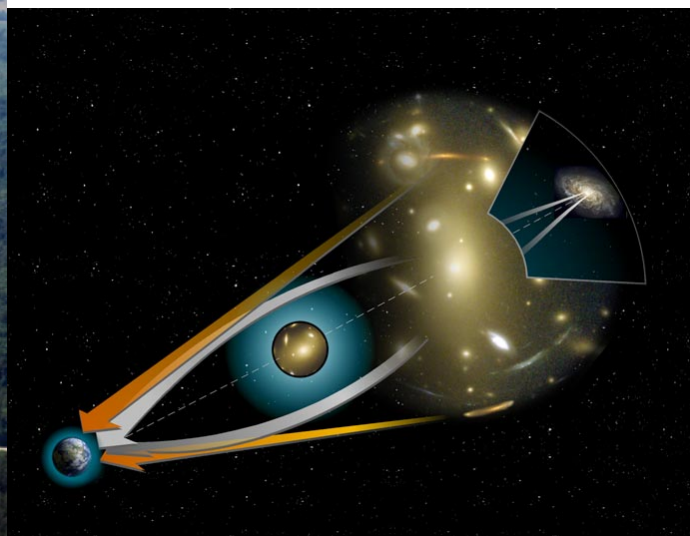


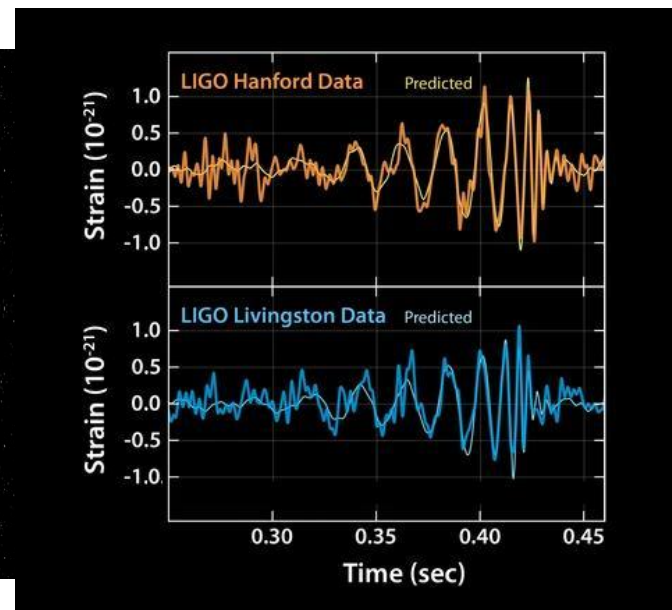
Could gravitational lensing impact the observed BBH population?



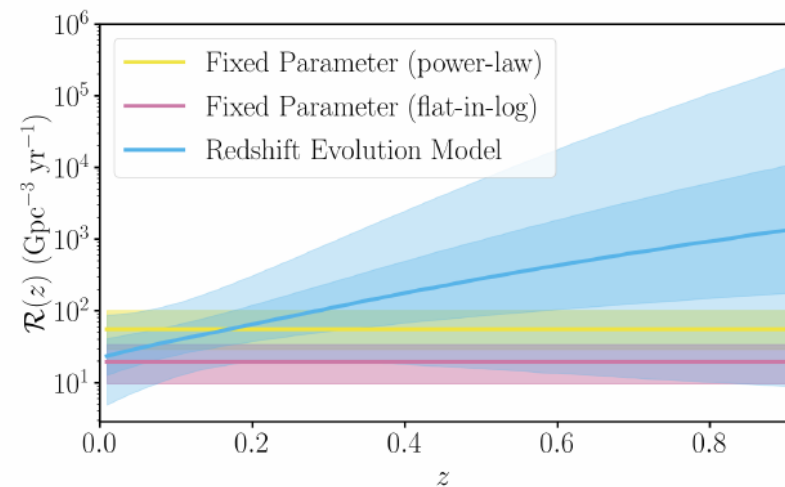
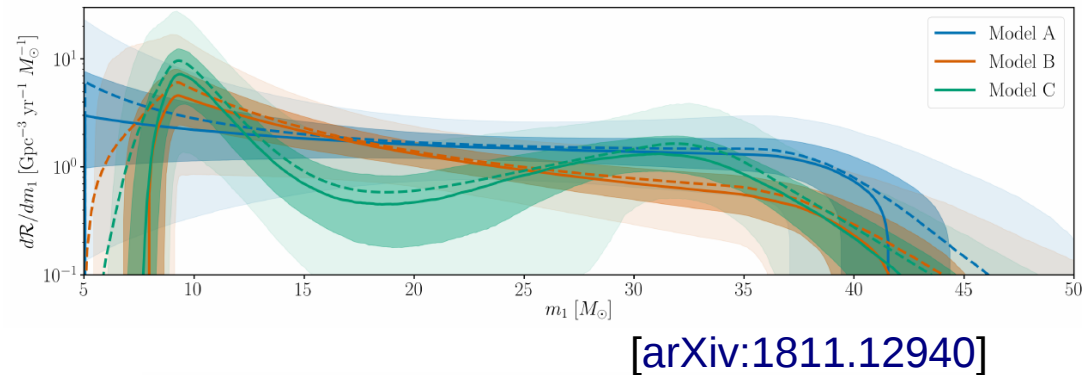
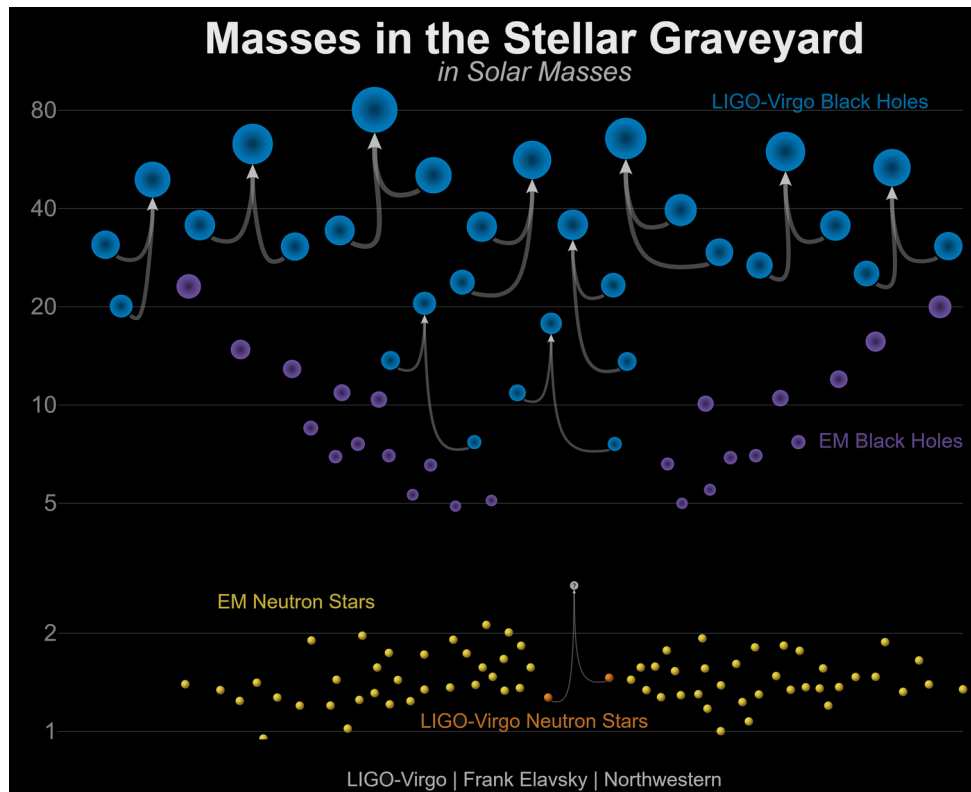
David Keitel
Institute of Cosmology & Gravitation
University of Portsmouth



[NASA/STScI]



The merging BBH population so far

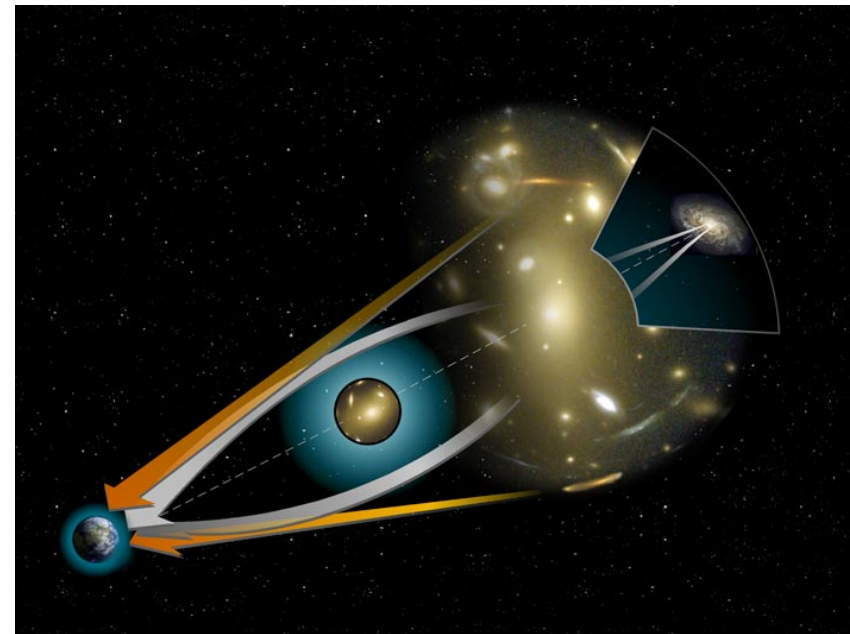
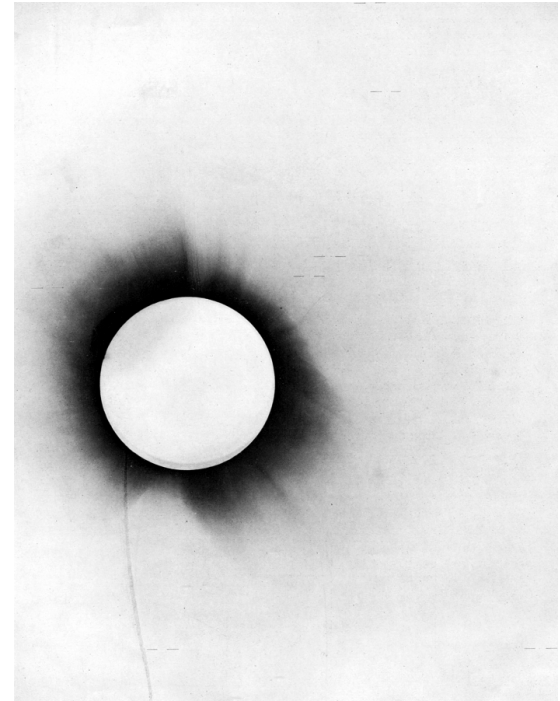


- LIGO-Virgo GWTC-1: ten BBHs from O1+O2 [arXiv:1811.12907]
- Venumadhav et al: 7 more (?) [arXiv:1904.07214]
- masses $\sim 7 - 50 M_\text{sun}$ • distances $\sim 300 \text{ Mpc} - 3 \text{ Gpc}$ ($z \sim 0.05 - 0.6$)
- O3 so far: > 2 dozen alerts for candidate binaries (of mysterious properties)
[https://gracedb.ligo.org/search/?query=public&query_type=S]

Gravitational Lensing

(of light)

- first experimental test of Einstein's GR (1919): gravitational light deflection by the sun
- Lensing of light sources at cosmological distances has become a crucial tool in observational astrophysics.
- strong lensing regime:
 - ◆ high magnifications
 - ◆ multiple images
 - ◆ significant time delays
- use as 'natural telescopes' for high-redshift sources
- Almost always: geometric optics, no frequency-dependent distortions.



Gravitational Lensing of GWs

- J.A. Wheeler: “Spacetime tells matter how to move, and matter tells spacetime how to curve.”

→ corollary: “Matter tells gravity how to move.”

- GWs = propagating gravitational field excitations. Can be deflected by heavy masses, just like light.

- early work: e.g. Vishveshwara 1970, Lawrence 1971/73, Peters 1974, Ohanian 1973/74



[SXS]

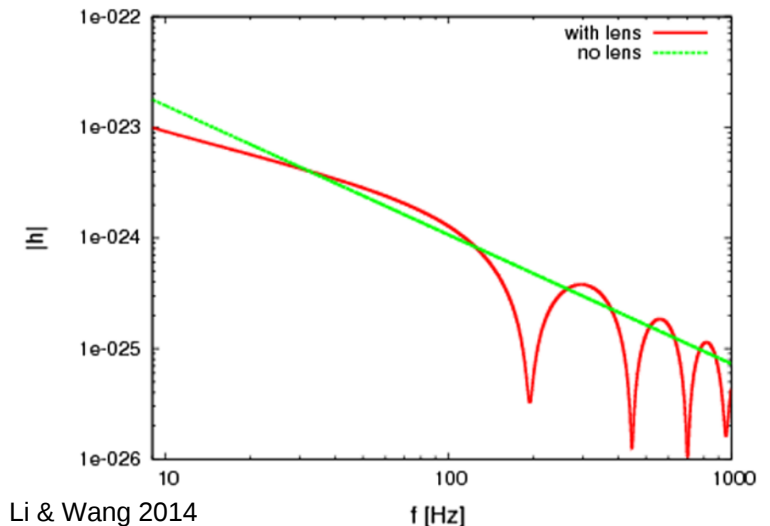
- much focus on future detectors (Einstein Telescope, LISA)

e.g. Takahashi&Nakamura 2003,
Serenio+ 2010, Biesiada+2014

- Wave optics effects can be important!

[e.g. Nakamura 1998]

(IMBHs as lenses, substructure in galaxy lenses)

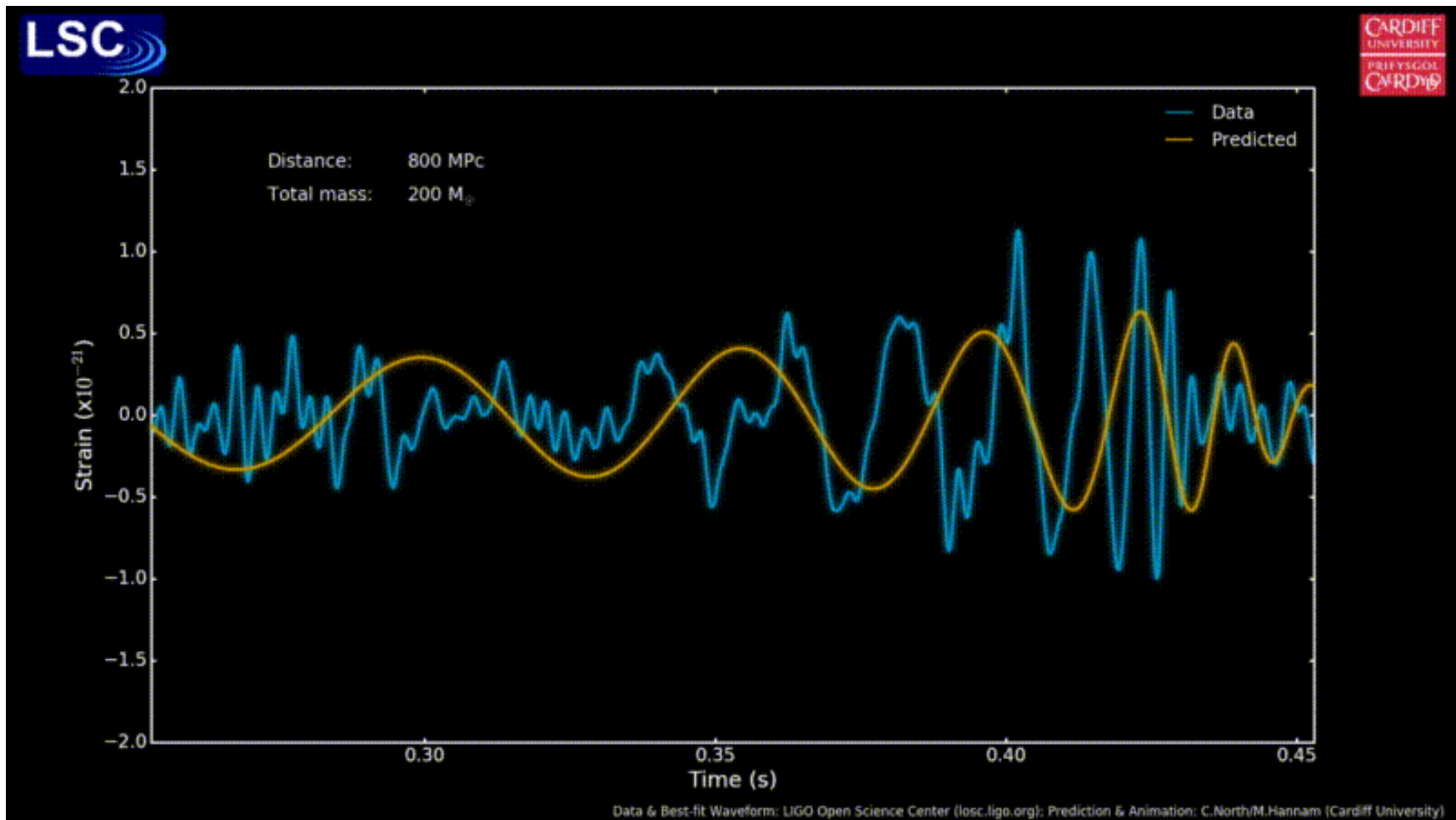


[Cao, Li & Wang 2014
PRD90,062003]

strong lensing of BBHs

(in the geometric limit)

- BBH parameter estimation in a nutshell:
 - ◆ phasing \rightarrow chirp mass
 - ◆ amplitude at known mass \rightarrow luminosity distance



strong lensing of BBHs

(in the geometric limit)

- BBH parameter estimation in a nutshell:
 - ◆ phasing \rightarrow chirp mass
 - ◆ amplitude at known mass \rightarrow luminosity distance
- if lensed: GW amplitude $\sim \sqrt{\text{magnification}}$
 - \rightarrow real distance higher by $\sqrt{\text{mag}}$
 - \rightarrow stronger cosmological redshift
- But we have still measured the same redshifted chirp mass!
 - \rightarrow Intrinsic BH masses would have been lower.

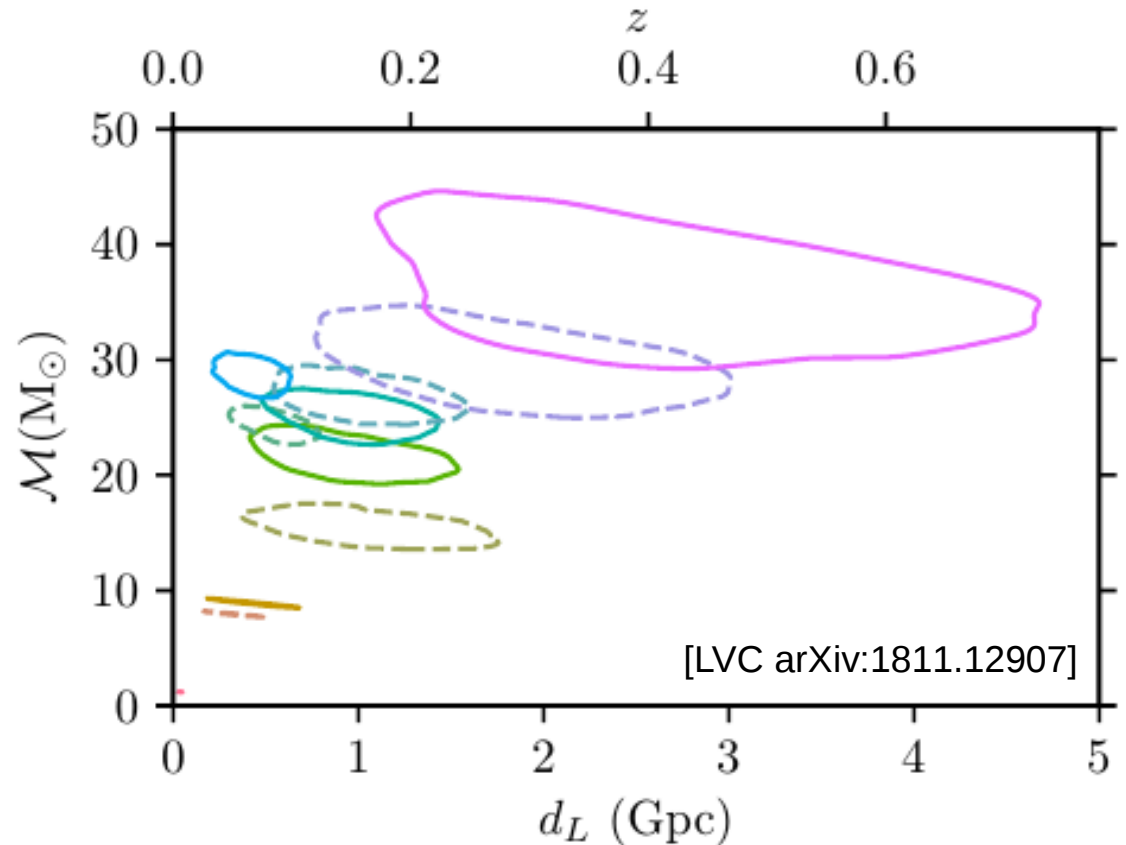
strong lensing of aLIGO detections?

- rich crop of LIGO-Virgo BBHs reaching up to cosmological distances

→ growing interest in lensing scenario

e.g.:

- ♦ [Smith+ 2018](#): “What if LIGO’s gravitational wave detections are strongly lensed by massive galaxy clusters?”
- ♦ [Oguri 2018](#): “Effect of gravitational lensing on the distribution of gravitational waves from distant binary black hole mergers”



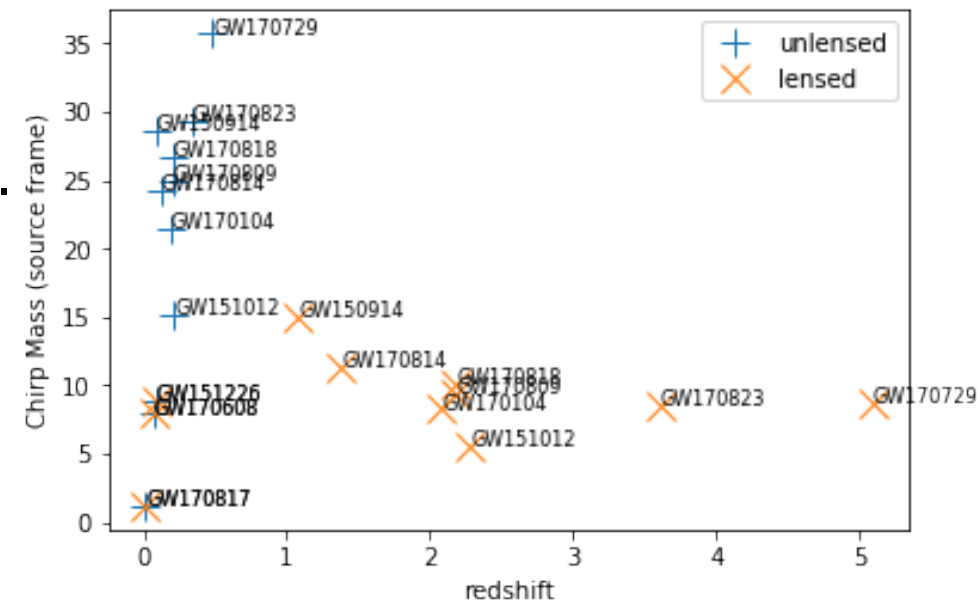
strong lensing of aLIGO detections?

- Broadhurst, Diego & Smoot [[arXiv:1802.05273](#)]:
“Reinterpreting Low Frequency LIGO/Virgo Events as Magnified Stellar-Mass Black Holes at Cosmological Distances”

→ black holes $> 20 M_{\odot}$ considered “puzzling”

→ A lensed, more distant and lighter BBH population could produce the same detections.

→ We’d have only found 1 image of each event, missing the possible counterparts.



- Broadhurst, Diego & Smoot [[arXiv:1901.03190](#)]:
“Twin LIGO/Virgo Detections of a Viable Gravitationally-Lensed Black Hole Merger”

→ claim that GW170809 and GW170814 are so similar that they could be lensed images of a single event (with intrinsic $M_{\text{chirp}} \sim 15 M_{\odot}$ instead of measured $\sim 30 M_{\odot}$)

strong lensing of aLIGO detections?

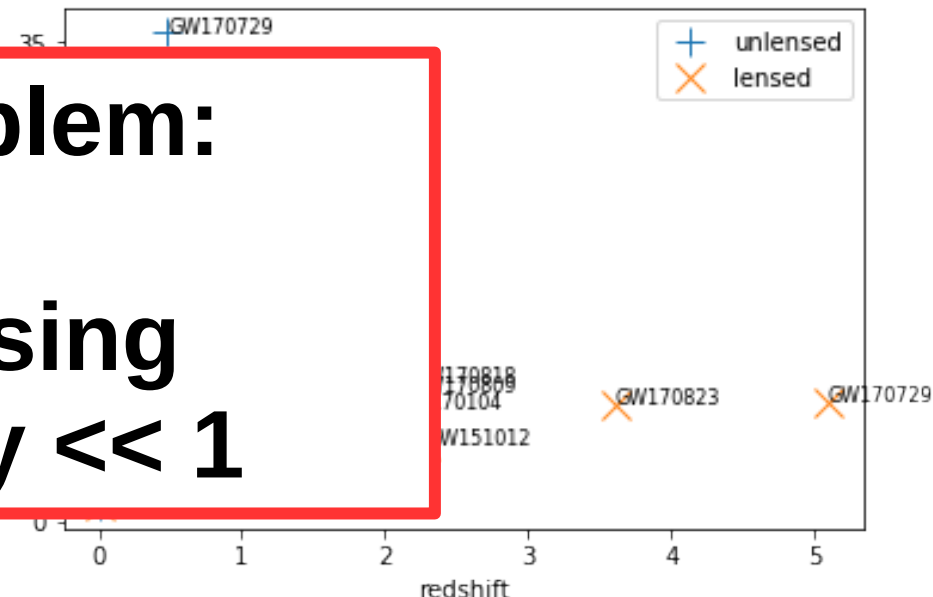
- Broadhurst, Diego & Smoot [[arXiv:1802.05273](#)]:
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→ black holes $> 20 M_{\odot}$ considered “puzzling”

→ A lensed, more distant
and lighter
could produce

→ We’d have
of each event
missing the

main problem:
prior lensing
probability $\ll 1$



- Broadhurst, Diego & Smoot [[arXiv:1901.03190](#)]:
“Twin LIGO/Virgo Detections of a Viable Gravitationally-Lensed Black Hole Merger”

→ claim that GW170809 and GW170814 are so similar
that they could be lensed images of a single event
(with intrinsic $M_{\text{chirp}} \sim 15 M_{\odot}$ instead of measured $\sim 30 M_{\odot}$)

Lensing tests on O2

- testing the Broadhurst+ claims & more generally searching for signatures of lensing in O1+O2 BBH events

arXiv.org > gr-qc > arXiv:1901.02674

General Relativity and Quantum Cosmology

Search for gravitational lensing signatures in LIGO-Virgo binary black hole events

O.A. Hannuksela, K. Haris, K.K.Y. Ng, S. Kumar, A.K. Mehta, [D. Keitel](#), T.G.F. Li, P. Ajith

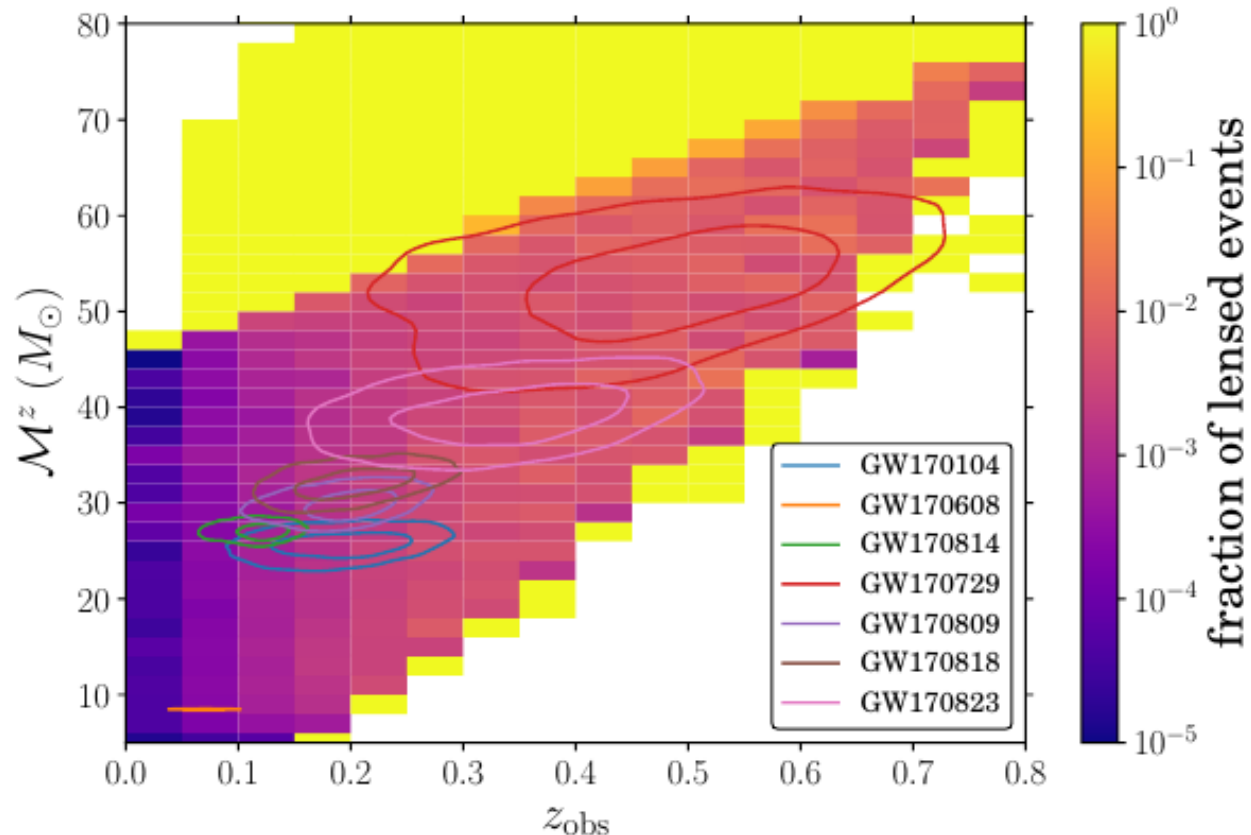
→ [ApJL 874:L2](#)

- three tests:
 - 1) test of the observed chirp mass – redshift distribution
 - 2) test for multiple images based on parameter overlaps
 - 3) test for frequency-dependent wave-optics effects

Lensing tests on O2

Test 1: observed chirp mass – redshift distribution

- expected lensing rate from massive galaxies depends on BBH masses and redshifts [Oguri 2018, Ng+ 2018]
- can be compared with observed distribution



[ApJL 874:L2]

- all observed events in region of low ($\leq 10^{-2}$) lensing probability

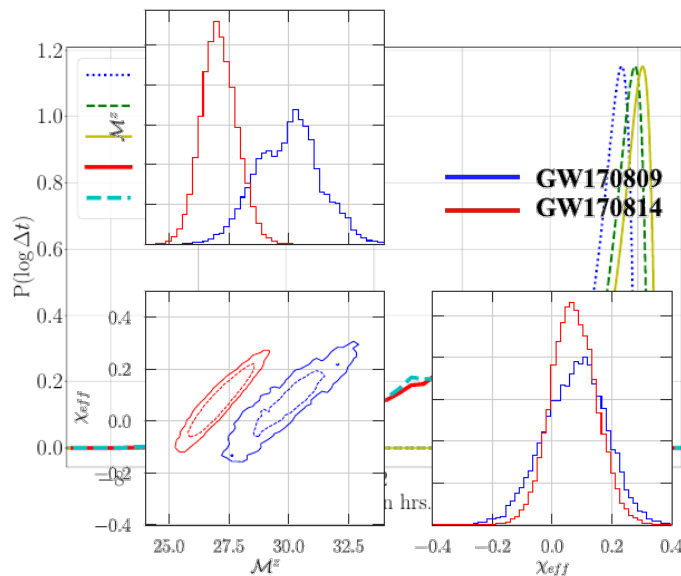
Lensing tests on O2

Test 2: multiple images?

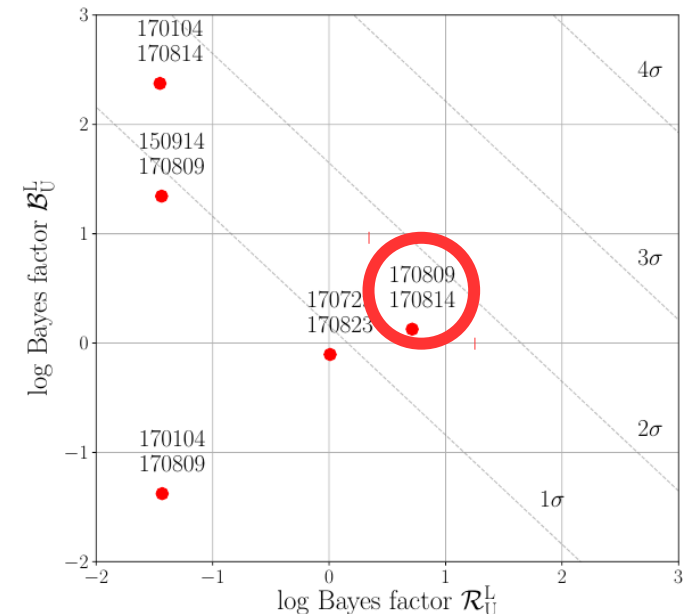
- geometric limit: lensing only magnifies, no waveform distortion
→ should measure same masses & spins for each image
- deflection angles much smaller than sky resolution
- test statistic: posterior overlap over mass, spin, sky parameters

→ Bayes factor $\mathcal{B}_U^L := \frac{\mathcal{Z}_L}{\mathcal{Z}_U} = \int d\theta \frac{P(\theta|d_1) P(\theta|d_2)}{P(\theta)}$ [Haris+, [arXiv:1807.07062](https://arxiv.org/abs/1807.07062)]

- extra info from time delays: more clustered for galaxy-mass lenses than unlensed (purely Poisson) events



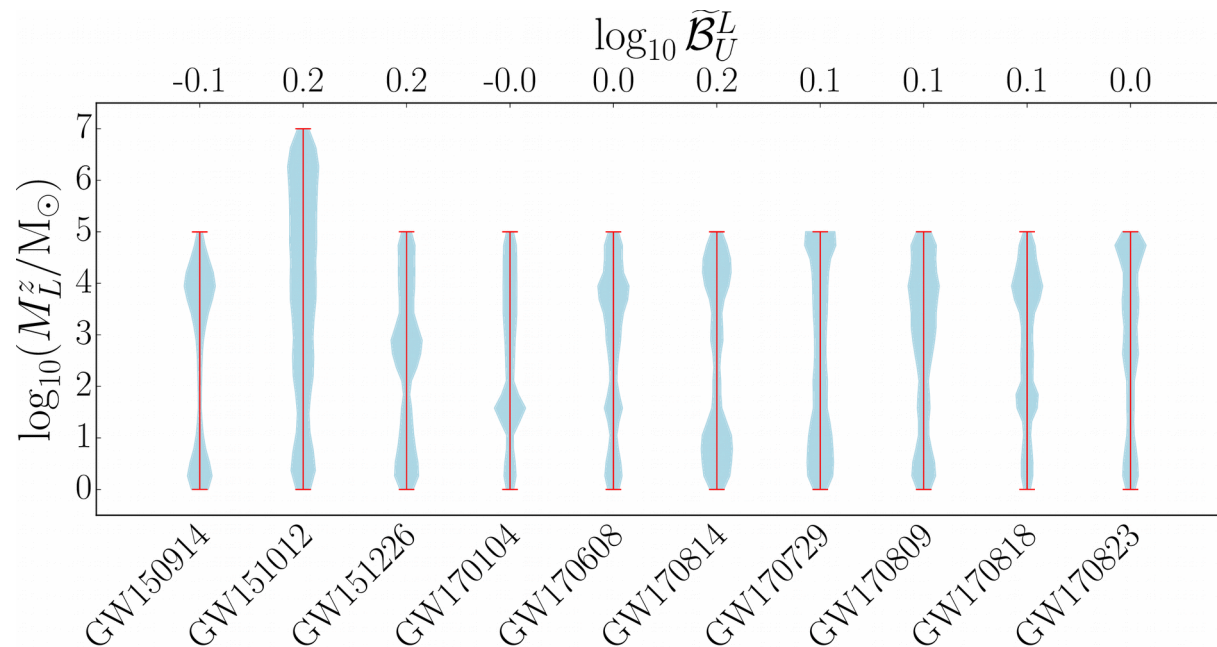
result:
no evidence for
lensed pairs



Lensing tests on O2

Test 3: wave optics effects?

- geometric limit breaks down for lens size \sim wavelength
→ for stellar-mass BBH signals: lenses $< 10^5 M_\odot$
- search for frequency-dependent magnification from point-mass lenses
(modified PhenomPv2 waveforms following [Lai+2018](#))

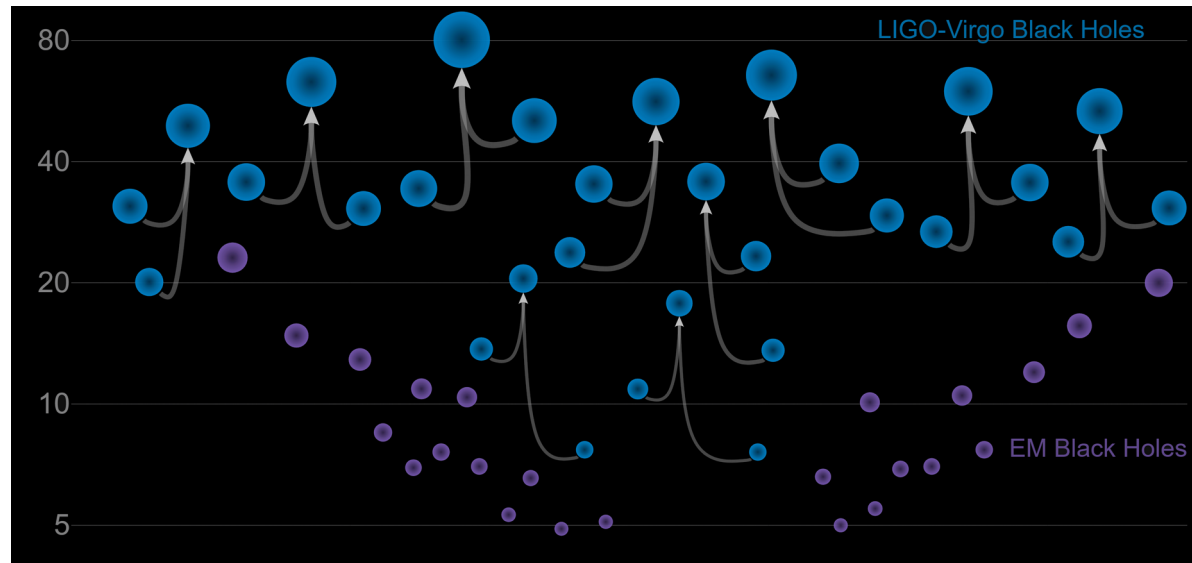


[ApJL 874:L2]

- no evidence for such distortions in any O1+O2 event

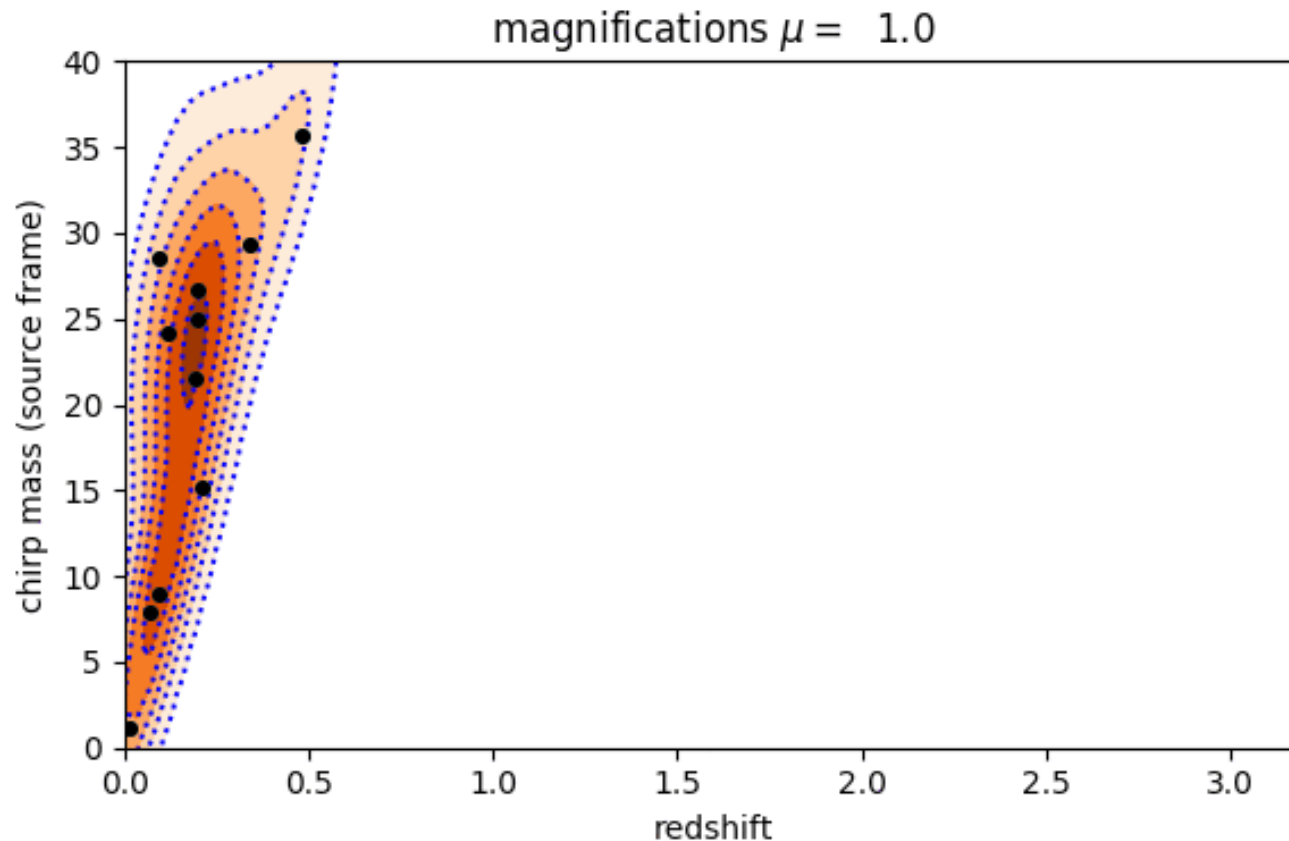
and now, actually about the title of this talk...

Could gravitational lensing impact the observed BBH population?



- We generally can't tell if an individual GW is lensed.
- But even less extreme lensing hypotheses than Broadhurst+ can leave imprints in the observed BBH population.
- If our population modelling doesn't include the lensing possibility, results may be biased.

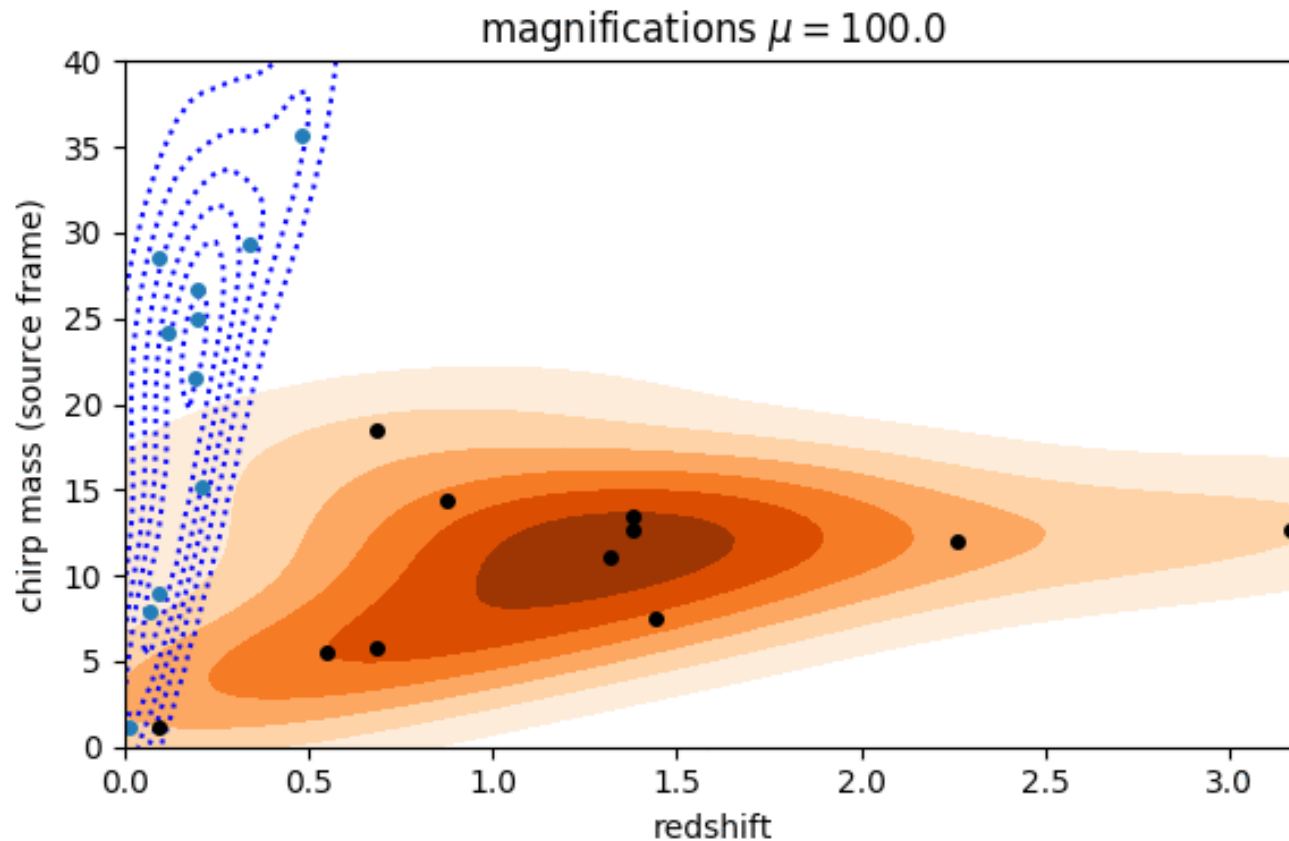
Could gravitational lensing impact the observed BBH population?



silly assumption of fixed magnification for all GWTC-1 events

remember: GW amplitude $\sim \sqrt{\text{magnification}}$

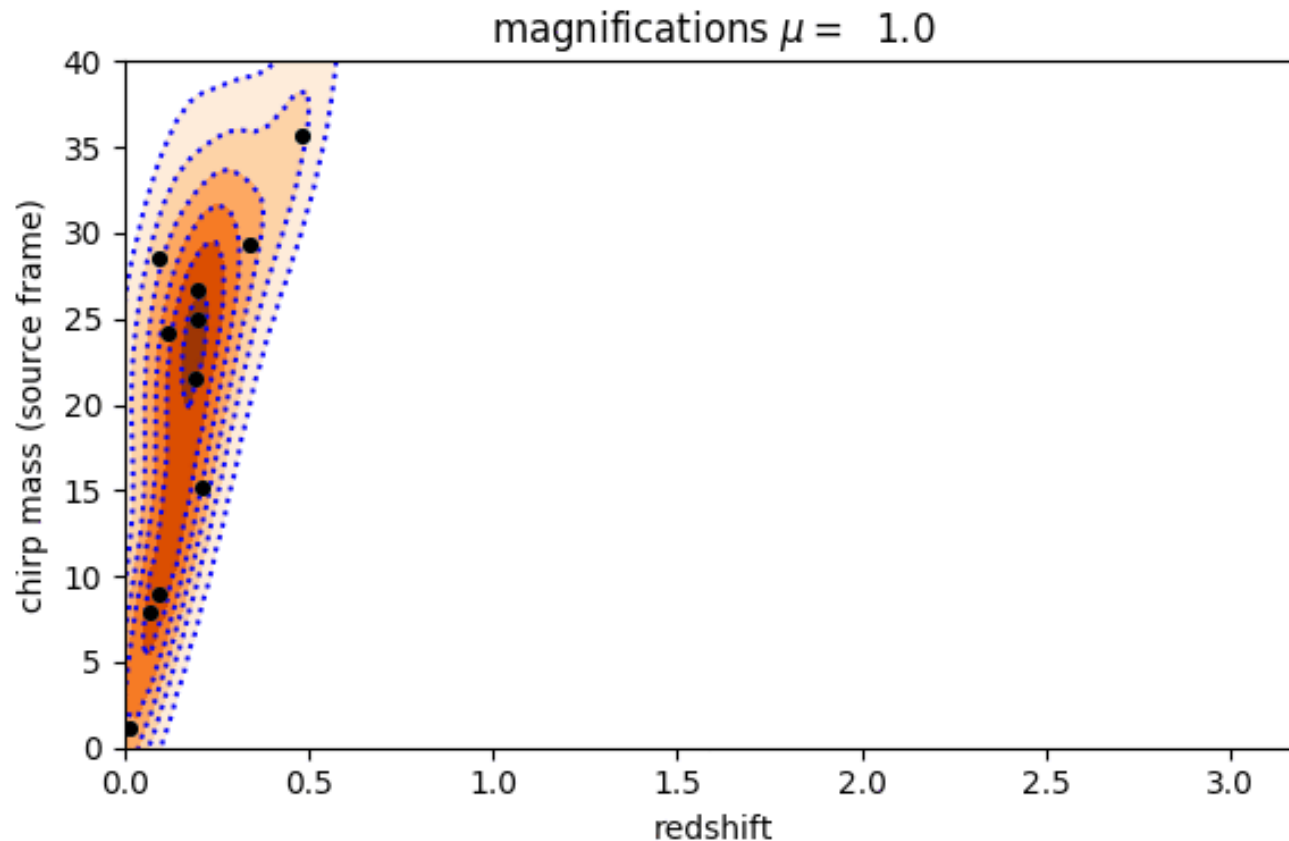
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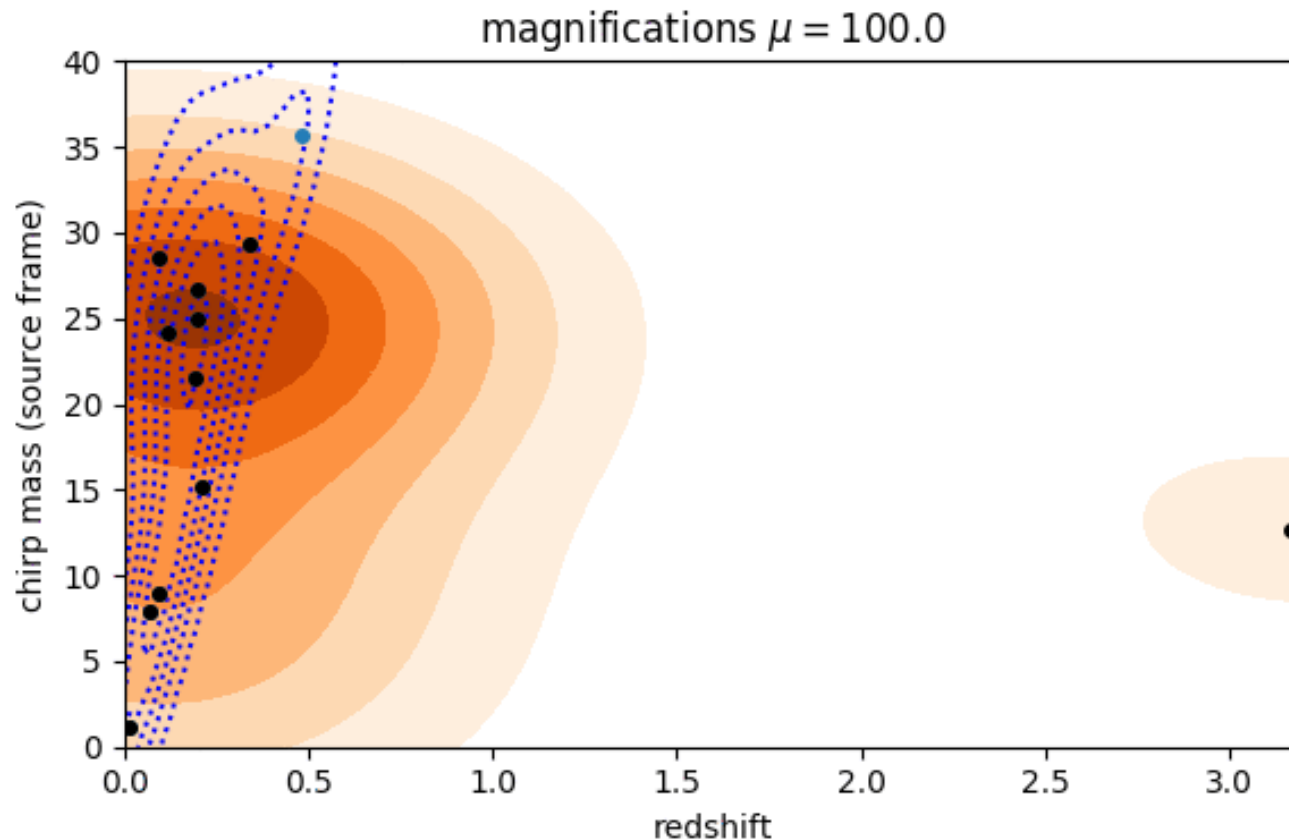
Could gravitational lensing impact the observed BBH population?



just one highly lensed event can distort pop inference
if the model is not flexible enough

remember: GW amplitude $\sim \sqrt{\text{magnification}}$

Could gravitational lensing impact the observed BBH population?

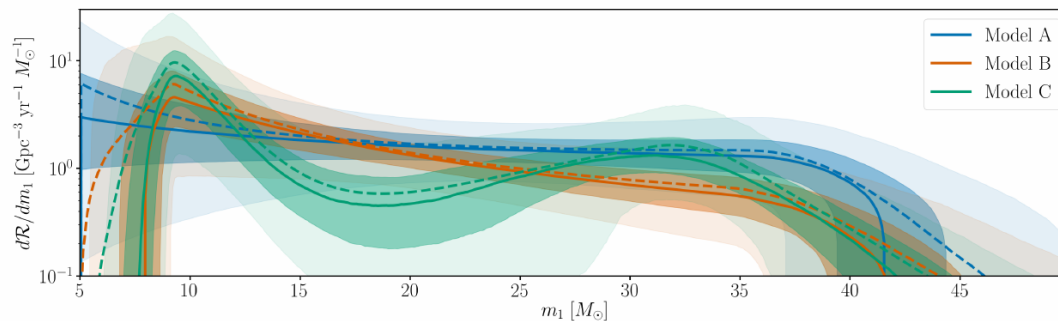


just one highly lensed event can distort pop inference
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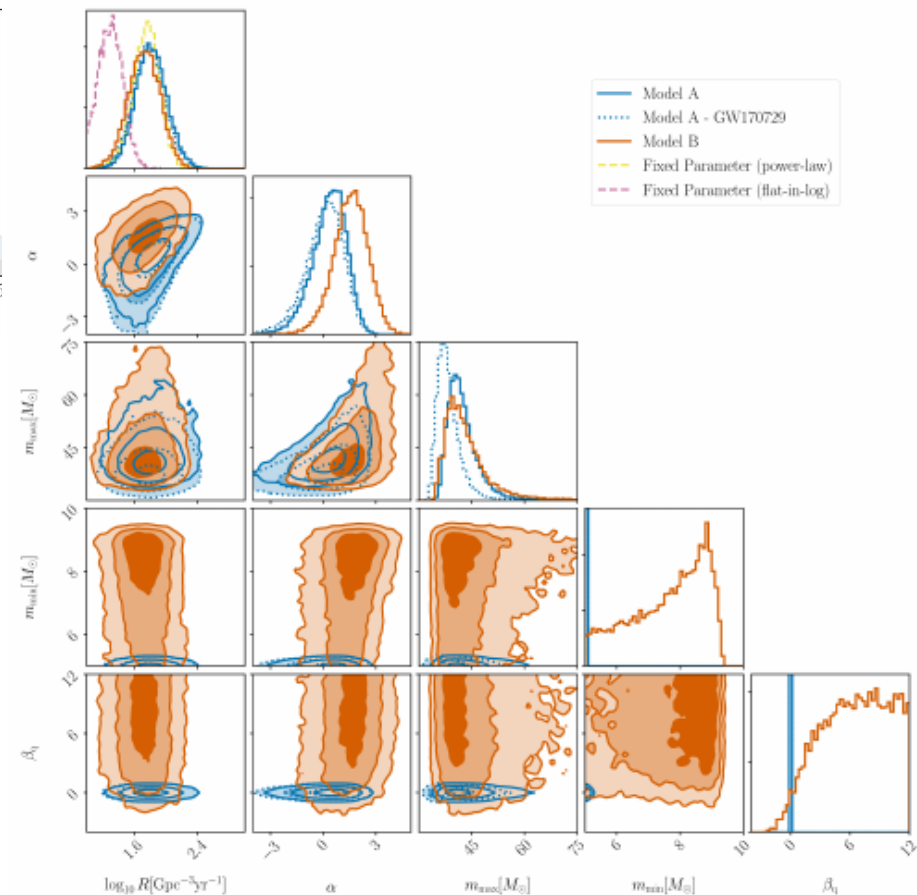
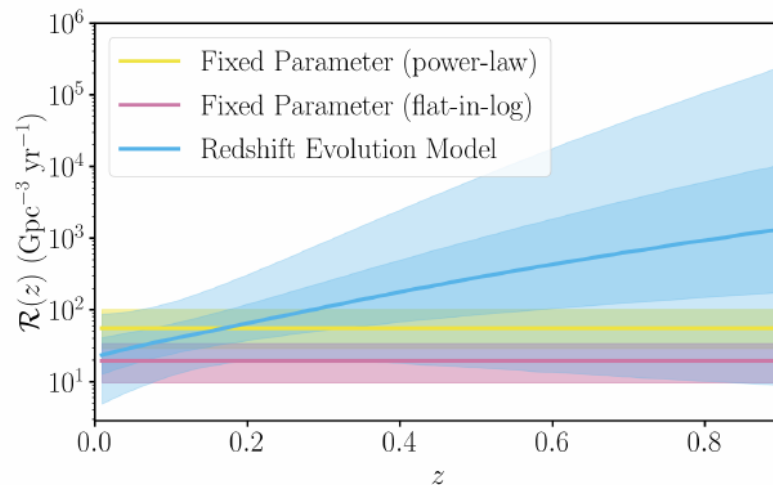
remember: GW amplitude $\sim \sqrt{\text{magnification}}$

BBH population modelling

- admittedly, state-of-the art modelling is *quite a bit smarter* than `matplotlib.contour()`... ;-)
- key concepts: Hierarchical Bayes, hyperparameters



[LVC arXiv:1811.12940]



BBH population modelling + lensing?

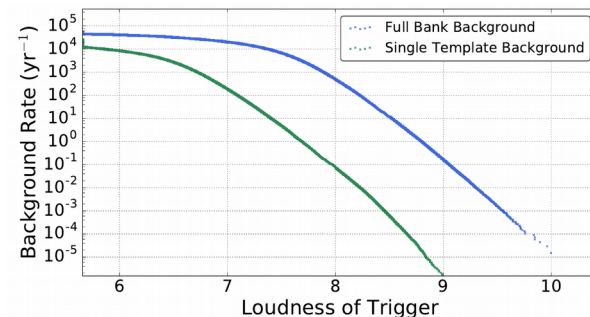
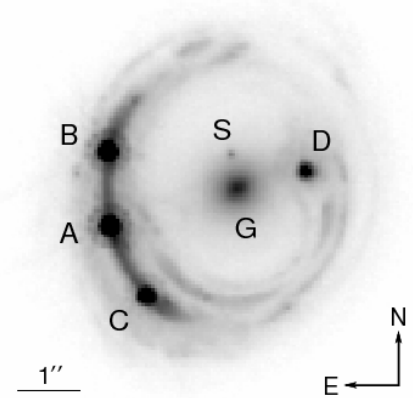
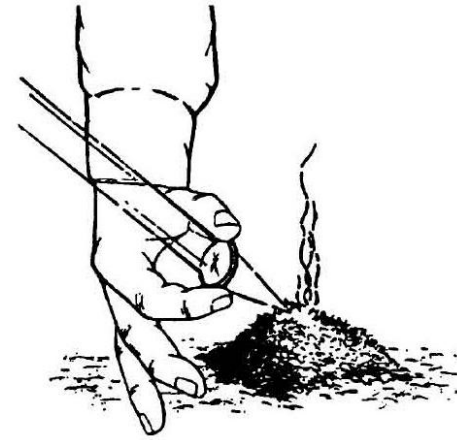
- Hierarchical Bayesian approach in [1811.12940](#) can be extended with arbitrary additional parameters.
- Sufficiently flexible generic $M(z)$ models can in principle account for lensing already. [see e.g. Fishbach et al 2018, [ApJL 863:L41](#)]
- to *explicitly* include lensing:
 - free magnification parameter for each event
 - possibility of multiple images
 - new population hyperparameters:
overall lensing rate, magnification distribution, time delay distribution
- Sounds like it should make the full model very underconstrained and full of degeneracies.
- But theory, EM observations and simulations should already significantly constrain the lensing sector!
- The prior is still that lensing should be rare overall, but in O3+ it could be worthwhile to explicitly include it in hierarchical population modelling to make sure our inferences are robust against it.

breakers of degeneracies

“we generally can’t tell if an individual GW is lensed”

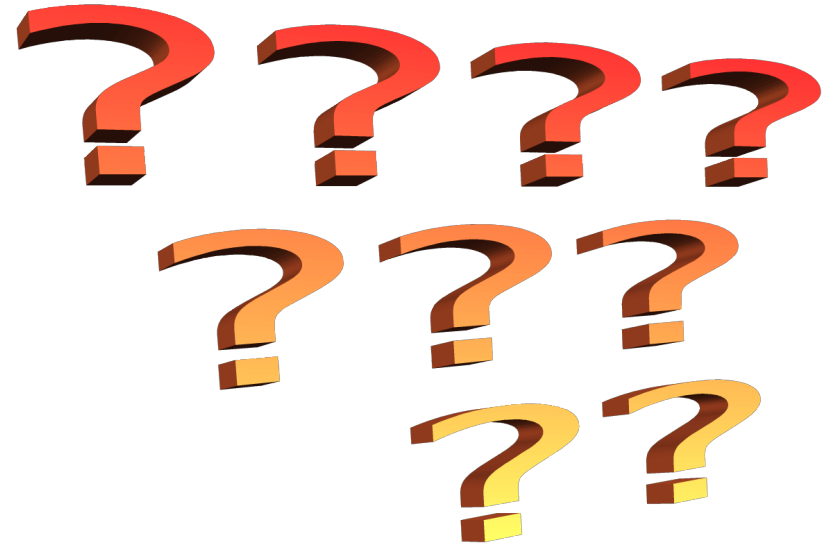
→ what would be smoking guns magnifying glasses to do so after all?

- identify a foreground object as the lens [[Smith+ 2018](#)]
problem: often huge sky localisation uncertainties, incomplete surveys
- microlensing / wave optics imprints on the waveform [[Lai+ 2018](#)]
problems: lens-model dependent, can look suspiciously like precession or eccentricity
- clearly lensed EM counterparts
problem: rare – but *the jackpot!*
 - measure H_0 from time delay [[Liao+2017](#)],
similar to standard quasar method [[Refsdal 1964](#), [Suyu+2013](#)]
 - test speed of gravity vs. light [[Fan+2017](#), [Collett & Bacon 2017](#)]
- subthreshold searches: strongly lensed events should come with short-delay counterparts [[Li et al 2019](#); [McIsaac, Keitel, et al. in prep.](#)]



Thanks for your attention!

Time for questions...



...and my thanks to collaborators
at Portsmouth and within the LVC

see you again before Christmas...?

30th Texas Symposium on Relativistic Astrophysics

15th - 20th December 2019

Portsmouth, UK

Invited speakers:

Antony Lewis (University of Sussex)

Astrid Eichorn (University of Southern Denmark
& Heidelberg University)

Chris Reynolds (University of Cambridge)

Claudia De Rham (Imperial College London)

Dany Page (National Autonomous University, Mexico)

Elena Gallo (University of Michigan)

Elena Rossi (Leiden University)

Elisa Resconi (Technical University Munich)

Elisabeth Krause [TBC] (University of Arizona)

Giovanni Losurdo (INFN Pisa)

Juan Garcia-Bellido (University of Madrid)

Luciano Rezzolla (University of Frankfurt)

Martin Lemoine (IAP, France)

Rennan Barkana (Tel Aviv University)

Takahiro Tanaka (Kyoto University)

Tanja Hinderer (University of Amsterdam)

Tom Giblin (Kenyon College Ohio)

Ulisses Barres de Almeida (CBPF)

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