Aspects of X-ray data analysis for accreting compact objects: theory and results

Piotr Życki

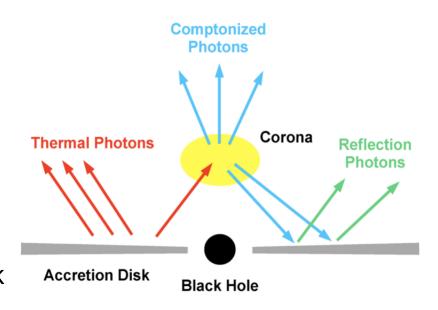
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PhD lecture series, 2025, fall semester

Lecture 3

Overall geometry

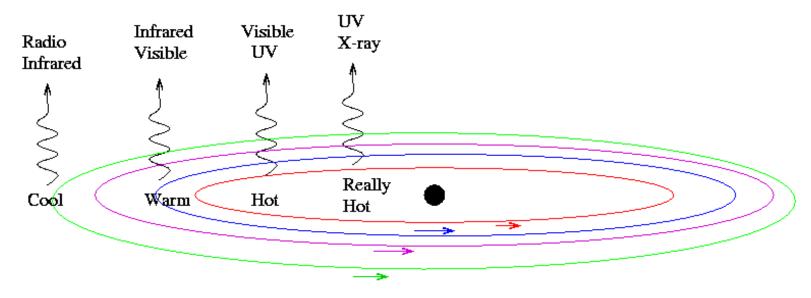
- Accretion disk around central black hole or neutron star.
- X-ray source:
 - Compact source
 - Extended corona
- Emission from the accretion disk
- Reflection/reprocessing by accretion disk



Thermal emission from accretion disks

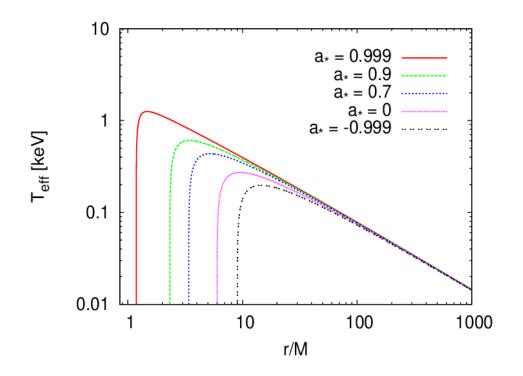
- Usual assumption: Keplerian rotation; locally blackbody radiation
- Radial dependance of temperature

$$F(r) \approx \frac{1}{r^3}$$



Thermal emission from accretion disks

- Usual assumption: Keplerian rotation; locally blackbody radiation
- Radial dependence of temperature



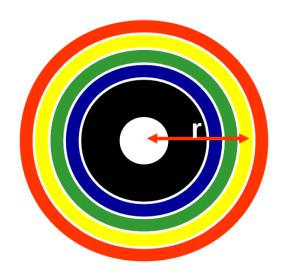
$$F(r) \approx \frac{1}{r^3} \left(1 - \sqrt{\frac{6}{r}} \right) \qquad \text{for a*} = 0$$

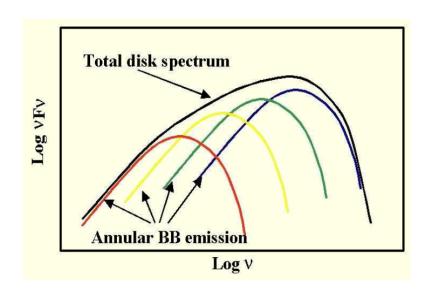
50% of power released between 6 and 25 $\rm R_{\rm g}$

Bambi, Cosimo. (2024). Black hole X-ray spectra: notes on the relativistic calculations. 10.48550/arXiv.2408.12262.

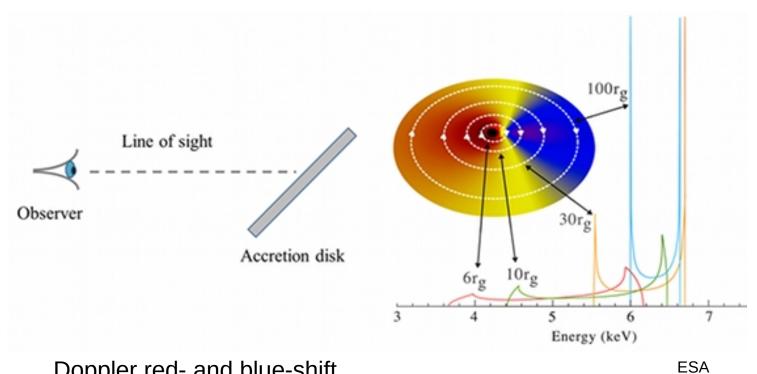
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- Usual assumption: Keplerian rotation; locally blackbody radiation
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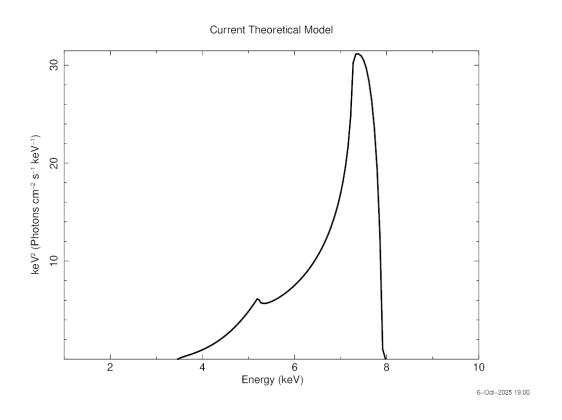


Reflection from a relativistic accretion disk

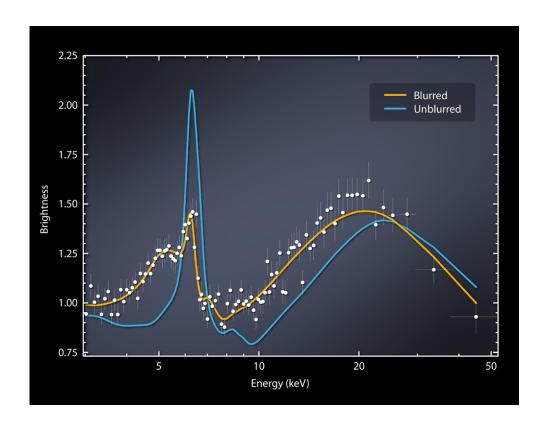


Doppler red- and blue-shift, Doppler boost, gravitational redshift

Reflection from a relativistic accretion disk



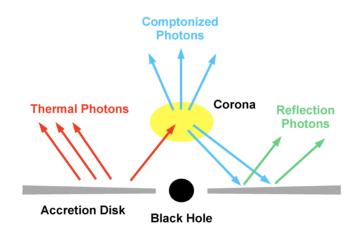
Effect on a spectrum



Effect on a spectrum

Radial structure – at each radius (ring) a different input spectrum and relativistic effects

Applies to all spectral components emitted at a given radius, assuming the emitter rotates – applies to accretion disk thermal emission, hard X-ray emission, reflection component



Short summary of spectral components

- Primary X-ray emission (non)thermal Comptonization, E>1 keV, power law $N_F \sim E^{-\Gamma}$
 - Hard spectral index Γ <2; goes **up** on EF_{Γ} plot; most of the energy around 100 keV
 - Soft spectral index Γ >2; goes **down** on EF_{ϵ} plot; most of the energy around 1 keV
- Reflection/reprocessing: spectral component peaking around 30 keV
- Accretion disk thermal emission: disk blackbody composition of black body spectra from different radii. Blackbody emission: disk is optically thick (geometrically thin)
- Relativistic effects, broadening of spectral features

Spectra of Cygnus X-1 in hard and soft state

High – mass X-ray binary, $M_{BH} \approx 20 M_{\odot}$, $M_{C} \approx 30 M_{\odot}$, $P_{orb} \approx 5.6 day$

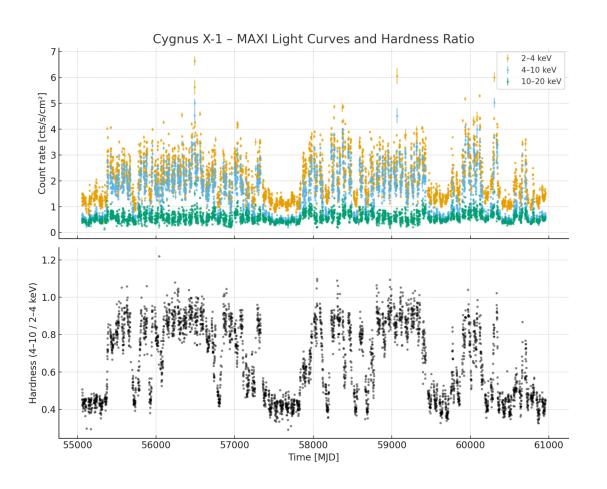
Discovered in 1964

In 1974 Stephen Hawking bet against Kip Thorne that Cyg X-1 is not a black hole. Admitted losing the bet in 1990.

One of the most observed BH sources

Shows a number of states, differing in spectral and temporal properties

Cyg X-1 long term X-ray lightcurve



Changes of count rate and hardness ratios

Spectra of Cygnus X-1 in the hard state

Hard X-ray component, well modelled by thermal Comptonization, with slope $\Gamma \approx 1.6$, kT ≈ 100 keV

Reflection component present, with Fe K α line at 6.4 keV.

Amplitude of the spectral component \approx 0.3 of that expected in the simplest geometry.

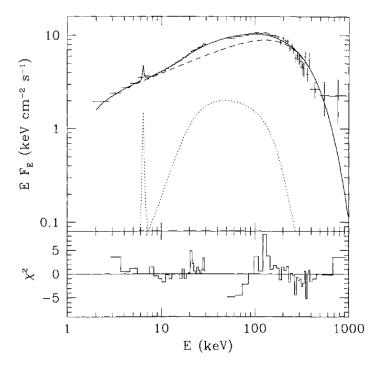
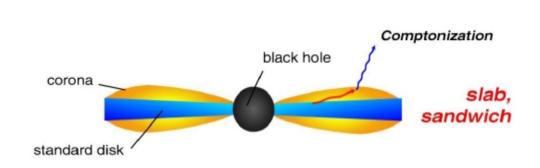


Figure 3. The isotropic one-temperature thermal Comptonization model fitted to the data set 2. The upper panel shows the data (crosses), the thermal Comptonization continuum (dashed curve) and the reflection component (dotted curve). The solid curve shows the sum. This model yields $\chi^2_{\nu} < 1$, but there is still a systematic residual pattern for the OSSE data (the lower panel).

Comptonization – the amplification factor



$$\Gamma \! \approx \! rac{7}{3} \, A^{-1/6}$$
 Beloborodov, 1999

For A=2 the photon index $\Gamma \approx 2.05$

In this geometry Γ can never be smaller than 2

A hard spectrum is not possible!



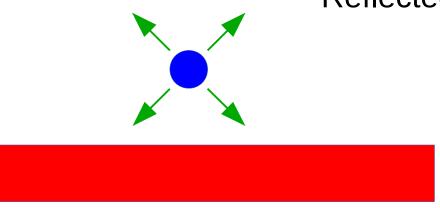
Fraction of energy dissipated in the disk

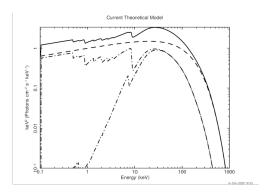
$$L_h = (1 - f)L_{tot}$$

$$\begin{split} L_s &= f \, L_{tot} + 0.5 * (1 - f) \, L_{tot} \\ A &= \frac{L_h}{L_s} \quad - \text{ amplification:} \end{split}$$

F. Haardt, L. Maraschi, 1991, ApJ, 380, L51

Reflected component





From the point-of-view of the X-ray source, half of the sky is covered by the reflector.

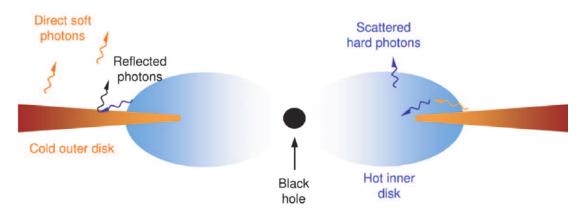
Reflection amplitude $R = \frac{\Omega}{2\pi}$ (also need to assume that the emission is isotropic)

Then, *R*, as determined from the fit to the data, provides information about the geometry.

Spectra of Cygnus X-1 in the hard state

"Photon-starved plasma" - cannot be a simple slab disk-corona geometry

Low amplitude of reflection, R=0.3, confirms the above



Inner hot accretion flow model

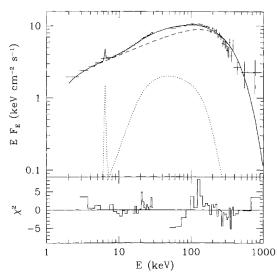


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