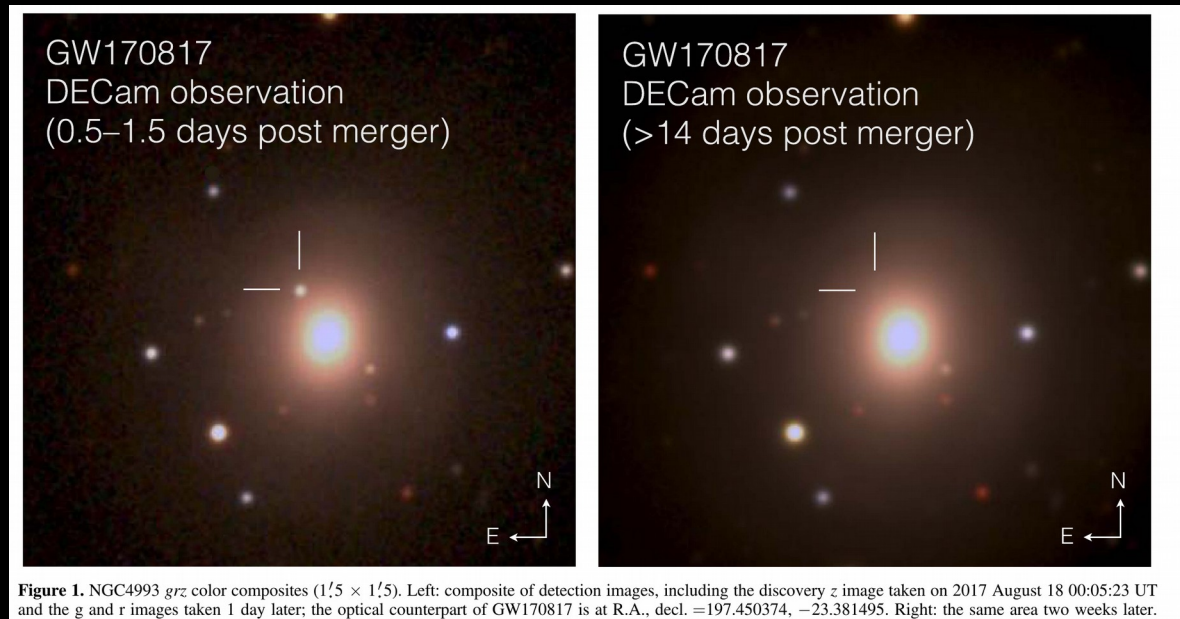
(recall: upper bound from tidal deformability)

\* See also Margalit & Metzger 2017, Shibata et al. 2017, Radice et al. 2018, Rezzolla et al. 2018, Ruiz & Shapiro 2018, ... for other EoS constraints in the context of GW170817

# A simple but robust NS radius constraint from GW170817

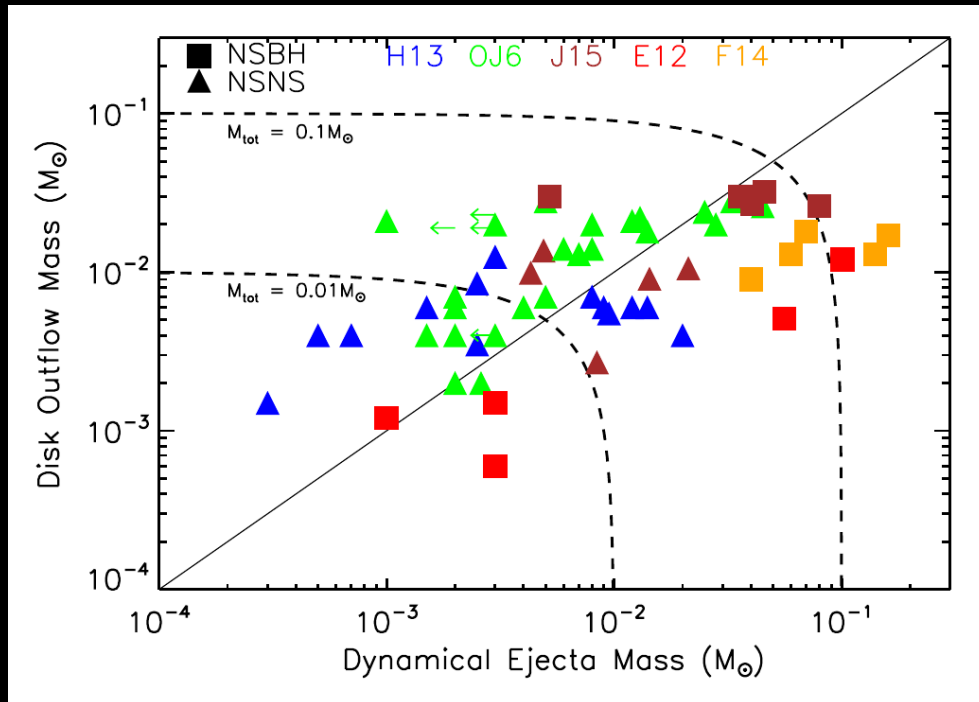
- High ejecta mass inferred from electromagnetic transient  
(high compared to simulations)
- provides strong support for a delayed/no collapse in GW170817
- even asymmetric mergers that directly collapse do not produce such massive ejecta

Reference	$m_{\text{dyn}} [M_{\odot}]$	$m_{\text{w}} [M_{\odot}]$
Abbott et al. (2017a)	0.001 – 0.01	–
Arcavi et al. (2017)	–	0.02 – 0.025
Cowperthwaite et al. (2017)	0.04	0.01
Chornock et al. (2017)	0.035	0.02
Evans et al. (2017)	0.002 – 0.03	0.03 – 0.1
Kasen et al. (2017)	0.04	0.025
Kasliwal et al. (2017b)	> 0.02	> 0.03
Nicholl et al. (2017)	0.03	–
Perego et al. (2017)	0.005 – 0.01	$10^{-5}$ – 0.024
Rosswog et al. (2017)	0.01	0.03
Smartt et al. (2017)	0.03 – 0.05	0.018
Tanaka et al. (2017a)	0.01	0.03
Tanvir et al. (2017)	0.002 – 0.01	0.015
Troja et al. (2017)	0.001 – 0.01	0.015 – 0.03



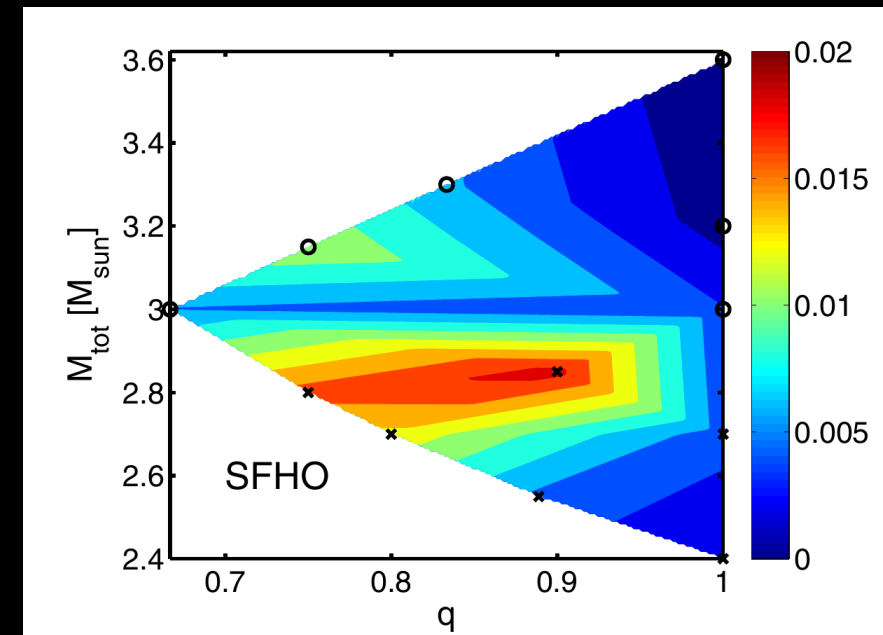
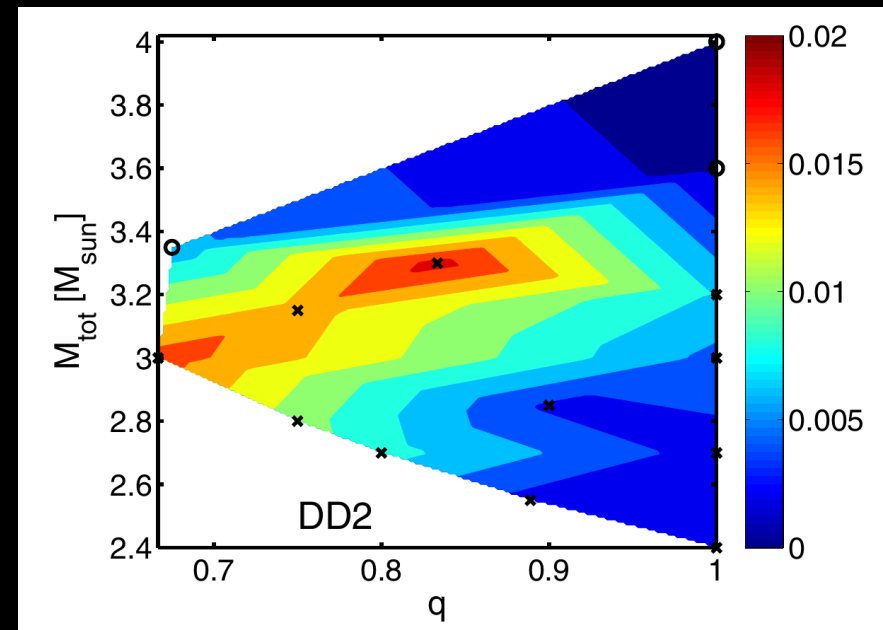
Soares-Santos et al 2017

- ▶ Ejecta masses depend on EoS and binary masses
- ▶ Note: high mass points already to soft EoS (tentatively/qualitatively)
- ▶ Prompt collapse leads to reduced ejecta mass
- ▶ Light curve depends on ejecta mass:  
→ 0.02 - 0.05  $M_{\text{sun}}$  point to delayed collapse



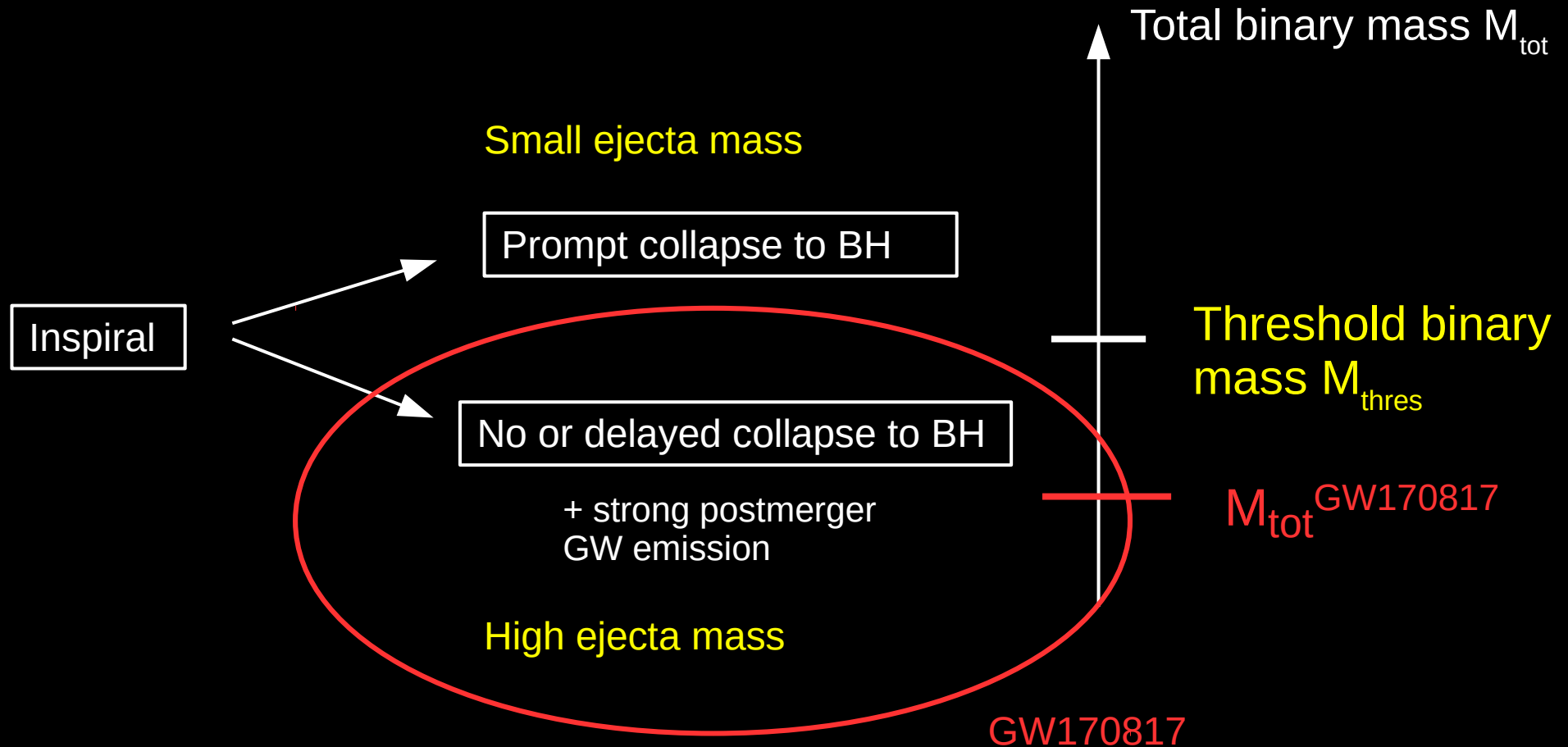
Compilation Wu et al 2016: dynamical and secular ejecta comparable

Only dynamical ejecta



Bauswein et al. 2013

# Collapse behavior



(1) If GW170817 was a delayed (/no) collapse:

$$M_{\text{thres}} > M_{\text{tot}}^{\text{GW170817}}$$

(2) Recall: empirical relation for threshold binary mass for prompt collapse:

$$M_{\text{thres}} = \left( -3.38 \frac{G M_{\text{max}}}{c^2 R_{\text{max}}} + 2.43 \right) M_{\text{max}} > 2.74 M_{\odot}$$

(with  $M_{\text{max}}$ ,  $R_{\text{max}}$  unknown)

(3) Causality: speed of sound  $v_s \leq c$

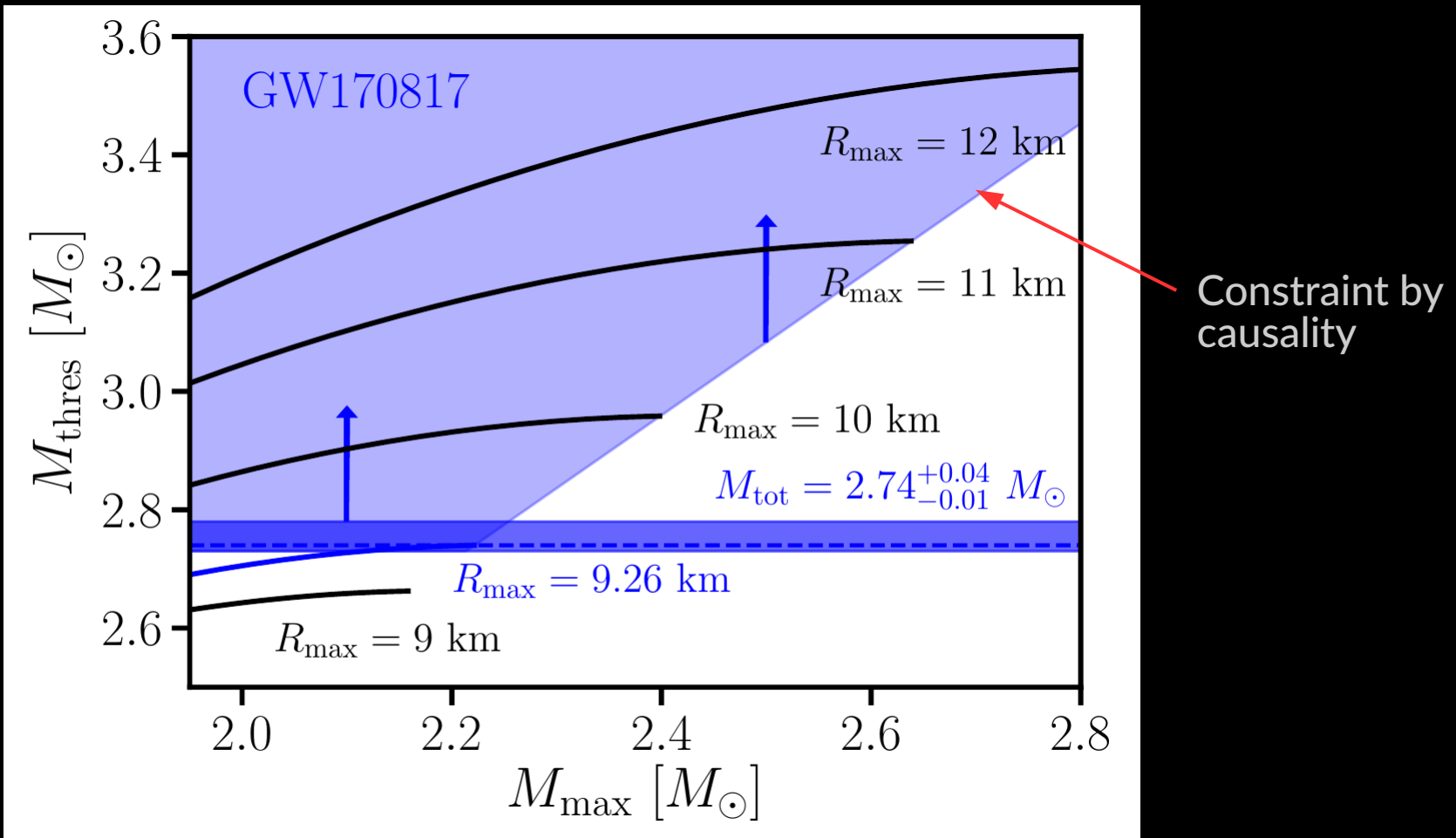
$$\Rightarrow M_{\text{max}} \leq \frac{1}{2.82} \frac{c^2 R_{\text{max}}}{G}$$

► Putting things together:

$$M_{\text{tot}}^{\text{GW170817}} \leq \left( -3.38 \frac{G M_{\text{max}}}{c^2 R_{\text{max}}} + 2.43 \right) M_{\text{max}} \leq \left( -\frac{3.38}{2.82} + 2.43 \right) \frac{1}{2.82} \frac{c^2 R_{\text{max}}}{G}$$

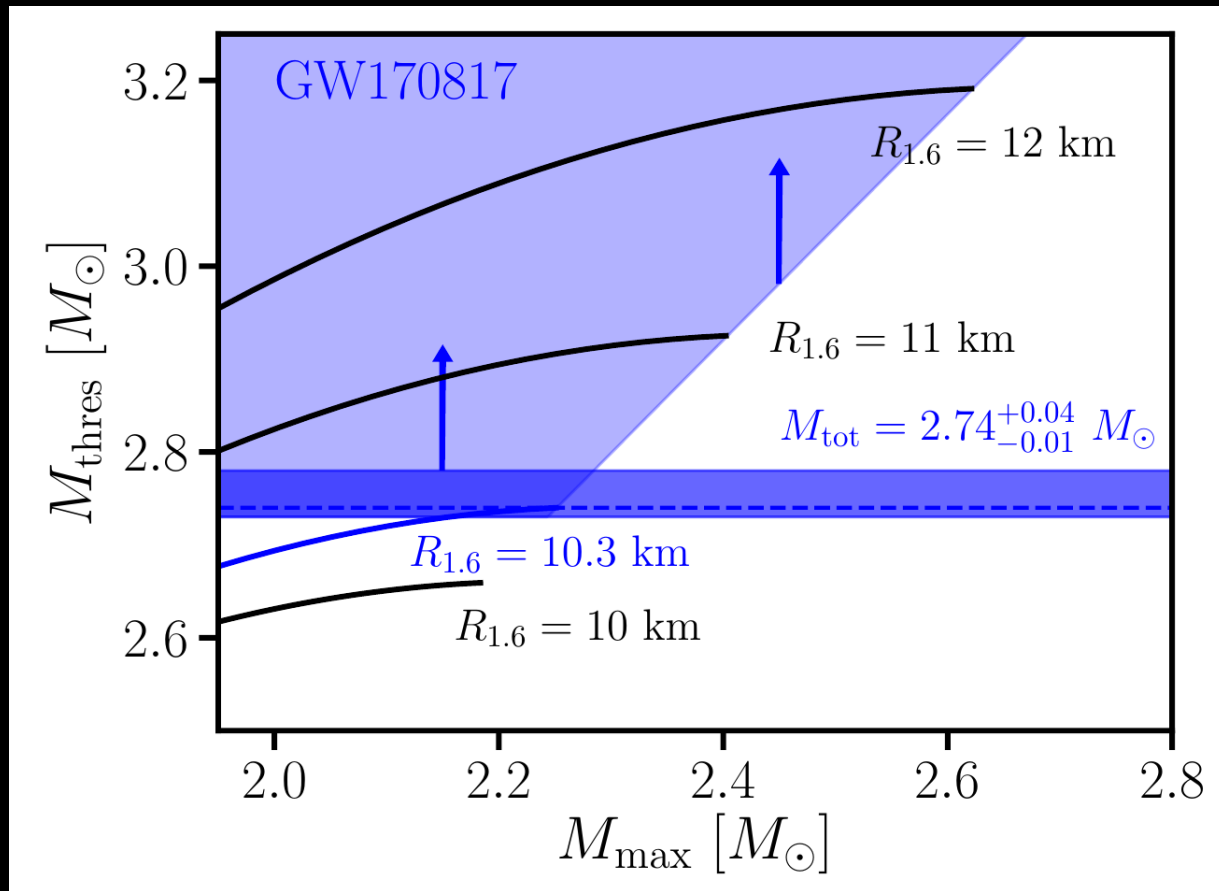
→ Lower limit on NS radius





$$M_{\text{thres}} = \left( -3.38 \frac{GM_{\text{max}}}{c^2 R_{\text{max}}} + 2.43 \right) M_{\text{max}}$$

$$M_{\text{thres}} \geq 1.2 M_{\text{max}}$$

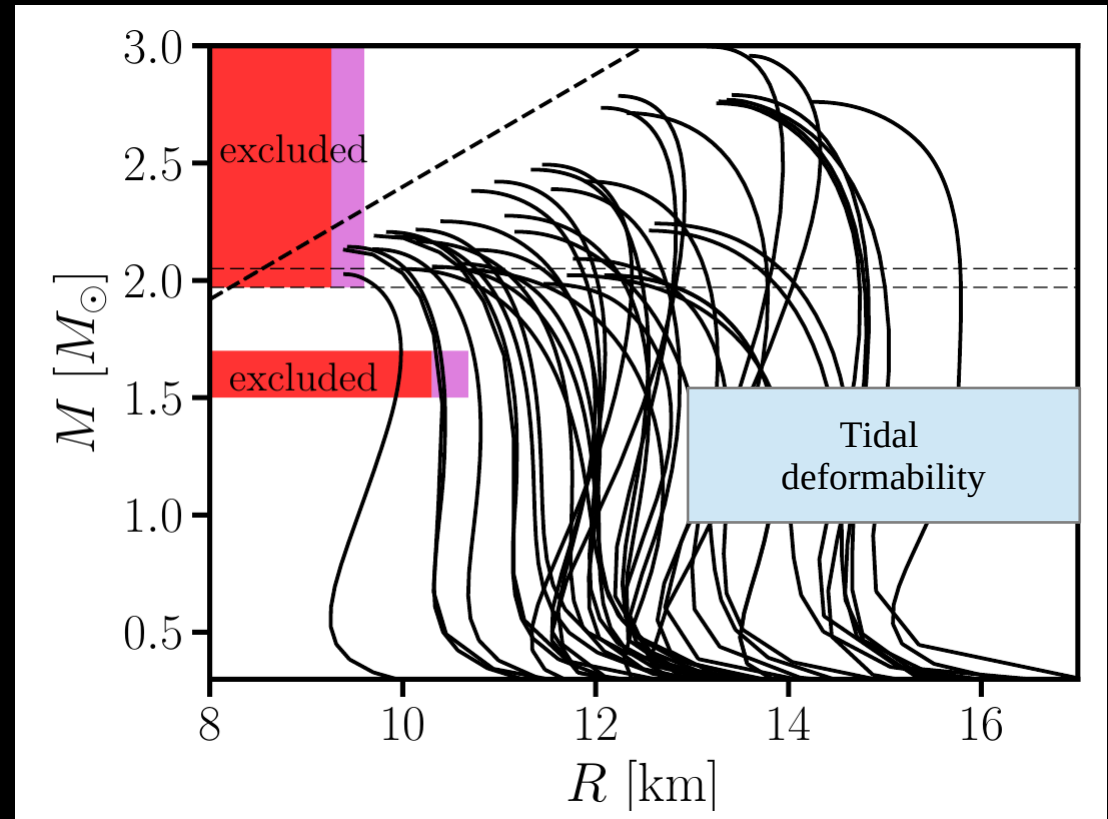


$$M_{\text{thres}} = \left( -3.6 \frac{G M_{\text{max}}}{c^2 R_{1.6}} + 2.38 \right) M_{\text{max}}$$

$$v_S = \sqrt{\frac{dP}{de}} \leq c \rightarrow M_{\text{max}} \leq \kappa R_{1.6} \Rightarrow M_{\text{thres}} \geq 1.2 M_{\text{max}}$$

# NS radius constraint from GW170817

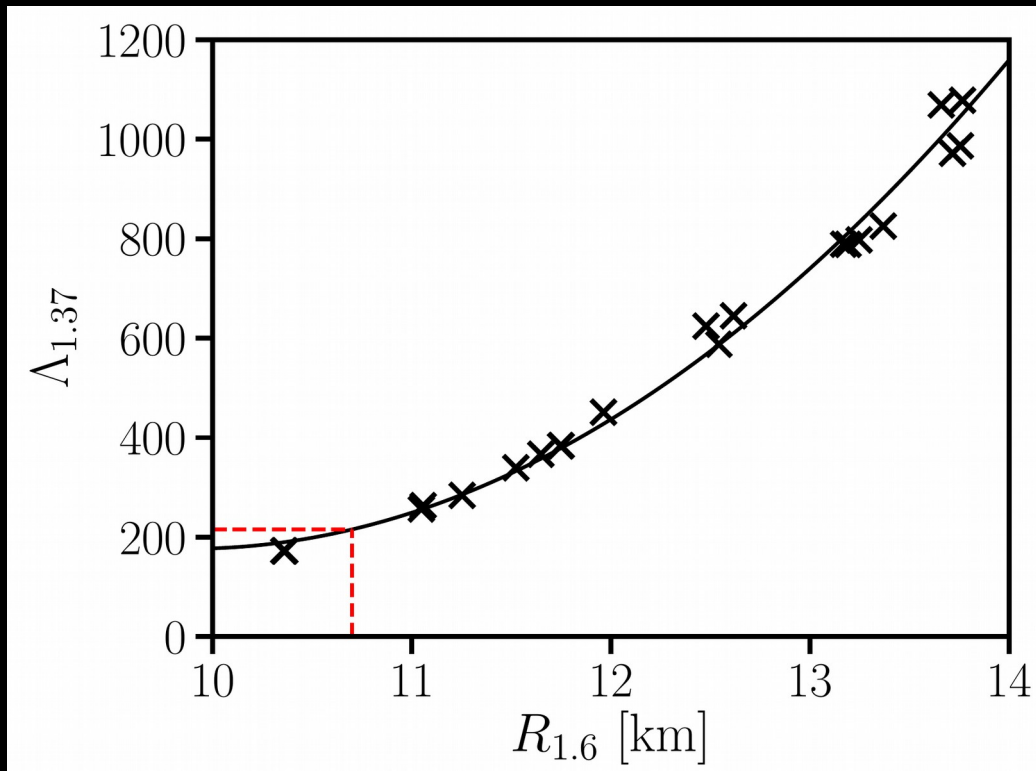
- ▶  $R_{\text{max}} > 9.6 \text{ km}$
- ▶  $R_{1.6} > 10.7 \text{ km}$
- ▶ Excludes very soft nuclear matter



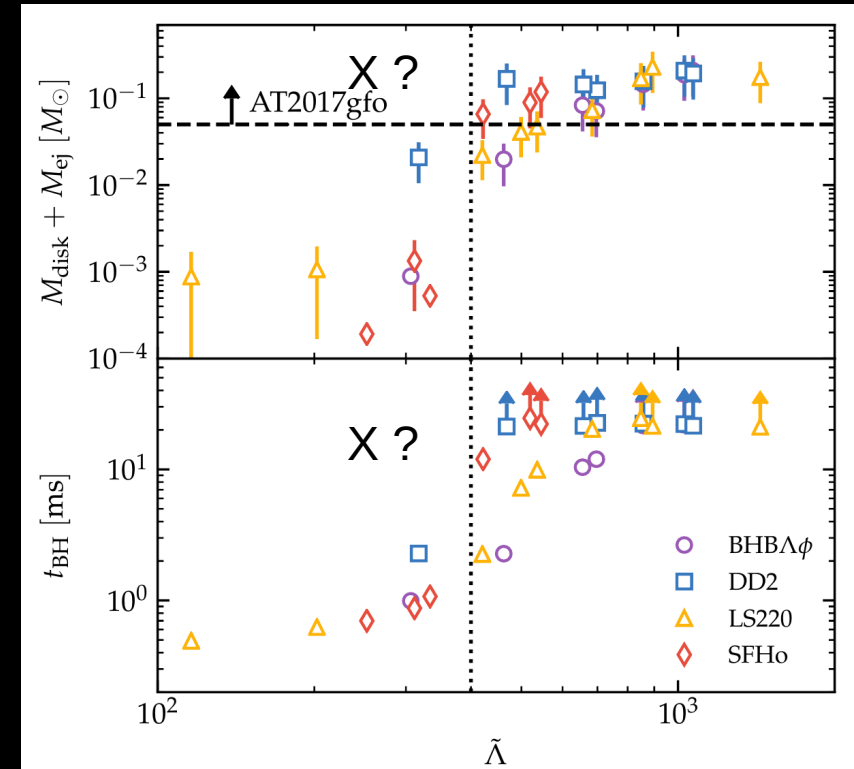
Bauswein et al. 2017

# Radius vs. tidal deformability

Radice et al 2018



Bauswein, unpubl.



- ▶ Radius and tidal deformability scale tightly → **Lambda > 210**
- ▶ Limit cannot be much larger otherwise we could get direct collapse / dim counterpart (unless one weakens some of the conservative assumptions)
- ▶ Radice et al. 2018 followed a very similar argument claiming **Lambda > 400** (300 in Dai 2019)
  - only 4 EoS considered – no complete coverage existing simulation data/parameter space
  - no argument why the fifth EoS shouldn't lie at  $\Lambda < 400$  (see also Tews et al. 2018)
  - full EoS dependence has to be investigated via  $M_{\text{thres}}$

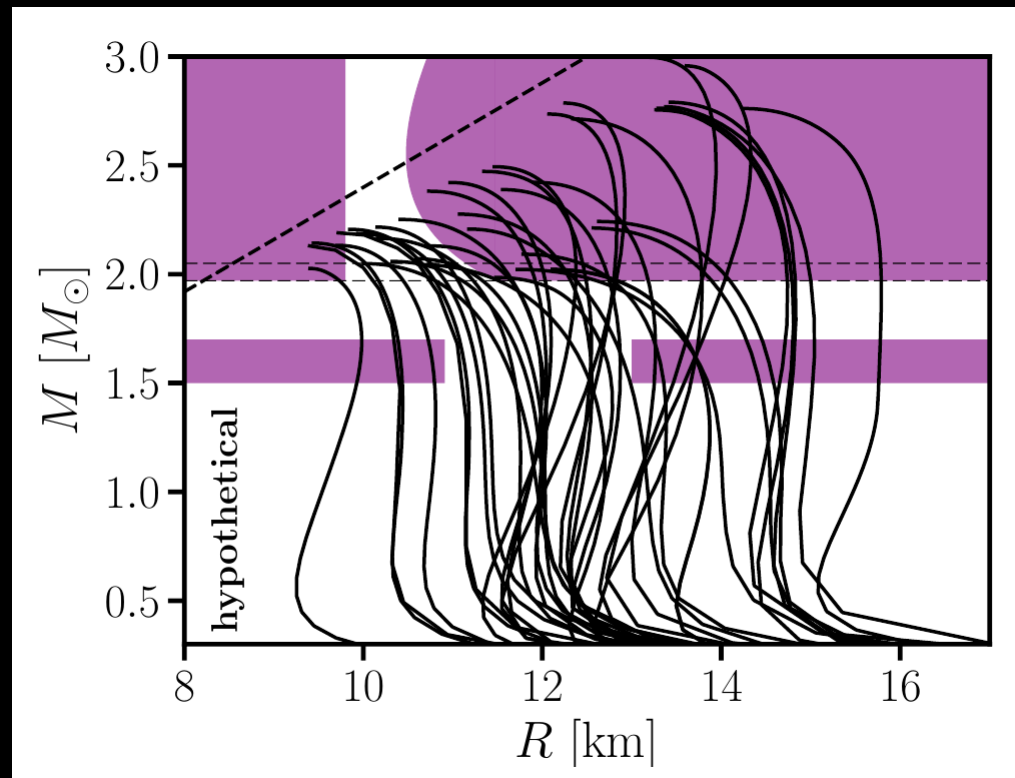
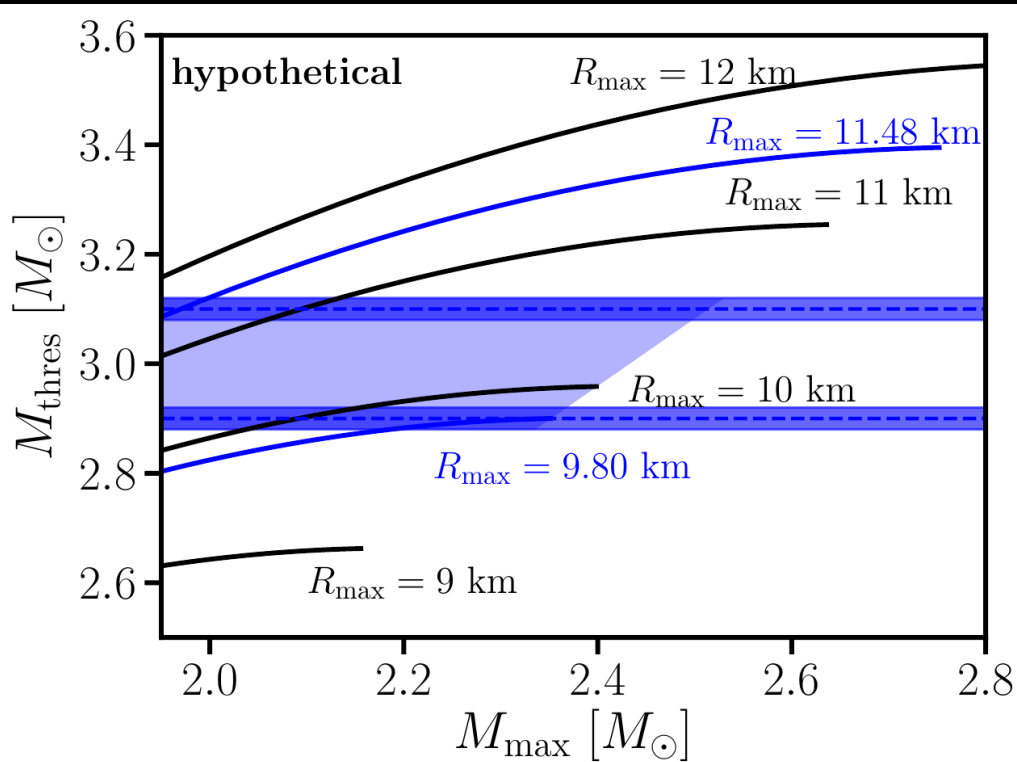
# Discussion - robustness

- ▶ Binary masses well measured with high confidence error bar
- ▶ Clearly defined working hypothesis: delayed collapse
  - testable by refined emission models
  - as more events are observed more robust distinction
- ▶ Very conservative estimate, errors can be quantified
- ▶ Empirical relation can be tested by more elaborated simulations (but unlikely that MHD or neutrinos can have strong impact on  $M_{\text{thres}}$ )
- ▶ Confirmed by semi-analytic collapse model
- ▶ Low-SNR constraint !!!

# Future

- ▶ Any new detection can be employed if it allows distinction between prompt/delayed collapse
- ▶ With more events in the future our comprehension of em counterparts will grow → more robust discrimination of prompt/delayed collapse events
- ▶ Low-SNR detections sufficient !!! → that's the potential for the future
  - we don't need louder events, but more
  - complimentary to existing ideas for EoS constraints

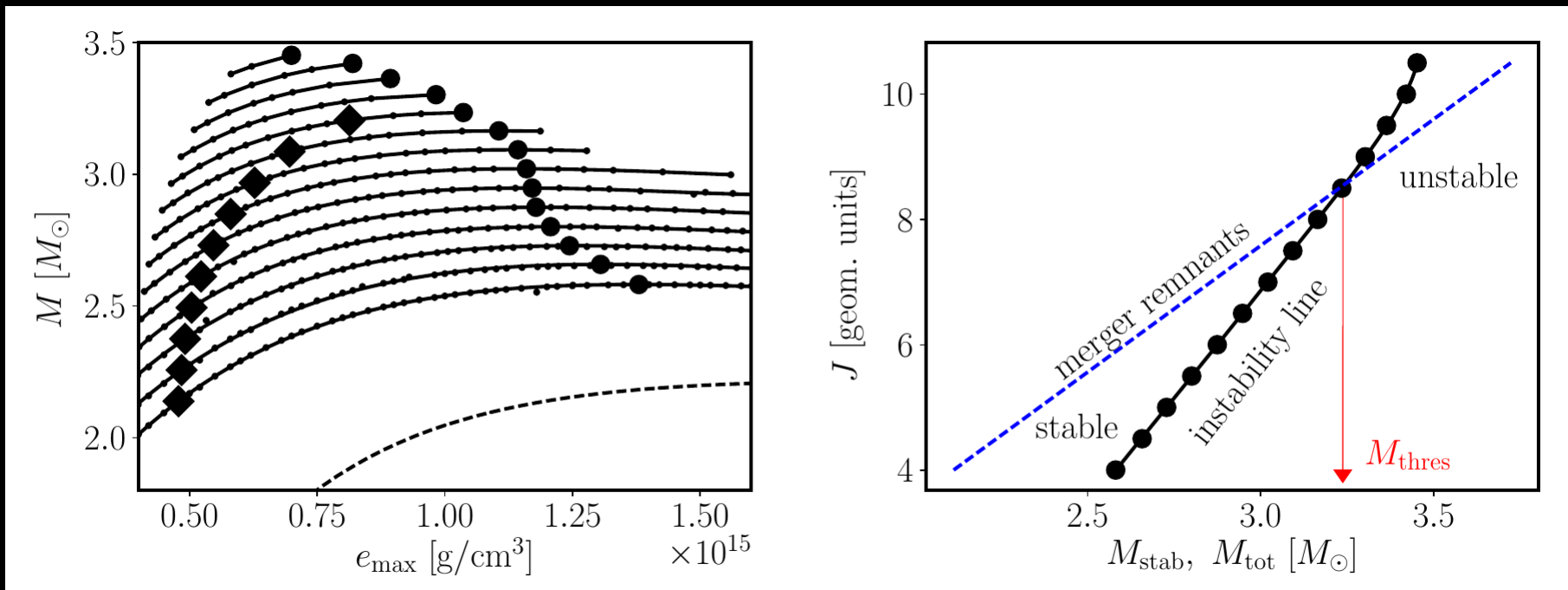
# Future detections (hypothetical discussion)



- as more events are observed, bands converge to true  $M_{\text{thres}}$
- prompt collapse constrains  $M_{\text{max}}$  from above

# Semi-analytic model: details

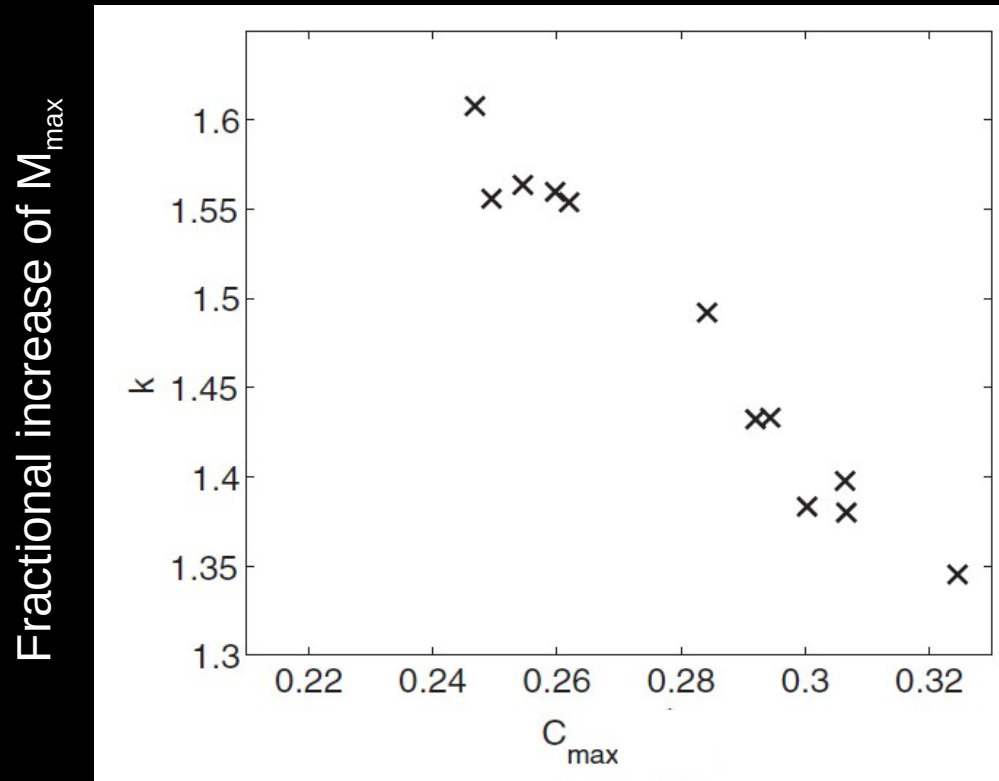
- ▶ Stellar equilibrium models computed with RNS code (diff. Rotation,  $T=0$ , many different microphysical EoS)  $\Rightarrow$  turning points  $\Rightarrow M_{\text{stab}}(J)$
- ▶ Compared to  $J(M_{\text{tot}})$  of merger remnants from simulations (very robust result)  $\rightarrow$  practically independent from simulations



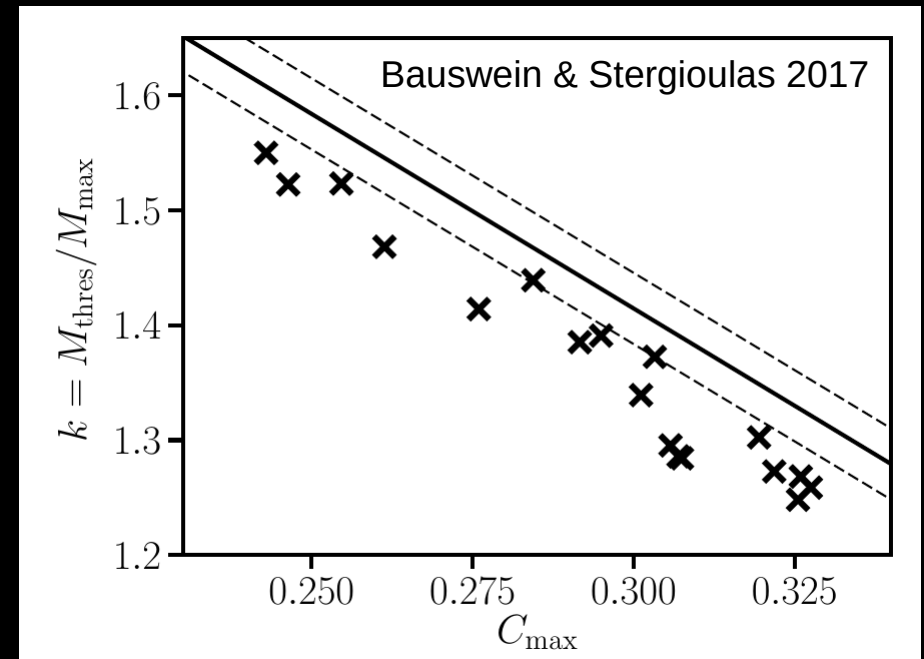
Bauswein & Stergioulas 2017



# Semi-analytic model reproducing collapse behavior



Bauswein et al 2013: numerical determination of collapse threshold through hydrodynamical simulations



Solid line fit to numerical data

Crosses stellar **equilibrium models**:

- prescribed (simplistic) diff. rotation
  - many EoSs at  $T=0$
  - detailed angular momentum budget !
- => equilibrium models qualitatively reproduce collapse behavior
- even quantitatively good considering the adopted approximations

# Future: Maximum mass

- ▶ Empirical relation

$$M_{\text{thres}} = \left( -3.6 \frac{G M_{\text{max}}}{c^2 R_{1.6}} + 2.38 \right) M_{\text{max}}$$

- ▶ Sooner or later we'll know  $R_{1.6}$  (e.g. from postmerger) and  $M_{\text{thres}}$  (from several events – through presence/absence of postmerger GW emission or em counterpart)

=> direct inversion to get precise estimate of  $M_{\text{max}}$

(see also current estimates e.g. by Margalit & Metzger, Rezzolla et al, Ruiz & Shapiro, Shibata et al., ...)

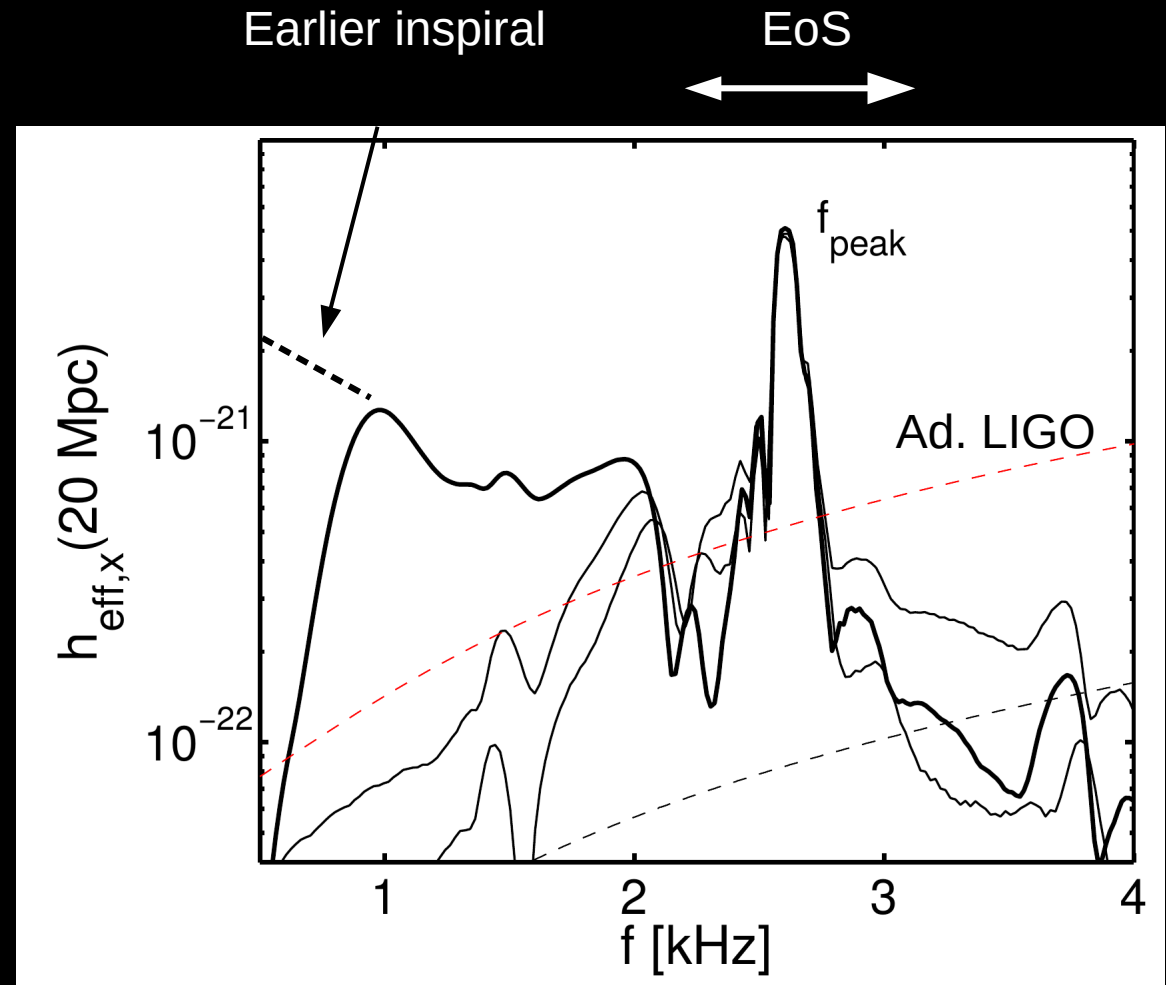
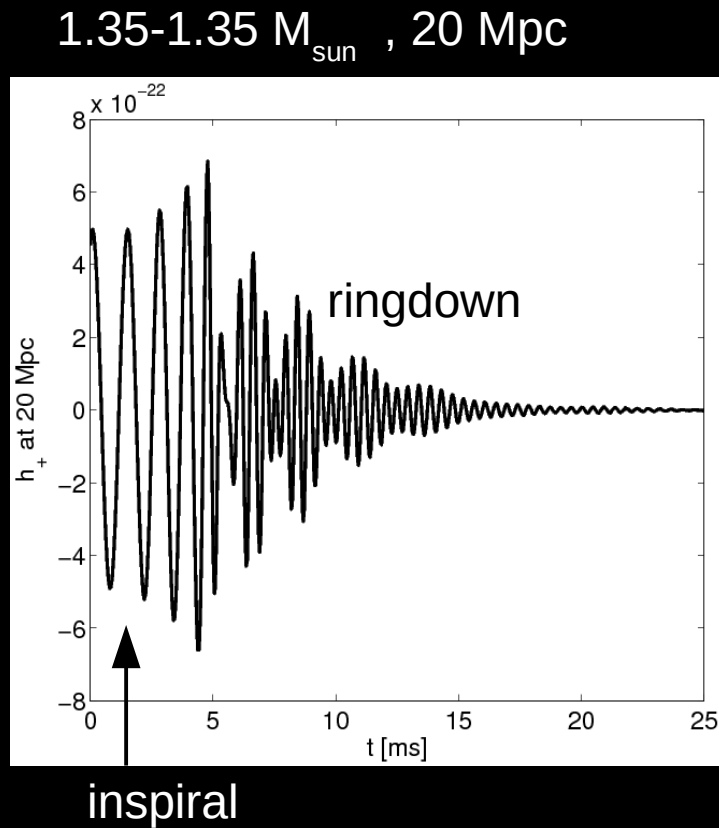
# Postmerger GW emission\*

(dominant frequency of postmerger phase)

- determine properties of EoS/NSs
- complementary to inspiral

\* not detected for GW170817 – expected for current sensitivity and  $d=40$  Mpc (Abbott et al. 2017)

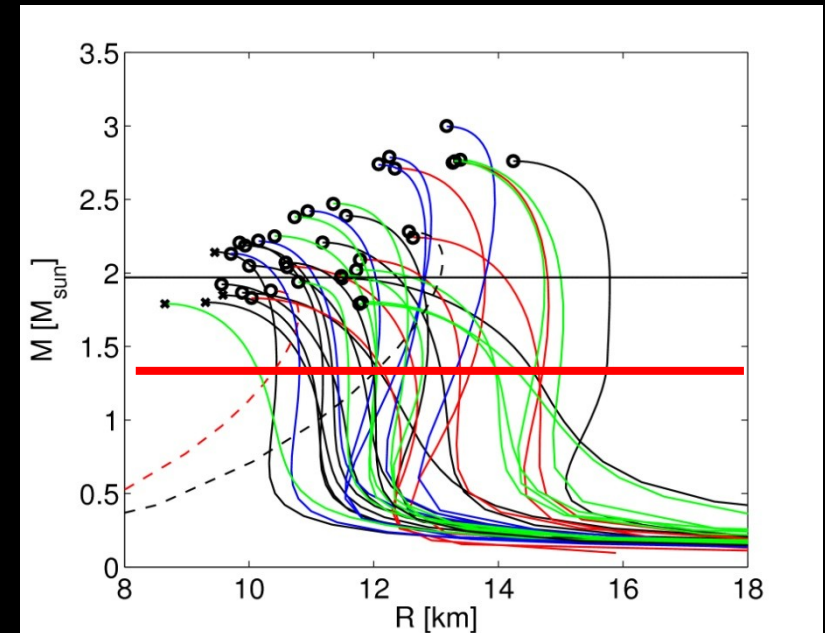
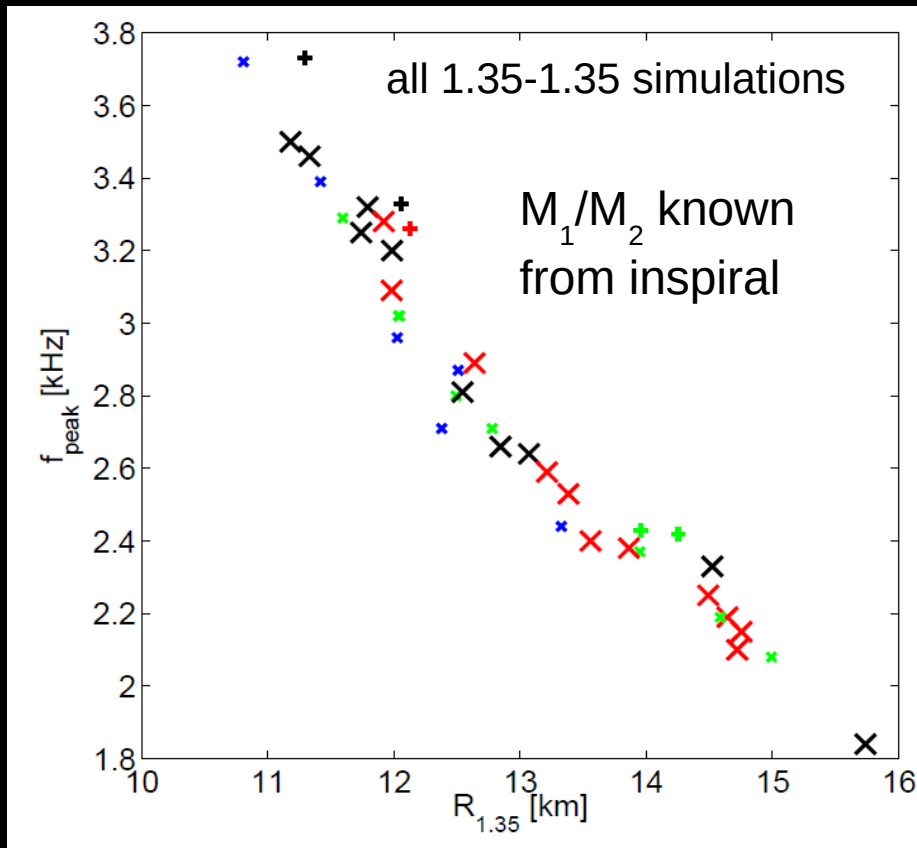
# Postmerger



Dominant postmerger oscillation frequency  $f_{\text{peak}}$

Very characteristic (robust feature in all models)

# Gravitational waves – EoS survey



characterize EoS by radius of nonrotating NS with  $1.35 M_{\text{sun}}$

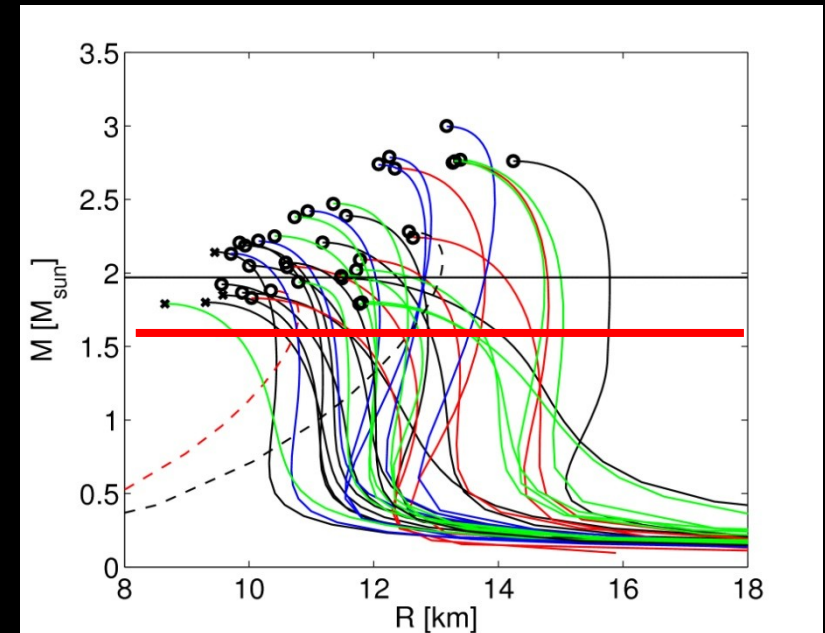
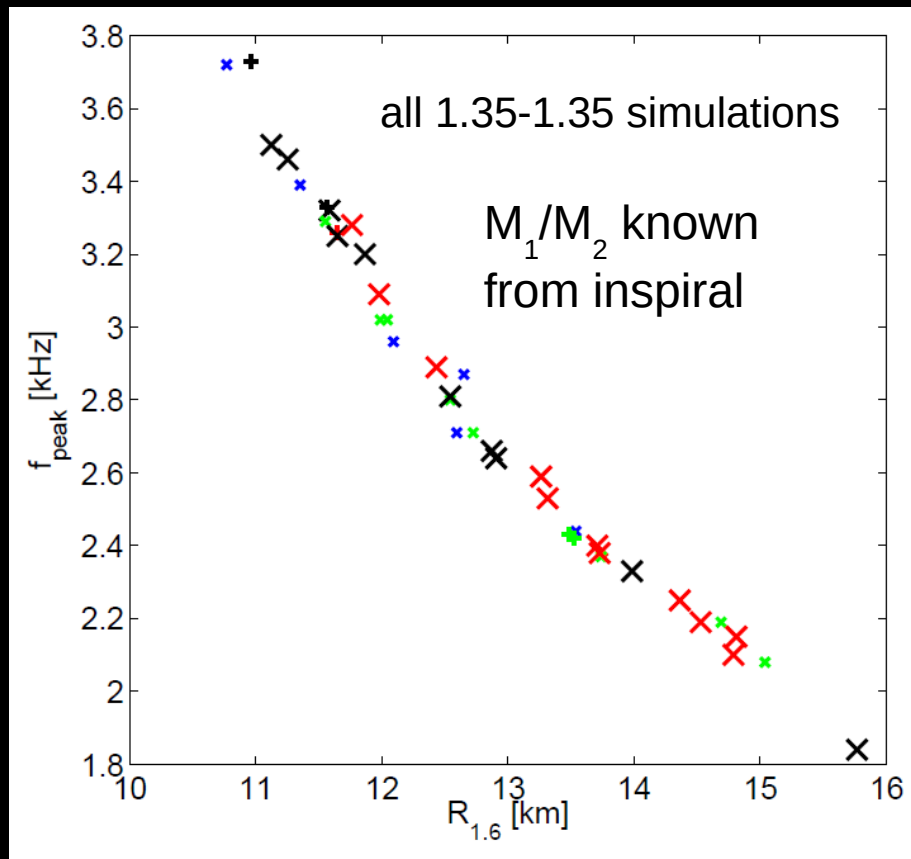
*Bauswein et al. 2012*

Pure TOV/EoS property  $\Rightarrow$  **Radius measurement** via  $f_{\text{peak}}$

Here only 1.35-1.35  $M_{\text{sun}}$  mergers (binary masses measurable) – similar relations exist for other fixed binary setups !!!

~ 40 different NS EoSs

# Gravitational waves – EoS survey



characterize EoS by radius of nonrotating NS with  $1.6 M_{\text{sun}}$

*Bauswein et al. 2012*

Pure TOV/EoS property => **Radius measurement** via  $f_{\text{peak}}$

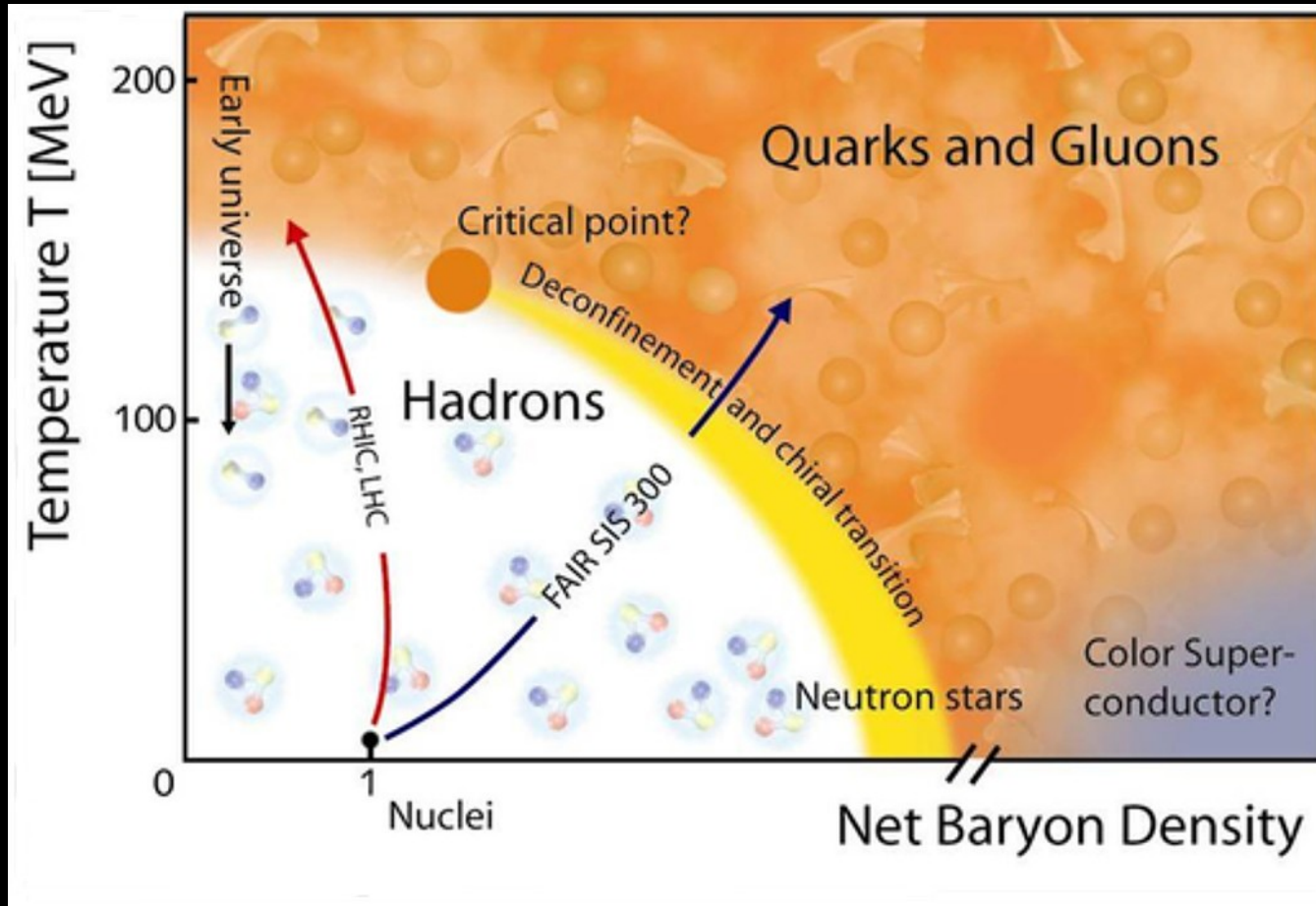
Smaller scatter in empirical relation ( $< 200$  m) → smaller error in radius measurement

Note:  $R$  of  $1.6 M_{\text{sun}}$  NS scales with  $f_{\text{peak}}$  from  $1.35$ - $1.35 M_{\text{sun}}$  mergers (density regimes comparable)

GW data analysis: Clark et al 2014, Clark et al 2016, Chatziioannou et al 2017, Bose et al. 2018, Breschi et al 2019, ... → detectable at a few 10 Mpc

Observable signature of (QCD) phase transition

# Phase diagram of matter

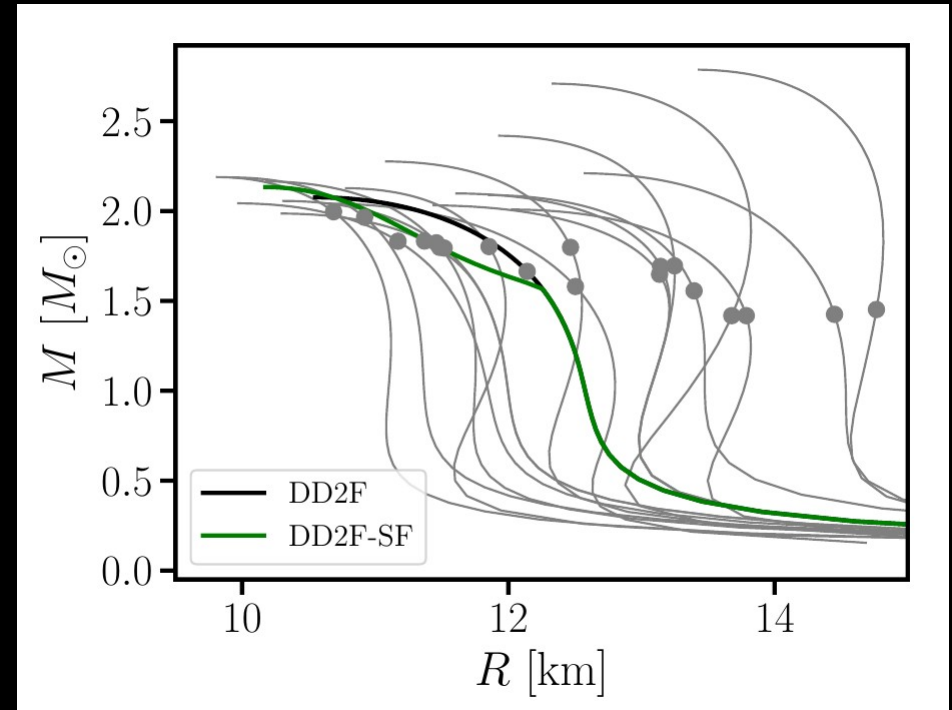
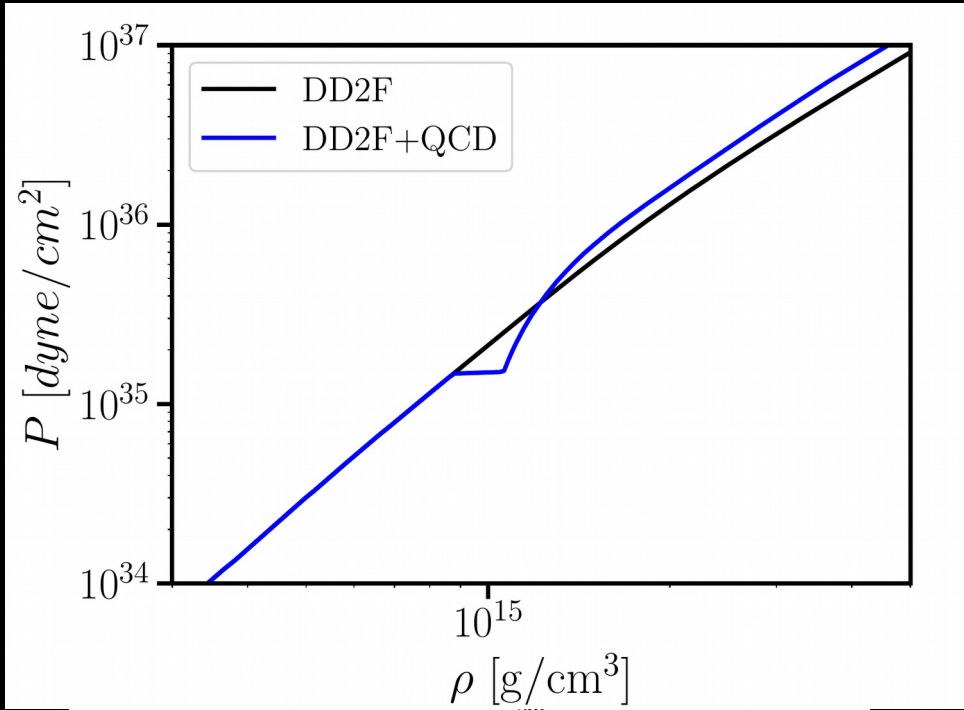


Does the phase transition to quark-gluon plasma occur (already) in neutron stars or only at higher densities ?



# EoS with 1<sup>st</sup>-order phase transition to quark matter

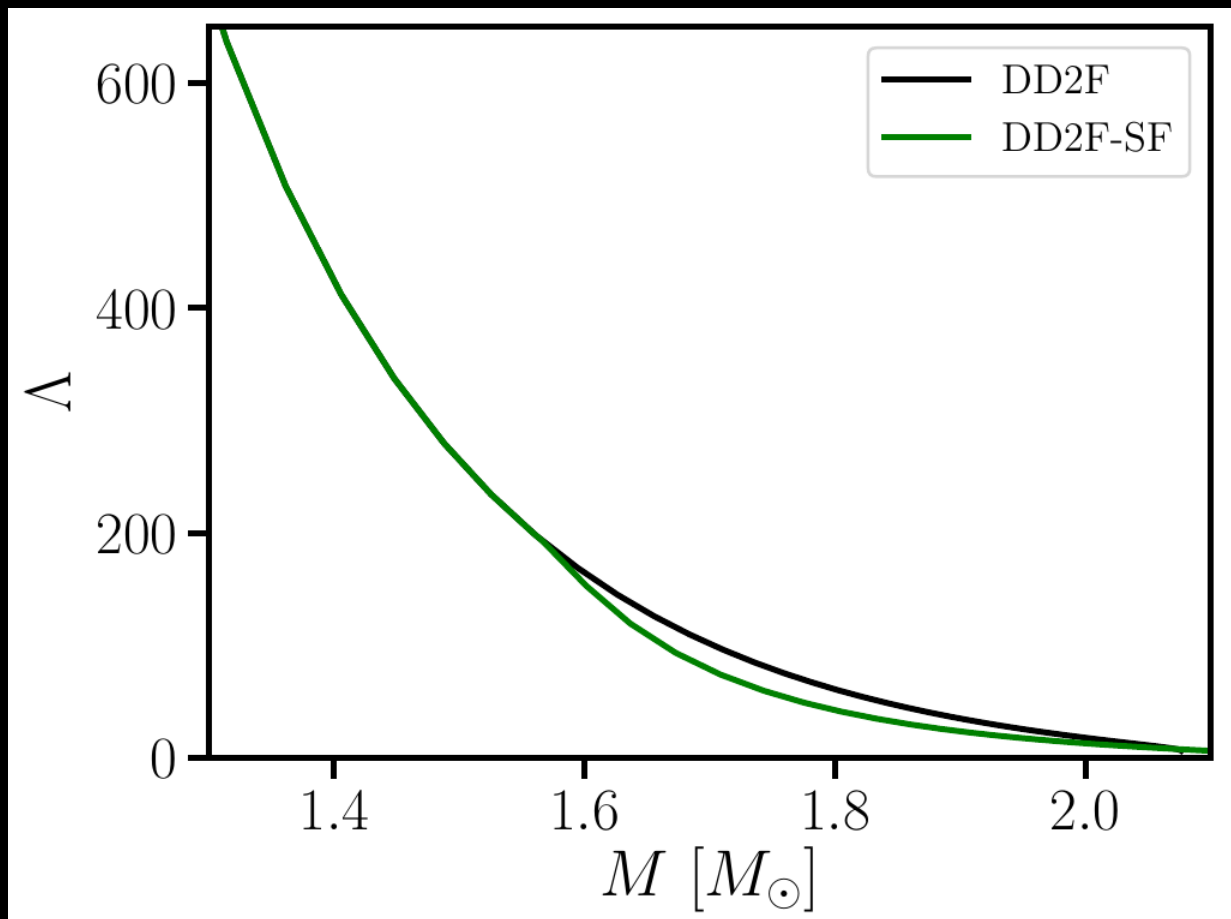
Bauswein et al. 2018



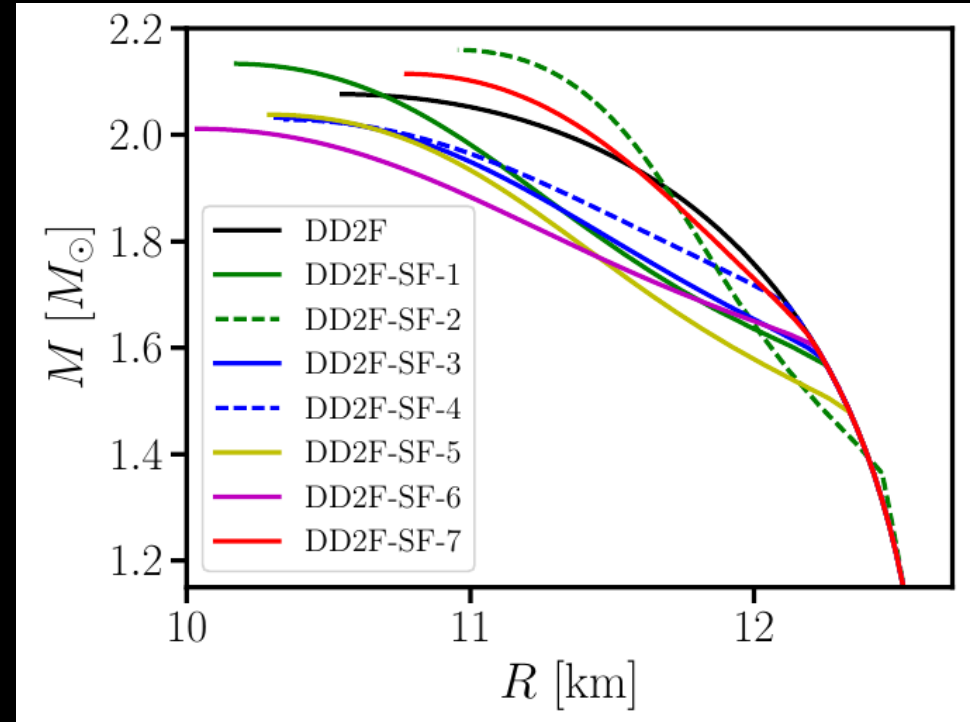
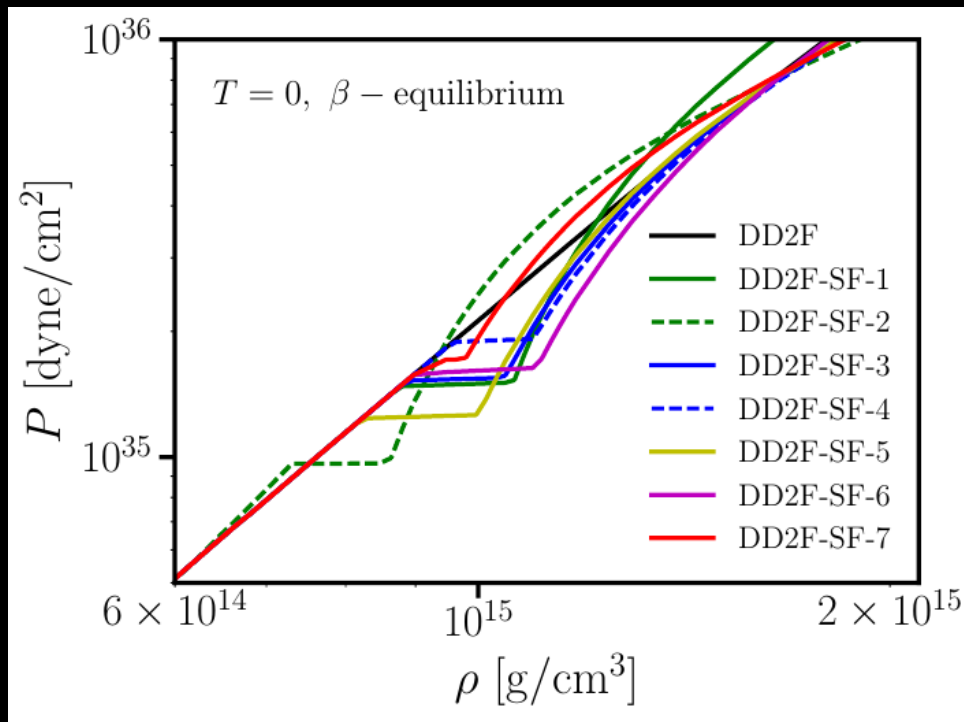
- ▶ EoS from Wroclaw group (Fischer, Bastian, Blaschke; Fischer et al. 2018) – as one example for an EoS with a strong 1<sup>st</sup>-order phase transition to deconfined quarks
- ▶ Difficult to measure transition in mergers through inspiral: Lambda very small, high mass star probably less frequent

# Phase transition

- Even strong phase transitions leave relatively weak impact on tidal deformability

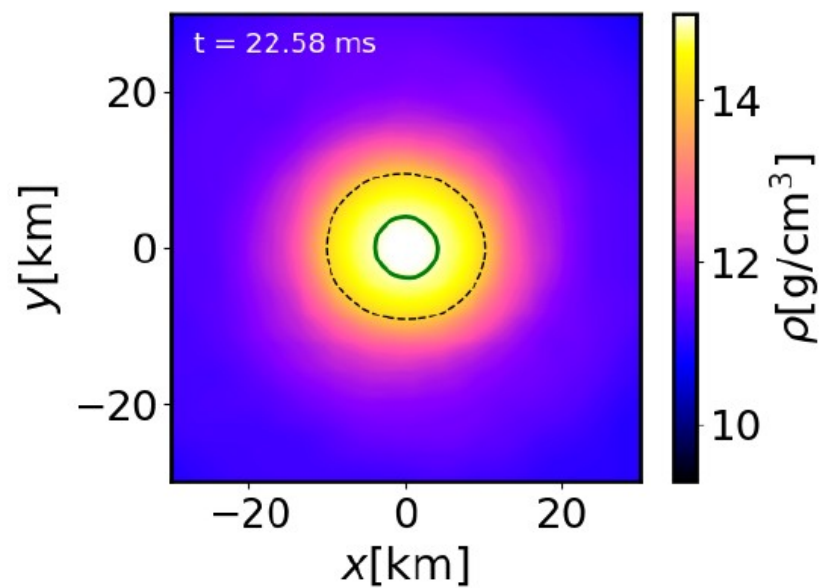
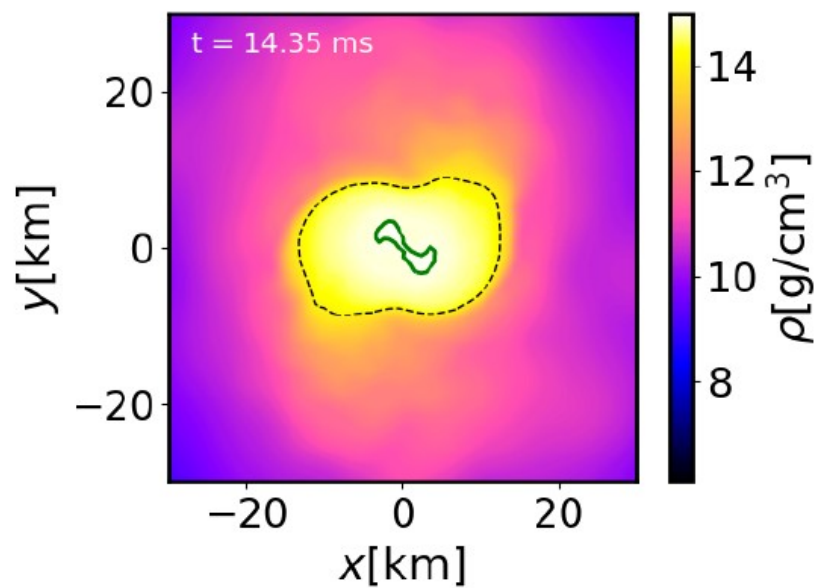
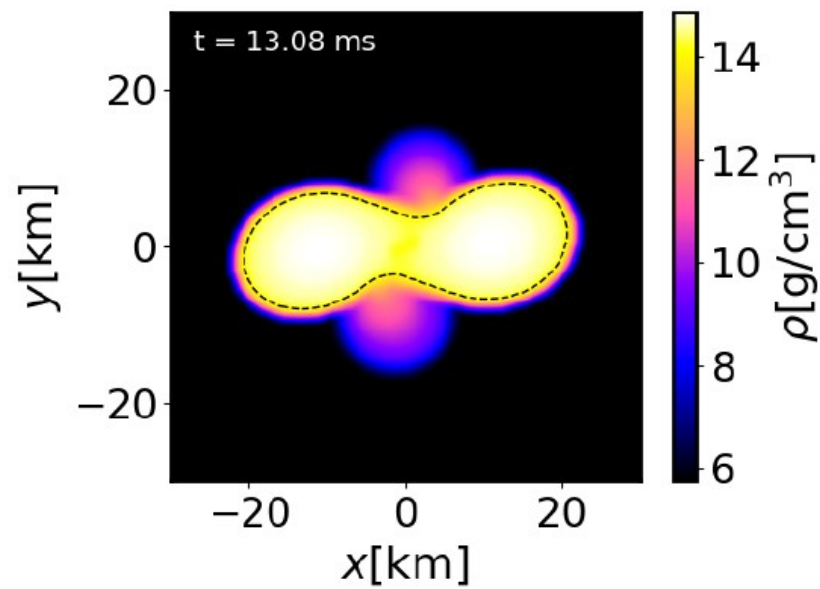
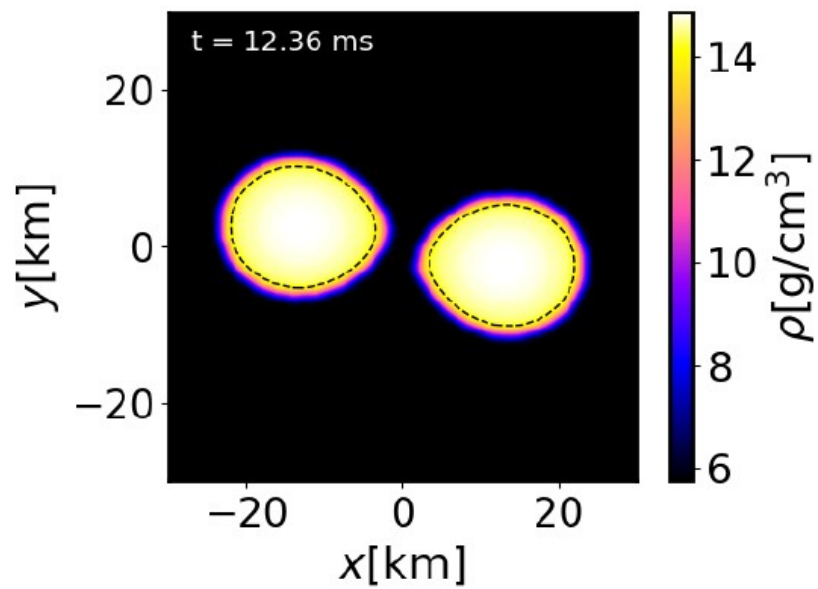


- ▶ 7 different models for quark matter: different onset density, different density jump, different stiffness of quark matter phase



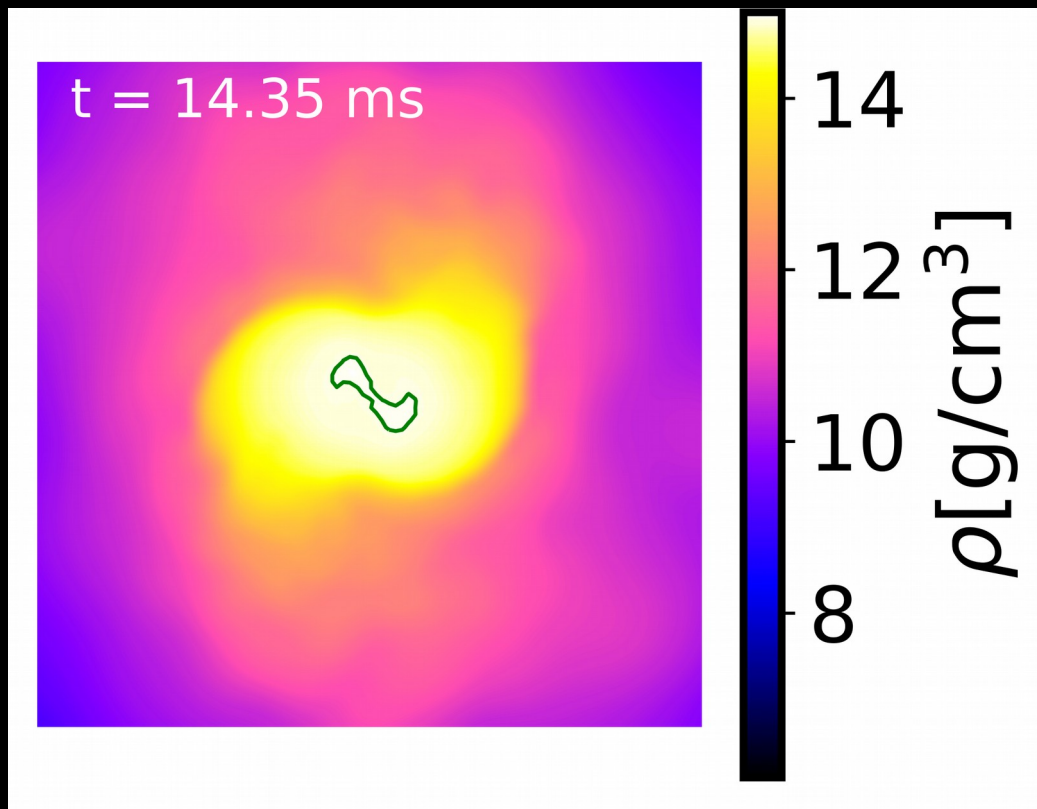
EoSs from Wroclaw group

Bauswein et al. 2019

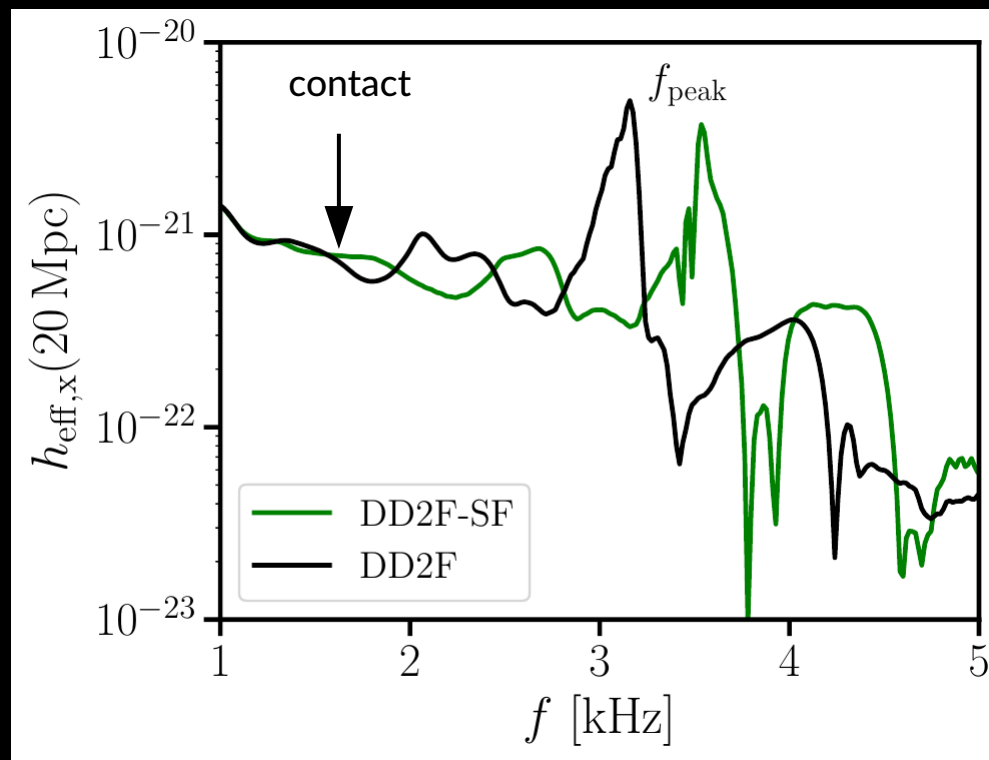


1.35-1.35 Msun - DD2F-SF-1

# Merger simulations



► GW spectrum 1.35-1.35 Msun



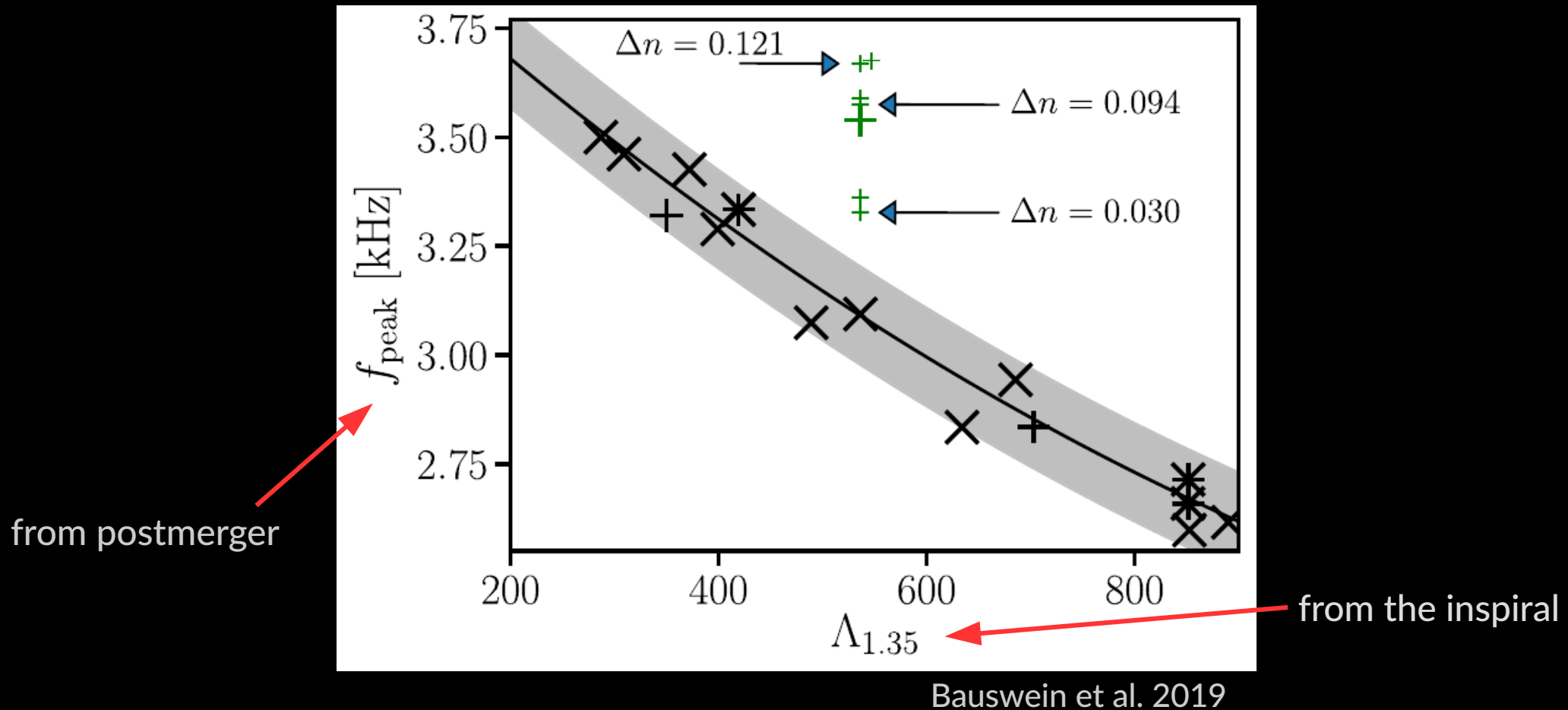
Bauswein et al. 2019

But: a high frequency on its own may not yet be characteristic for a phase transition

→ unambiguous signature

(→ show that all purely baryonic EoS behave differently)

# Signature of 1<sup>st</sup> order phase transition



- Tidal deformability measurable from inspiral to within 100-200 (Adv. Ligo design)
- Postmerger frequency measurable to within a few 10 Hz @ a few 10 Mpc (either Adv. Ligo or upgrade: e.g Clark et al. 2016, Chatzioannou et al 2017, Bose et al 2018, Torres-Rivas et al 2019)
- Important: “all” purely hadronic EoSs (including hyperonic EoS) follow  $f_{\text{peak}}$ - $\Lambda$  relation → deviation characteristic for strong 1<sup>st</sup> order phase transition

# Conclusions

- ▶ NS radius must be larger than 10.7 km (very robust and conservative)
- ▶ More stringent constraints from future detections
- ▶ NS radius measurable from dominant postmerger frequency
- ▶ Explicitly shown by GW data analysis
- ▶ Threshold binary mass for prompt collapse → maximum mass  $M_{\text{max}}$
- ▶ Strong 1<sup>st</sup> order phase transitions leave characteristic imprint on GW (postmerger frequency higher than expected from inspiral)
- ▶ Complementarity of inspiral and postmerger phase → postmerger probes higher density regime

