

Turbulence and magnetic configurations in neutron star interiors

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MERLIN project

The Magnetic Field Dynamics in Neutron Stars

<https://merlin-neutronstars.bitbucket.io/>

OPUS-LAP

Joint NCN - DFG grant, CAMK and FSU Jena



Bryn Haskell (PI), **Raj Kishor Joshi (postdoc)**, [Ankan Sur (alumnus)]

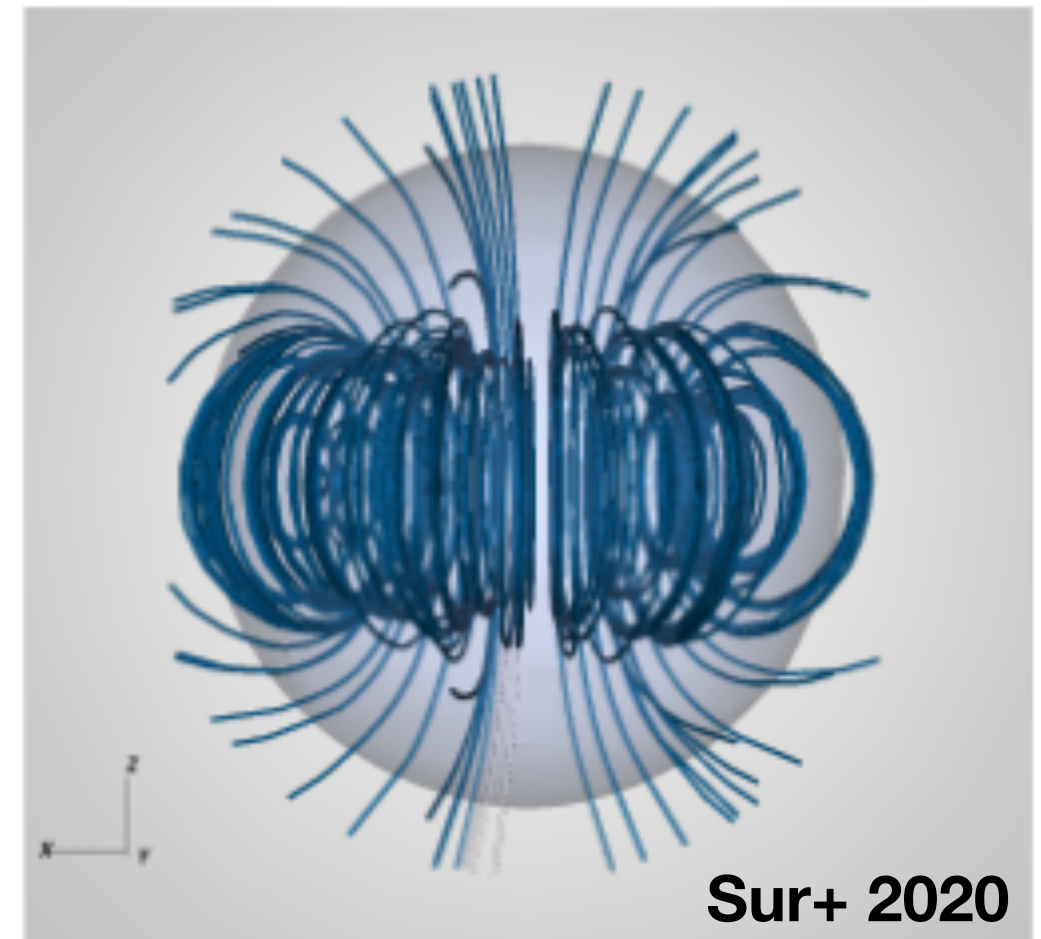


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[**William Cook (postdoc)**]

Physical problem

- Magnetic field configuration in NSs unknown
- Evidence for dipole far from the star, but NICER suggests more complicated structure

[Gendreau + 2016, Bilous + 2019, Sur + 2024]



- Dipole is unstable and a toroidal component is needed to stabilise the field (how strong?)

[Tayler + 1957, 1973, Markey and Tayler 1973, 1974]

[Braithwaite+ 2006 2009, Cioffi+ 2011, 2013, Lasky+ 2011]

- Turbulence plays a role in the evolution of the field

[Sur + 2020, 2021, Sarin+ 2023]

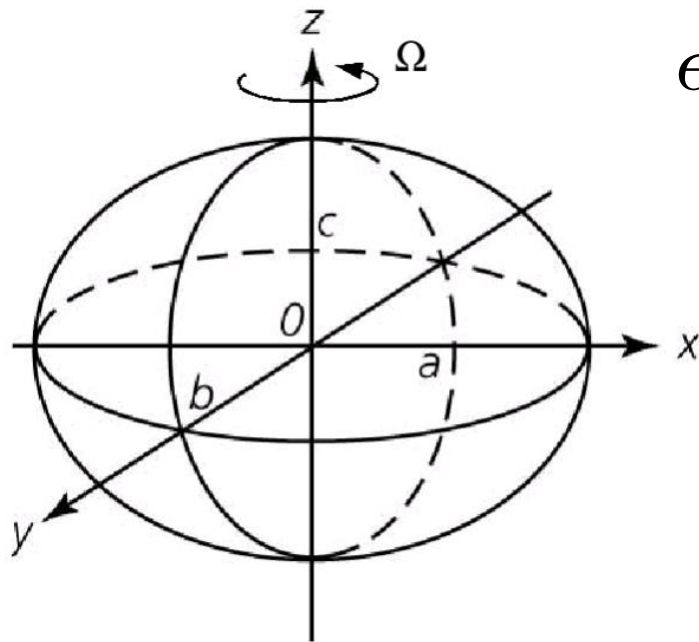
Minimum ellipticity

- **A magnetised NS (or a merger remnant) produces a 'continuous' GW signal**

[Bonazzolla and Gourgoulhon 1996]

$$10^7 \text{ G} \lesssim B \lesssim 10^{16} \text{ G}$$

- Magnetic fields can support a quadrupole in the star



$$\epsilon = \frac{I_{xx} - I_{yy}}{I_{zz}}$$

- GW emission at $2\nu_{spin}$ and ν_{spin}

$$\epsilon \propto 10^{-11} \left(\frac{B}{10^{12} \text{ G}} \right)^2$$

Magnetic deformation

$$\epsilon \propto 10^{-9} \left(\frac{B}{10^{12} \text{ G}} \right) \left(\frac{H_c}{10^{14} \text{ G}} \right)$$

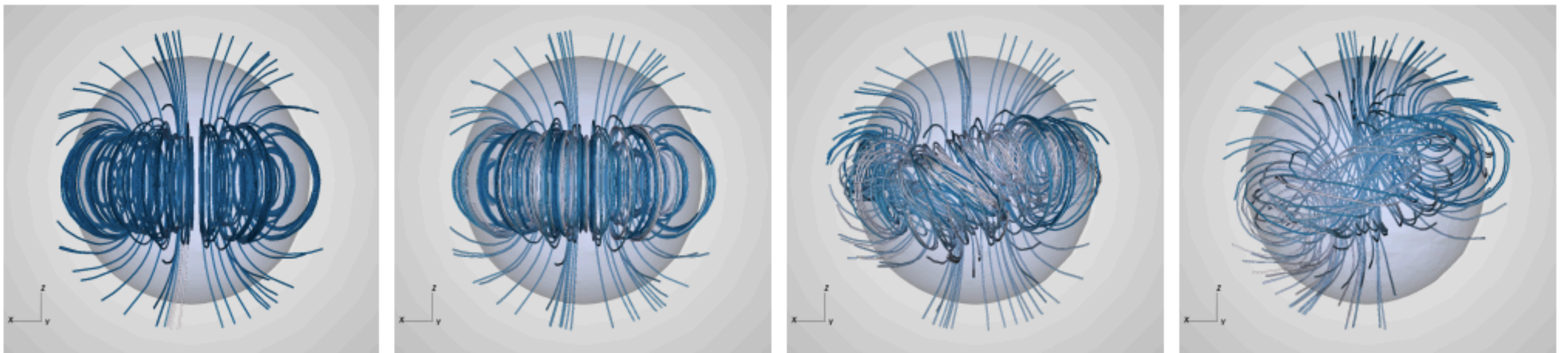
- Evidence for residual deformation in the radio pulsar population

[Woan+ 2018]

Project objectives

- Perform long-term high resolution simulations of isolated NS to investigate magnetic configurations
- Tool of choice AthenaK [**Stone et al. 2024, Zhu+ 2024, Fields+ 2025**]
- Investigate turbulent cascades in magnetised stars [**Sur et al. 2021**]
- Use insight to investigate GW emission and simulate mergers of magnetised BNS

Sur+ 2020

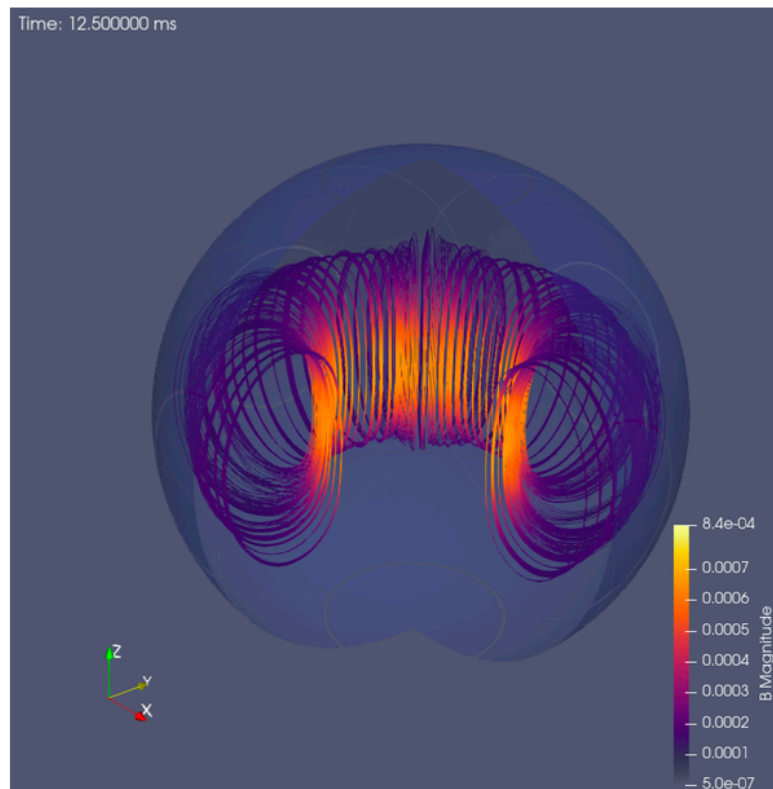


Problem setup

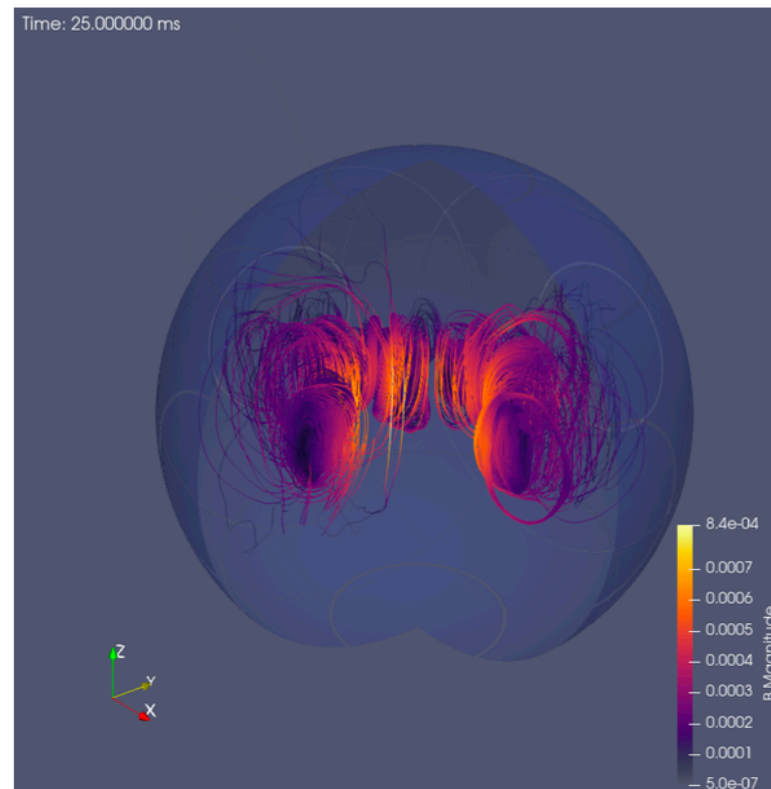
- Setup TOV star with Gamma law EoS and Poloidal field (average $B = 1.23 \times 10^{16}$ G)

$$A^\phi = A_b \max(p, p - 0.04p_{\max})$$

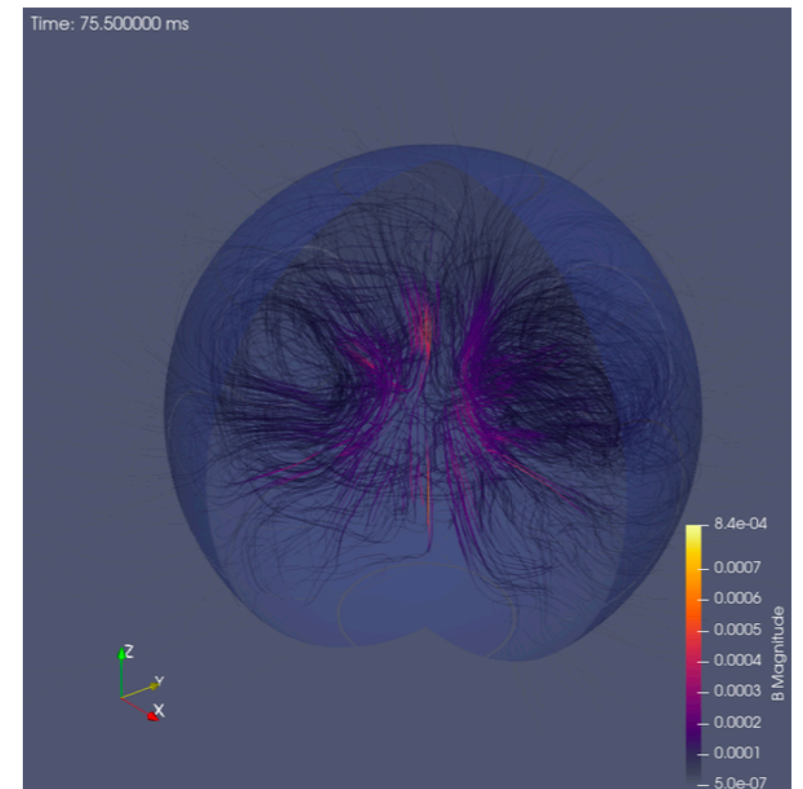
- Evolve (Cowling approximation) up to 1200 ms with (230, 114, 57) m resolutions
- Study relaxation after initial instability of the poloidal field



(a) $t = 12.5\text{ms}$



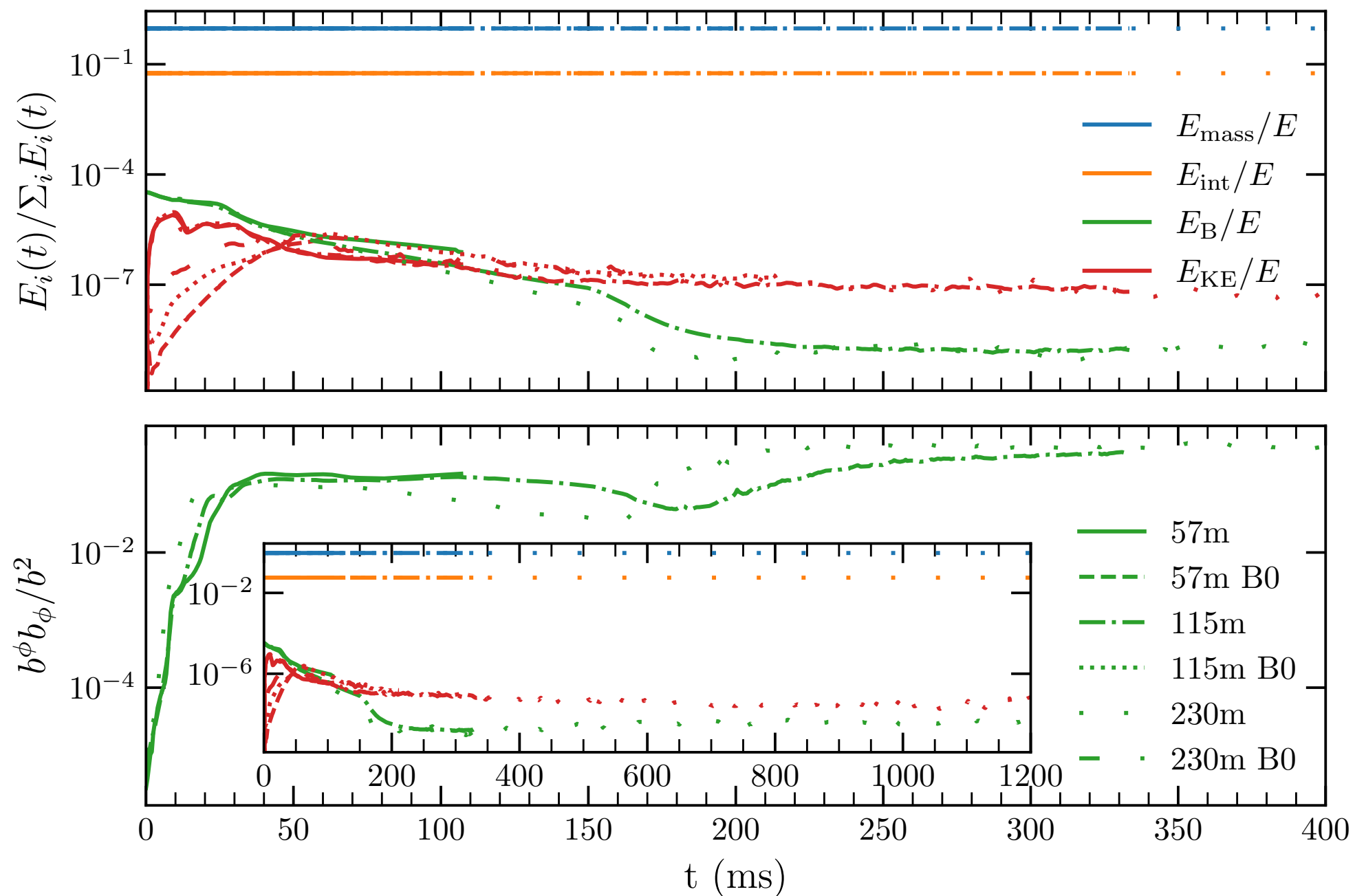
(b) $t = 25\text{ms}$



(c) $t = 75\text{ms}$

B field evolution

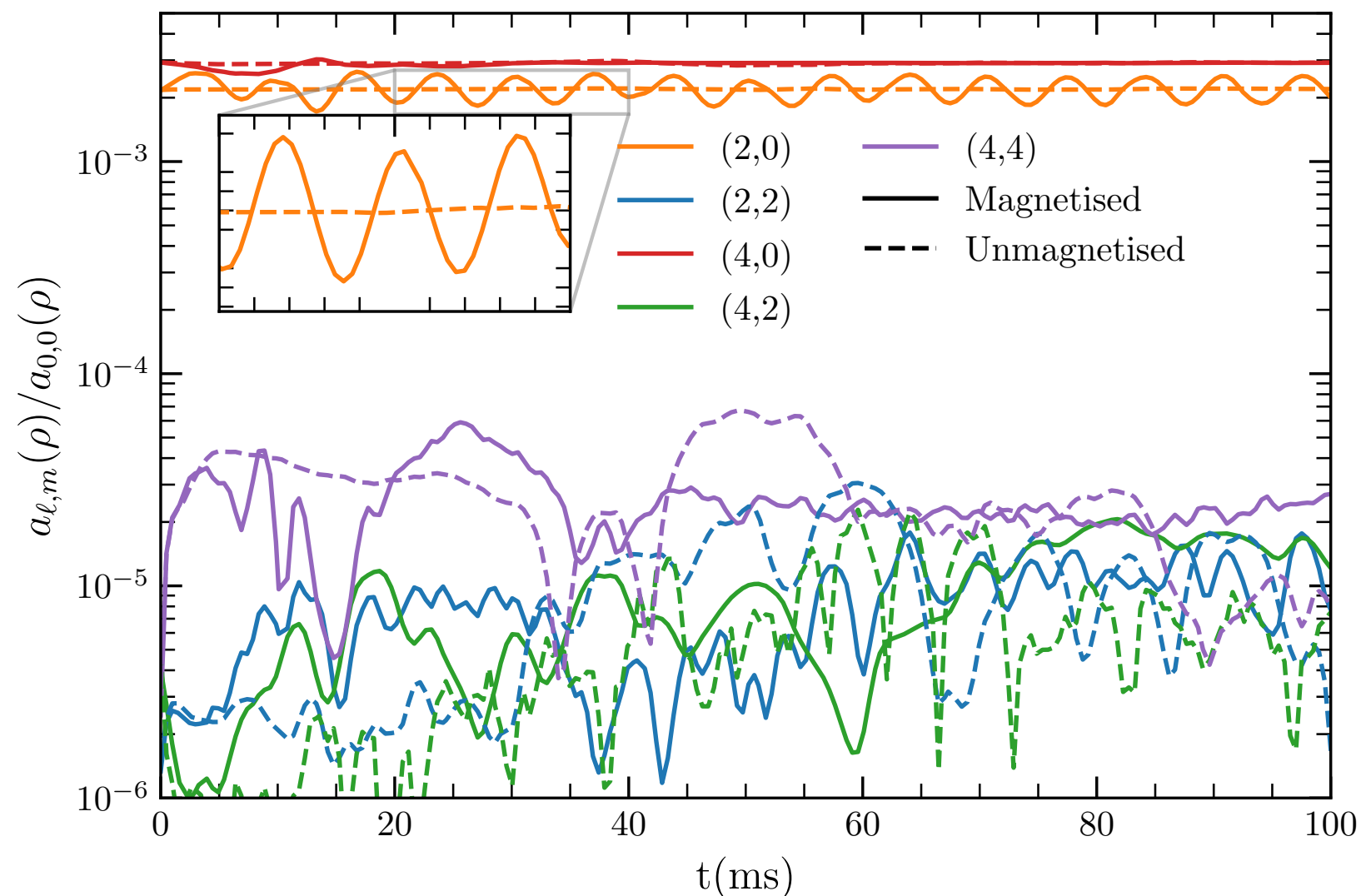
- Magnetic energy decays
- Toroidal component of $\sim 15\%$ of total consistently develops



Oscillations

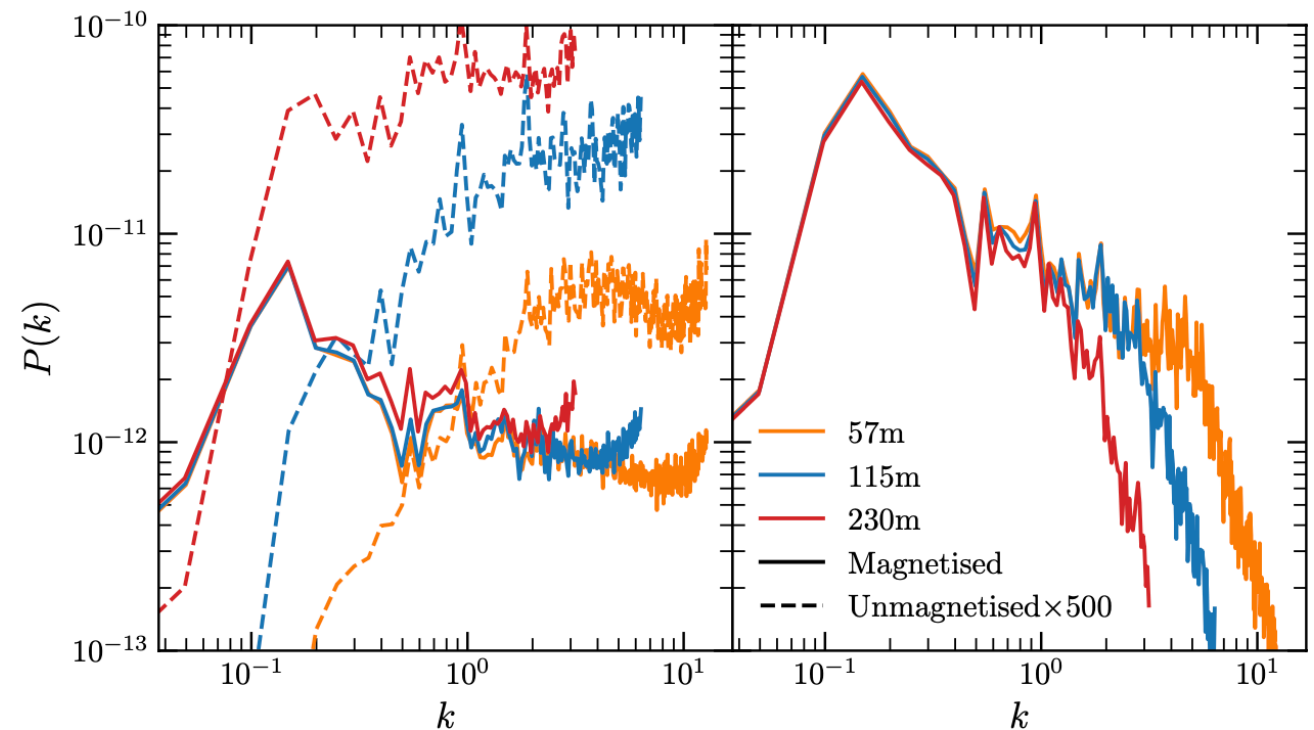
- $l=2, m=0$ oscillation (absent in pure hydro) appears at 145 Hz
- Sotani+ 08 find Alfvén modes at similar frequencies.

Link to QPOs in magnetars [Israel+05]



Turbulence

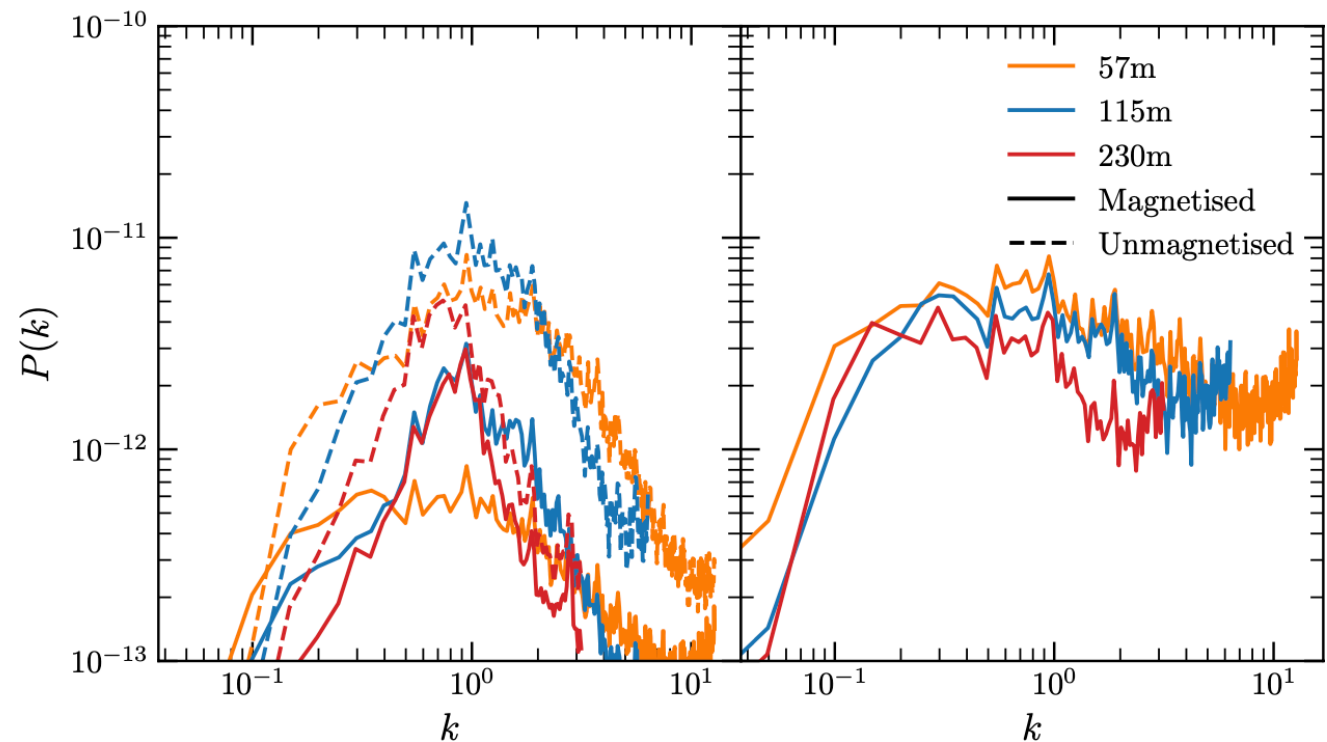
- Sur+ 2021 found a turbulent cascade - indistinguishable between HD and MHD
- We find clear evidence for a cascade (scaling $\sim$ Kolmogorov), clear difference in high res B runs.
- After accounting for overall decay, spectral density remains constant



Kinetic

(a) $t = 2.995\text{ms}$

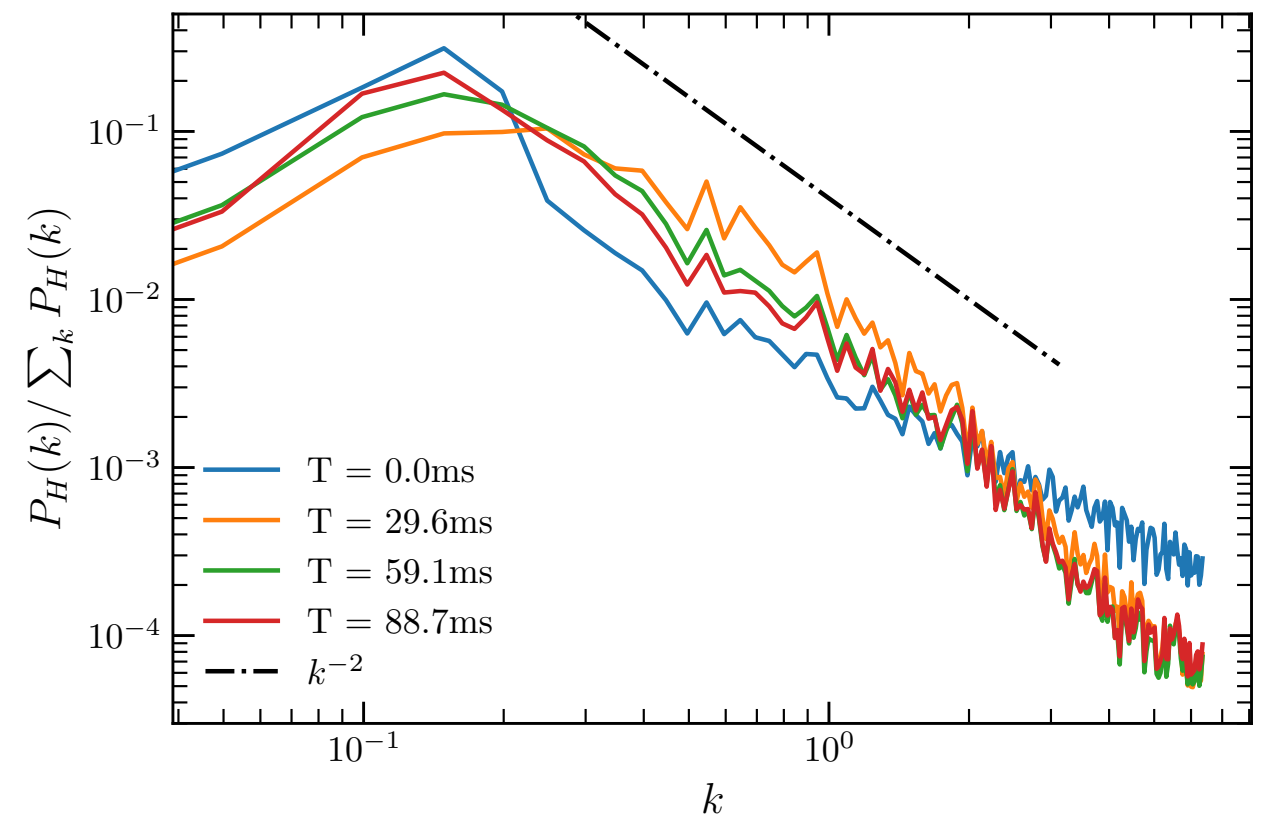
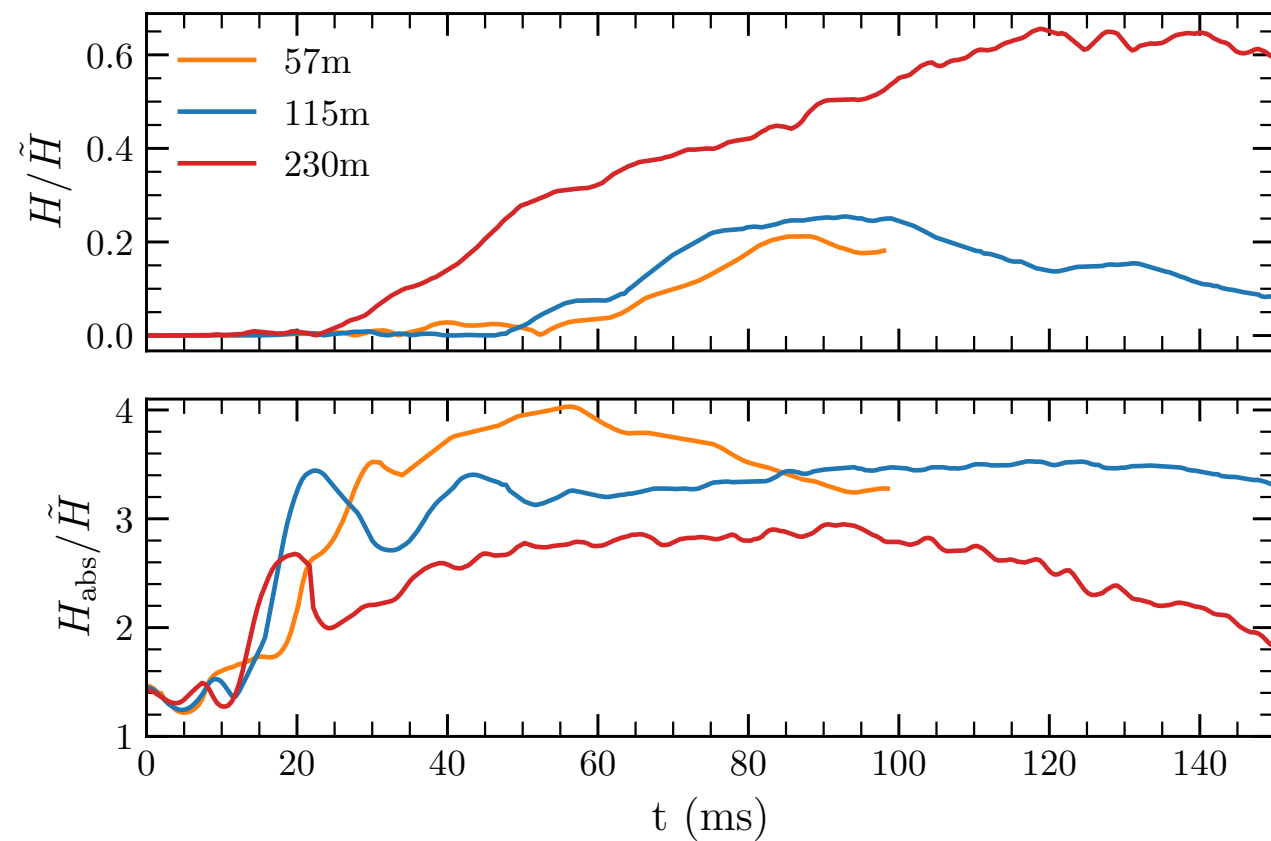
Magnetic



(c) $t = 60.091\text{ms}$

Helicity

- Helicity not conserved as energy falls off the grid due to turbulent cascade
- Inverse cascade develops large scale toroidal component



$$H = \int_V A \cdot B \, dV$$

$$H_{\text{abs}} = \int_V |A \cdot B| \, dV$$

Conclusions

- High res simulations reveal magnetically driven turbulence and inverse cascade
- Poloidal unstable - toroidal component of approx. 15% total energy develops
- Alfvén oscillations excited
- More realistic configurations (initial B field, exterior field, rotation) needed
- Applications to BNS simulations, and GW emission from isolated NSs