

Aspects of X-ray data analysis for accreting compact objects: theory and results

Piotr Życki

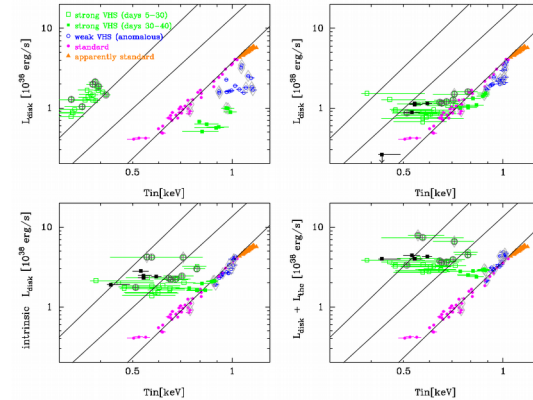
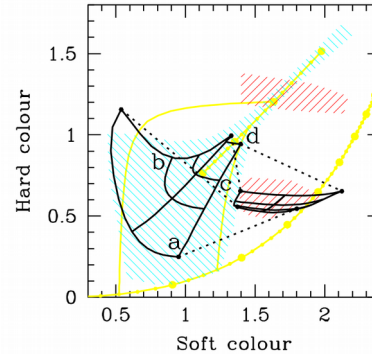
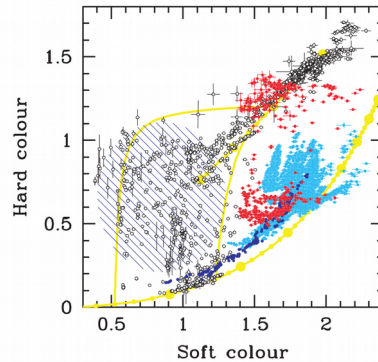
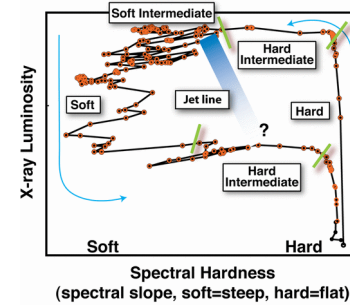
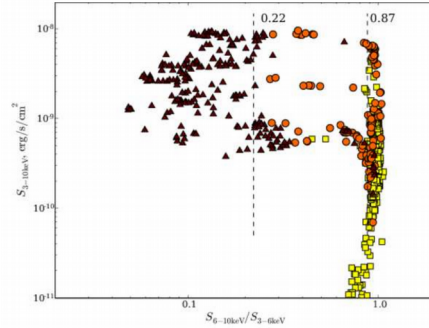
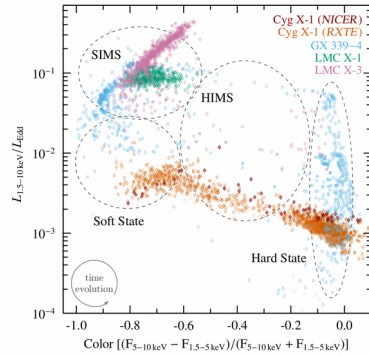
Nicolaus Copernicus Astronomical Center, Polish Academy of Sciences

Lecture 8, 9.12.2025

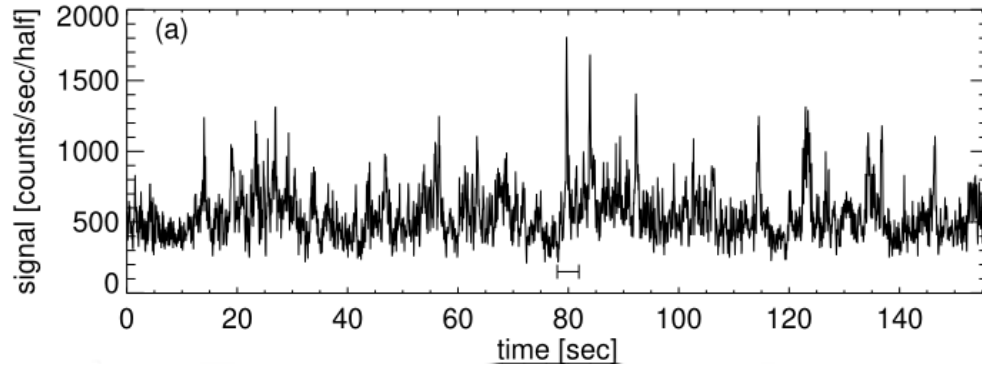
PhD lecture series, 2025, fall semester

Previous lecture

Color-color and color-intensity (HID) diagrams



More on X-ray variability



rms = 20-30%

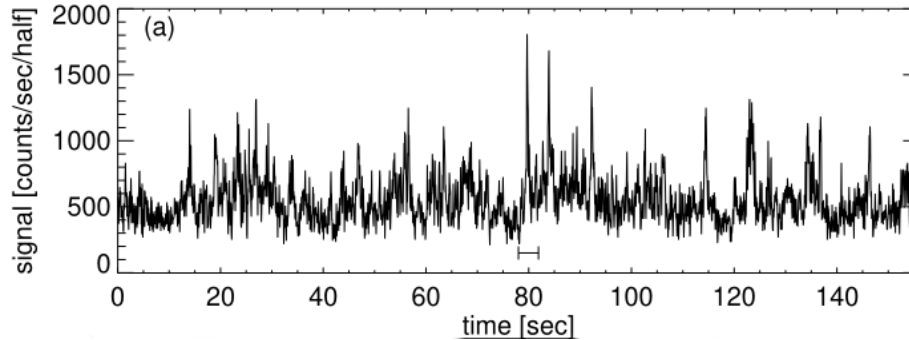
mean value $x_m = \frac{1}{N} \sum_i^N x_i$

std error $\sigma^2 = \frac{1}{N} \sum_i^N (x_i - x_m)^2$

std deviation $\sigma = \sqrt{\sigma^2} = \sqrt{\frac{1}{N} \sum_i^N (x_i - x_m)^2}$

root mean square $\text{rms} = \frac{\sigma}{x_m} = \frac{1}{x_m} \sqrt{\frac{1}{N} \sum_i^N (x_i - x_m)^2}$

More on X-ray variability



rms = 20-30%

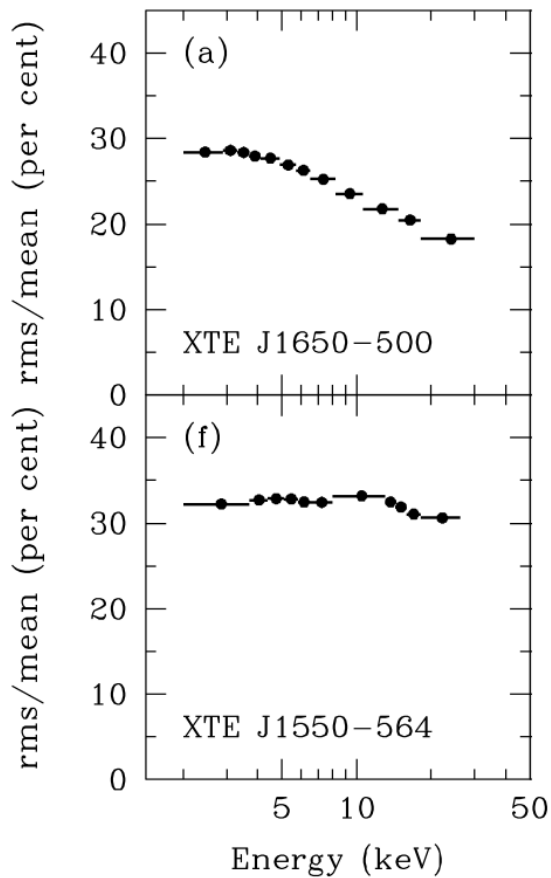
For a small number of events their distribution is given by a Poisson distribution

$$P(n) = \frac{e^{-\lambda} \lambda^n}{n!}, \quad \text{where } \lambda = \text{mean value}$$

The dispersion of the Poisson distribution = it's mean. If e.g. mean=10, then dispersion approx 3 → 30%

Note: the variability is not symmetric around the mean value!

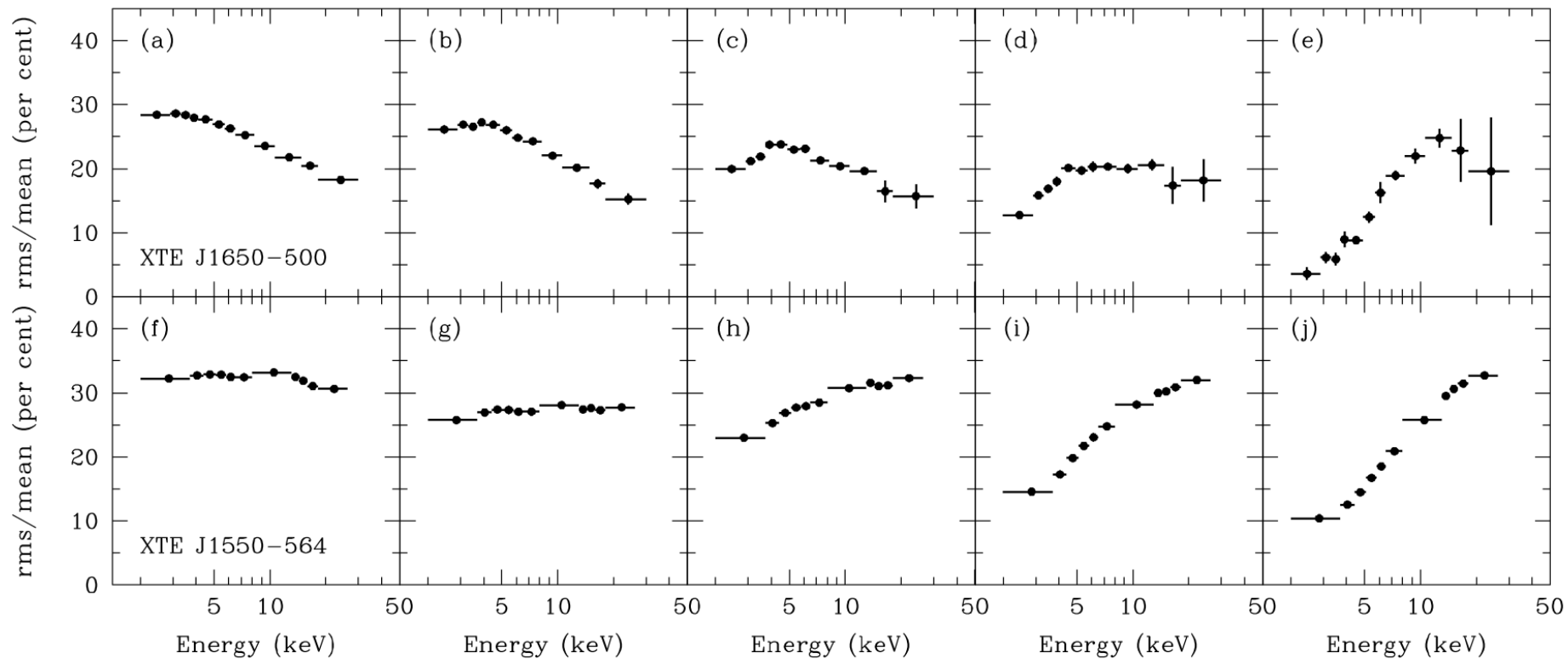
Dependence of variability on energy



Hard state

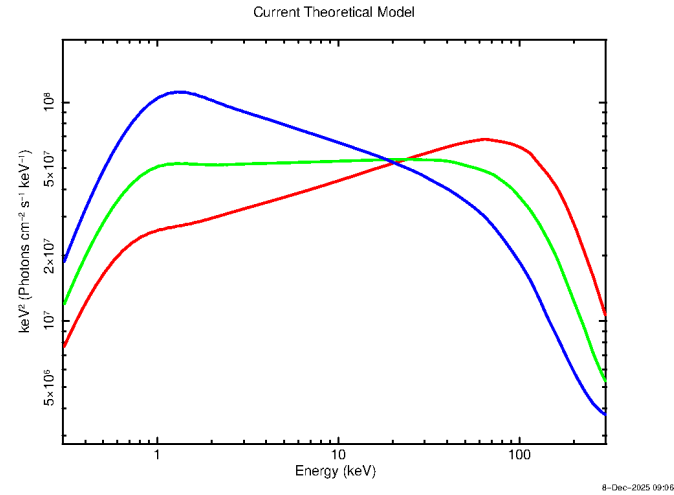
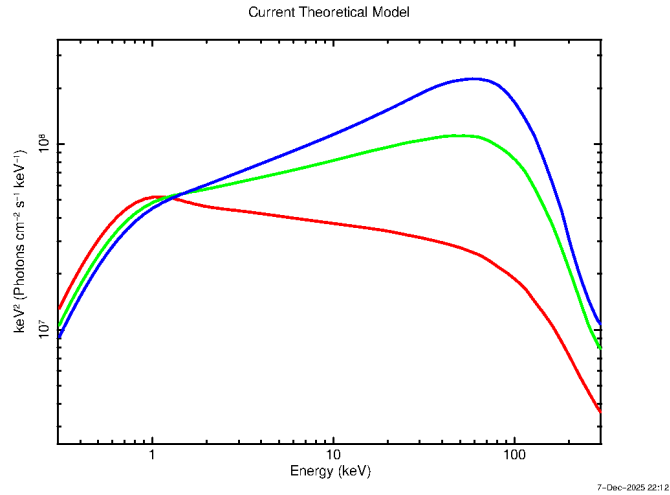
Time bin = 1/256 sec; duration = 512 sec

Dependence of variability on energy

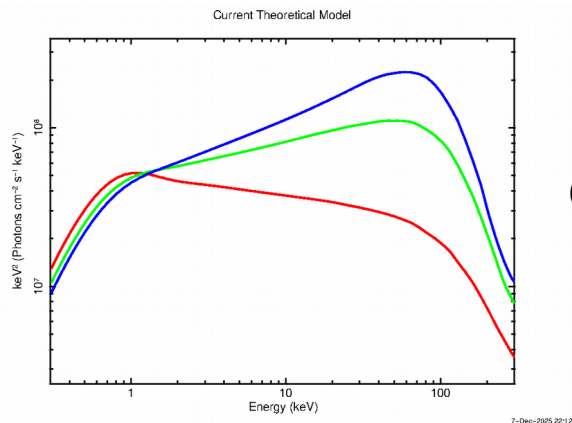


How to understand rms(E)

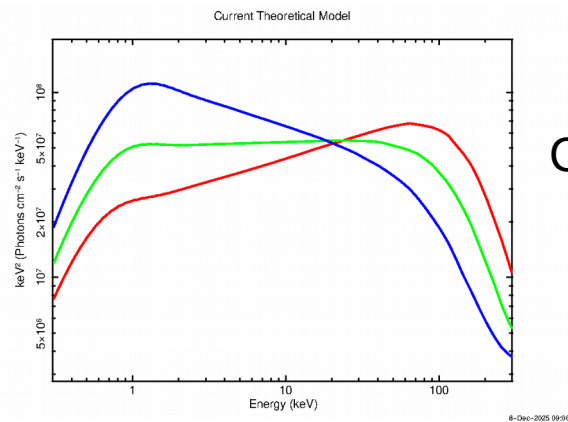
Changing luminosity together with a change of the spectrum



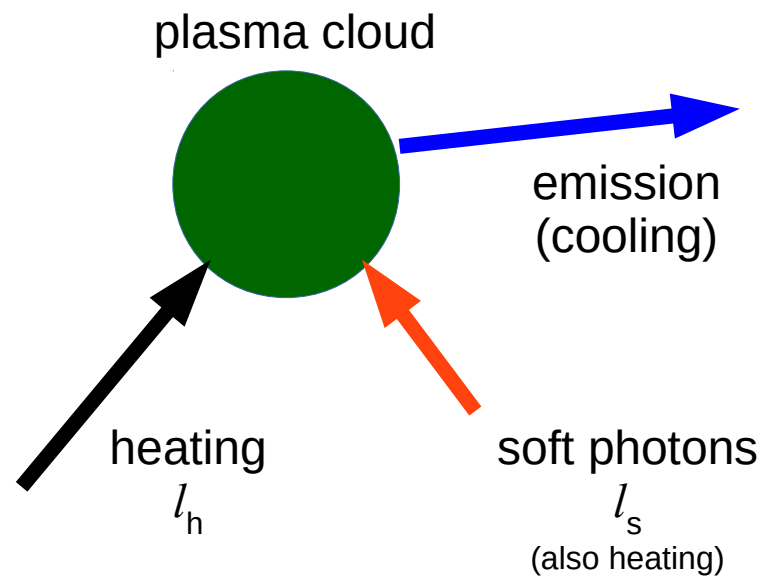
Spectral variability in Comptonized plasma



Changing l_h



Changing l_s



XTE J1650-500 – hard state

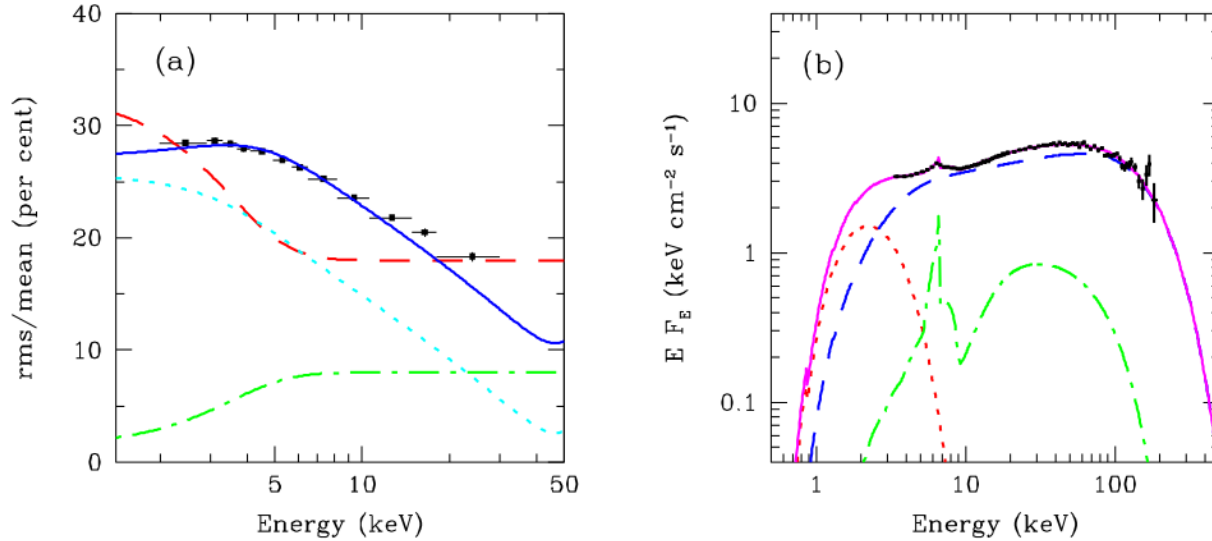
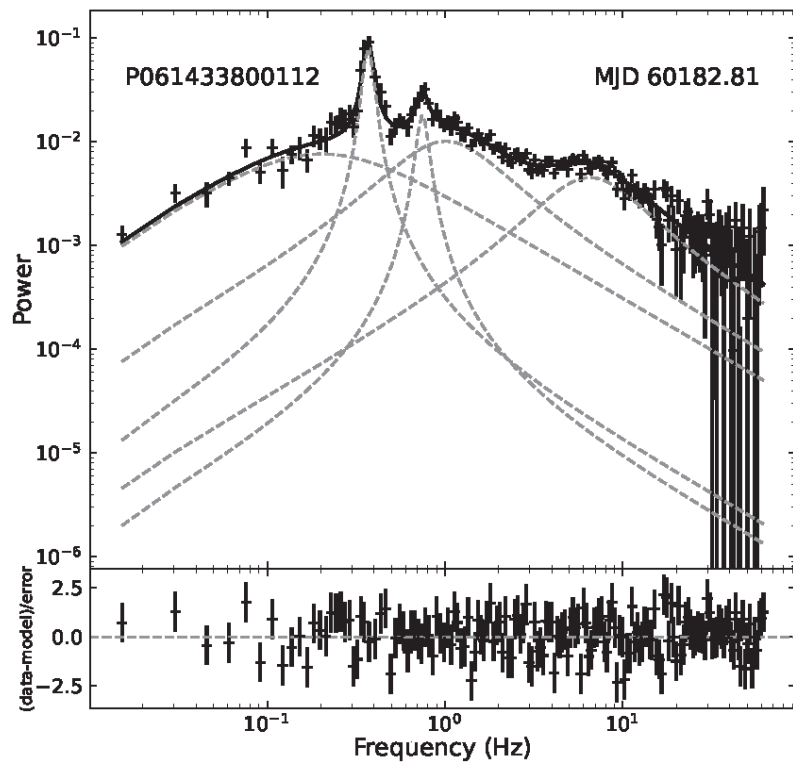
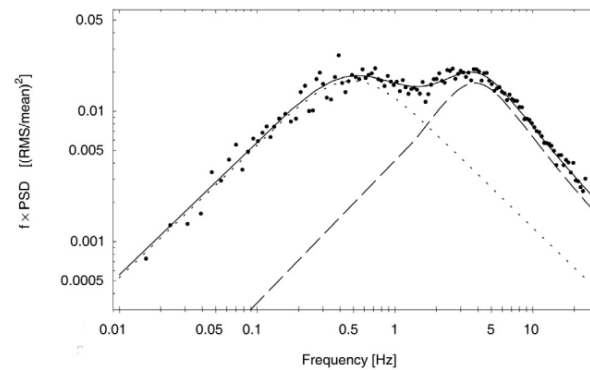


Figure 1. (a) Hard-state (obsid 60113-01-04-00) rms spectrum of XTE J1650–500 observed by *RXTE*. The dashed curve (red in the colour version of the figure online) represents the two-component variability model, with $r(N_s) = 0.36$ and $r(N_h) = 0.18$, clearly not consistent with the data. The solid (blue in colour) curve shows the model with varying soft photon input (dotted curve, cyan in colour) at $r(\ell_s) = 0.25$ plus an additional hard component normalization variability (dash-dotted curve, green in colour) with $r(N_h) = 0.08$. (b) Energy spectrum of the same observation, with the unfolded PCA and HEXTE data together with the best-fitting model. The model consists of the following components: the soft component modelled by DISKBB (dotted curve, red in colour, showing unscattered seed photons only), its Comptonization in thermal plasma (dashed curve, blue in colour) and reflection (dash-dotted curve, green in colour). The solid curve (magenta in colour) shows their sum.

Quasi-periodic oscillations



VS



Quasi-periodic oscillations in AGN

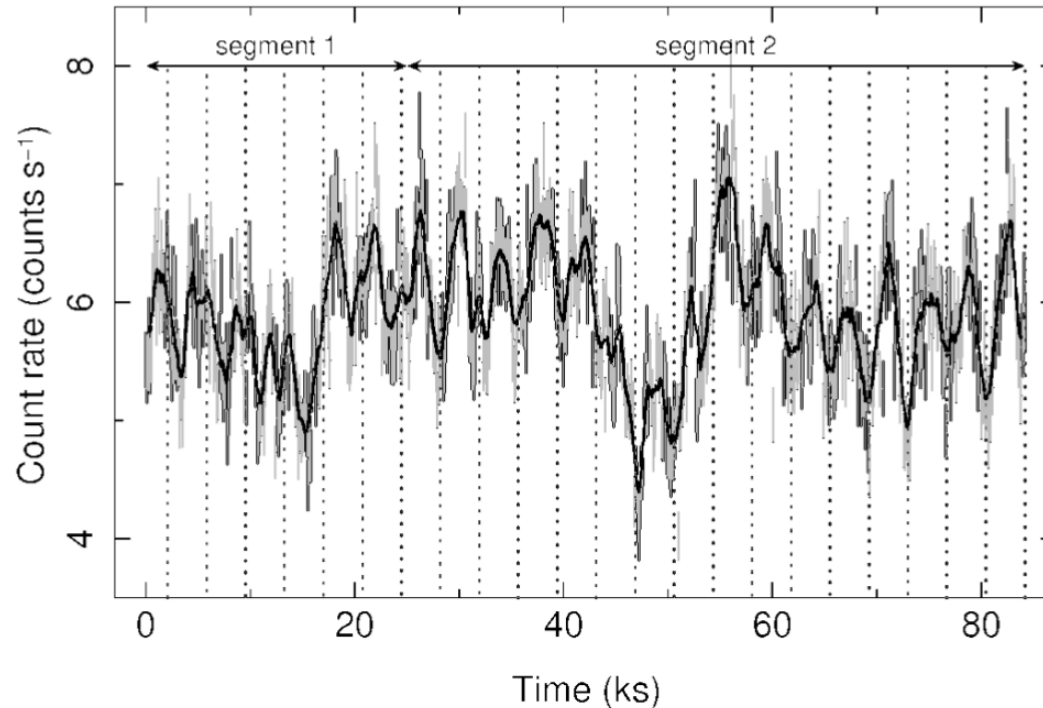


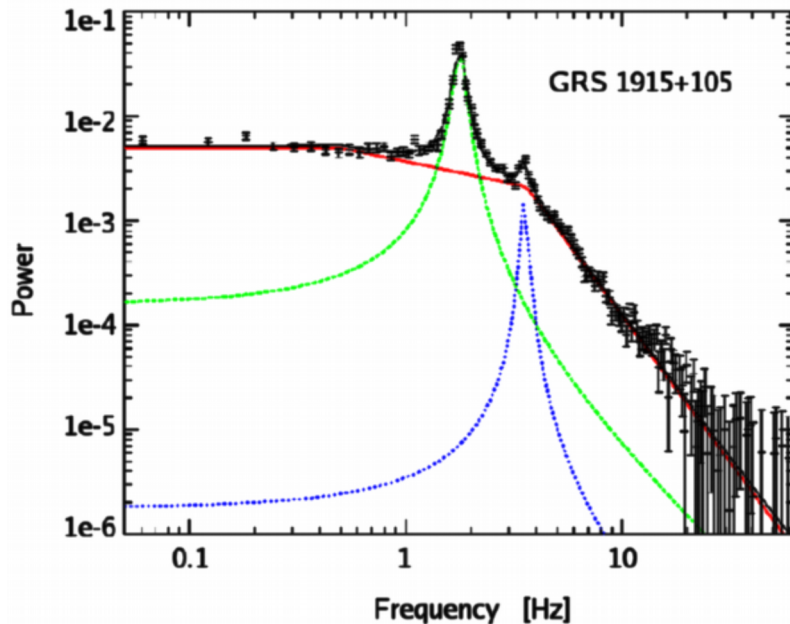
Figure 1 | XMM-Newton light curve of RE J1034+396.

The mechanism of quasi-periodic oscillations

Some kind of disk oscillations, vertical or radial (diskoseismology)
(Robert Wagoner et al., 1990-ies – early 2000)

If so, then it would be the disk emission that would be oscillating

Energy spectra of Quasi-periodic oscillations

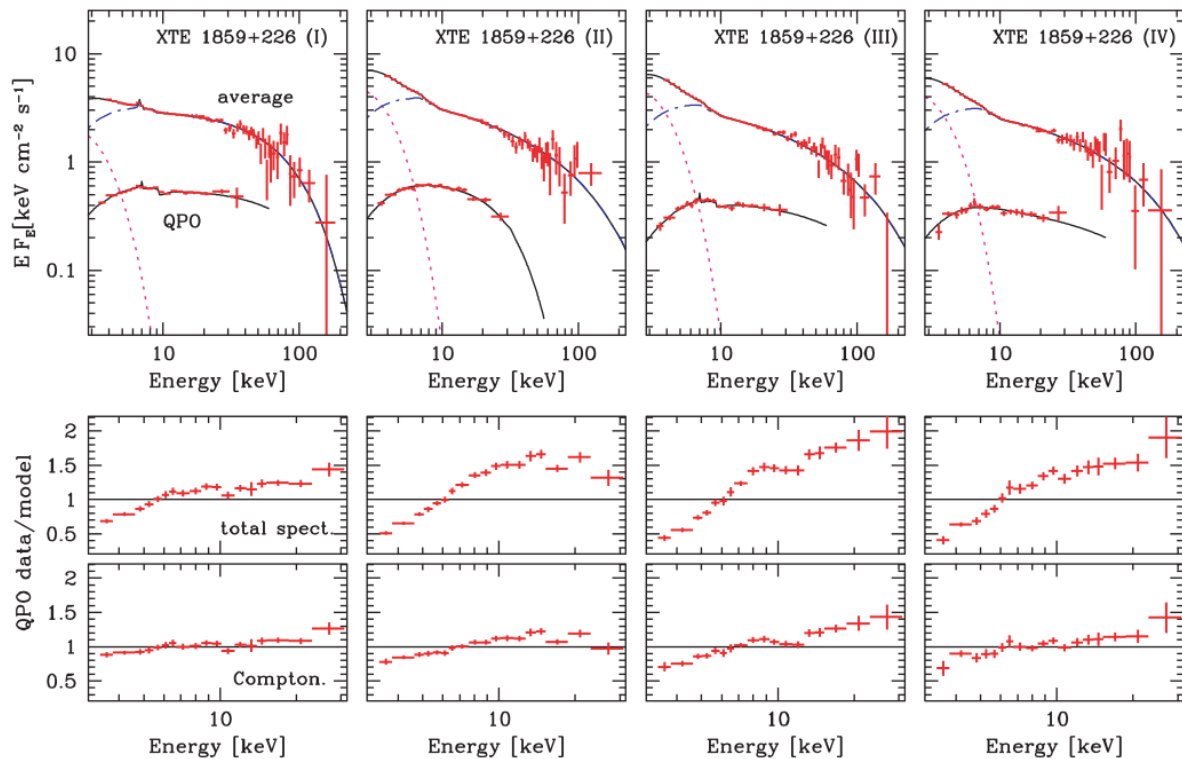


Model the power spectrum: power law or a sum of Lorentz functions for the continuum, and a Lorentzian for the QPO, **as a function of energy**.

Integrate the QPO Lorentzian over frequency to obtain its total variability amplitude.

$$\sigma(E) = x_m * \text{rms}(E) \quad - \text{ QPO energy spectrum}$$

What oscillates in QPO?

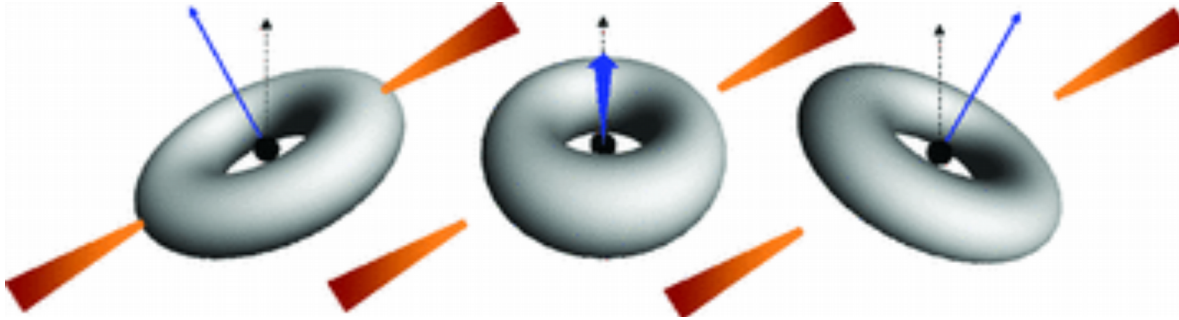


What oscillates in QPO?

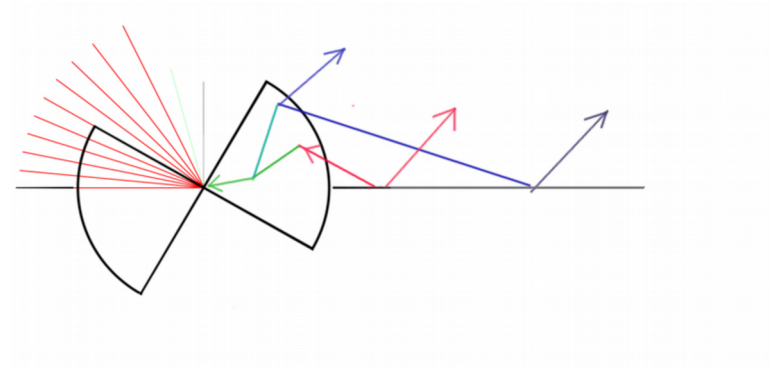
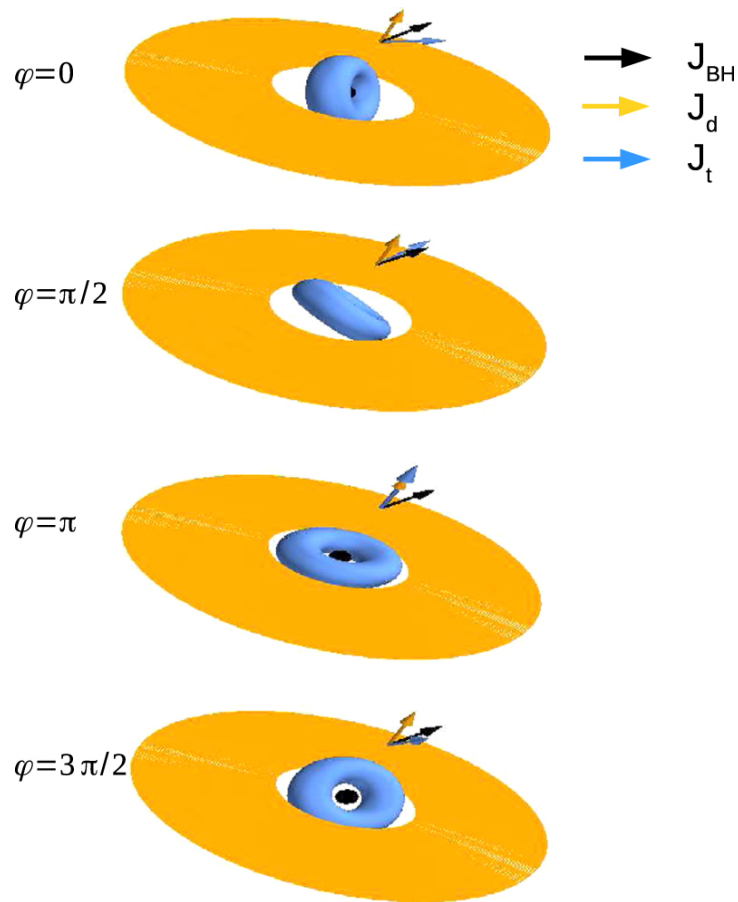
It is the **hard X-rays** that oscillate in QPO in X-ray binaries.

The disk emission does not participate in these oscillations.

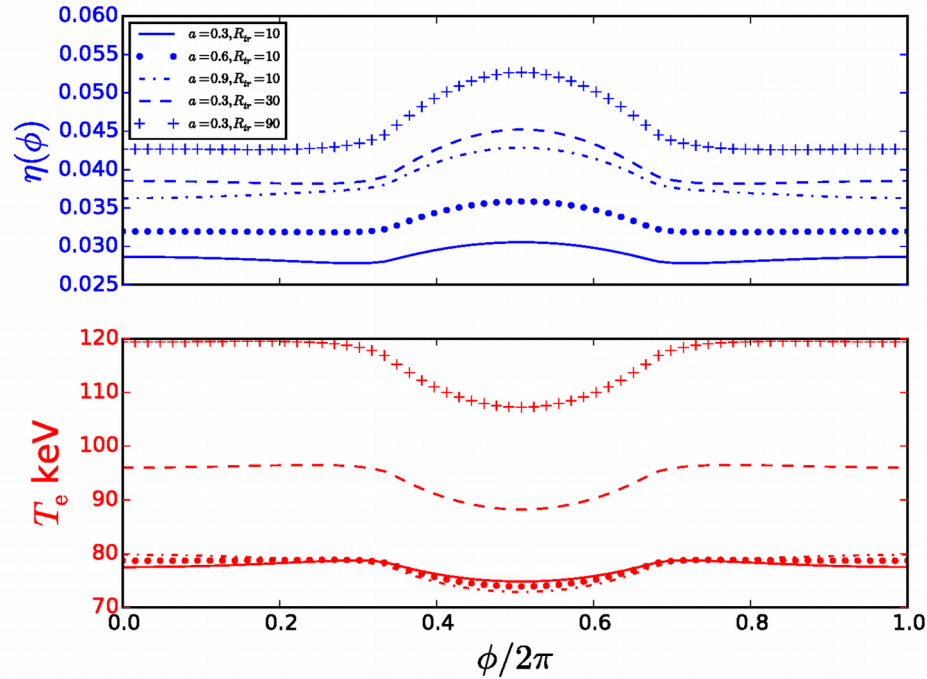
Lense-Thirring precession model



Lense-Thirring precession model



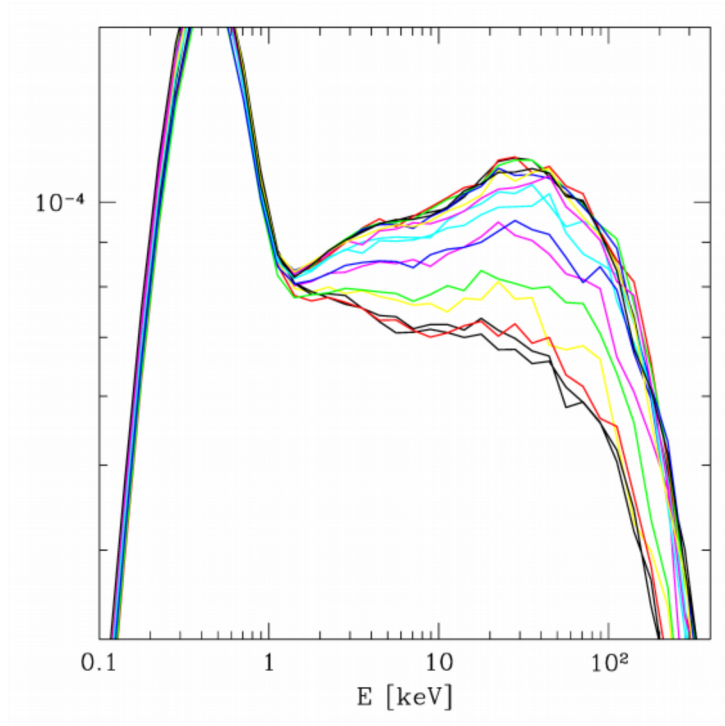
Lense-Thirring precession model



Fraction of the disk emitted energy intercepted by the hot torus

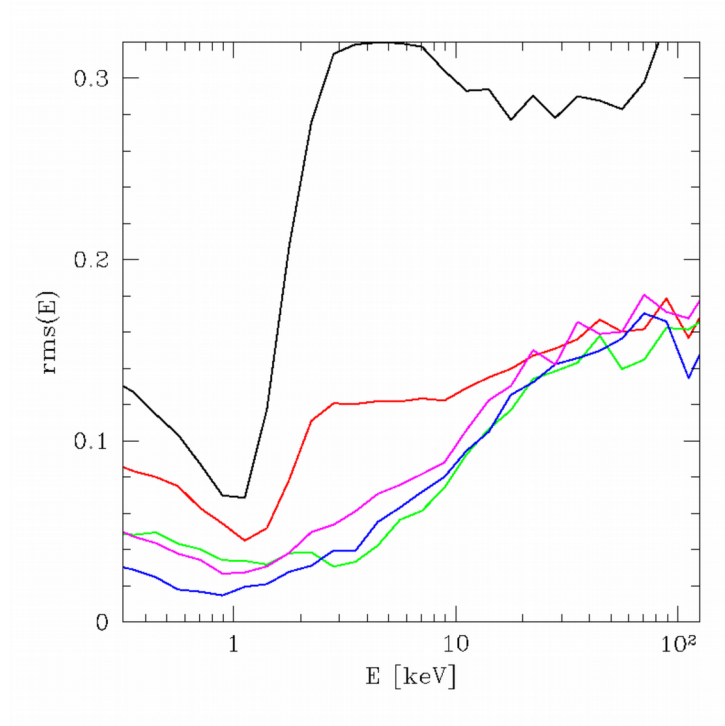
Electron temperature

Lense-Thirring precession model



Evolution of the spectrum during a QPO cycle

Lense-Thirring precession model



$\text{rms}(E)$