

# White dwarf cooling through neutrinos and $L_{\mu} - L_{\tau}$

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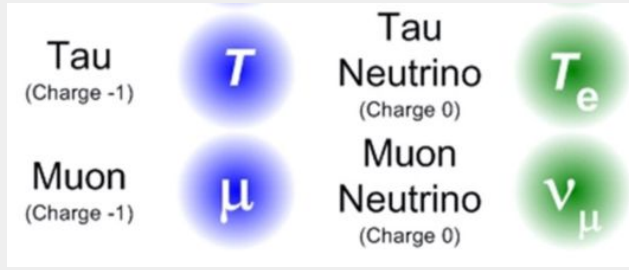
PAiP-2025

# 01

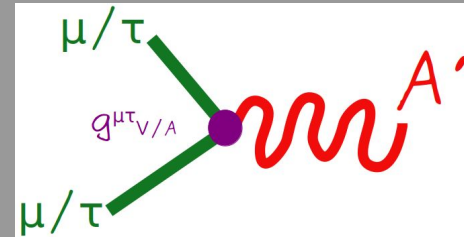
## Motivation and model

# $L_\mu - L_\tau$ model

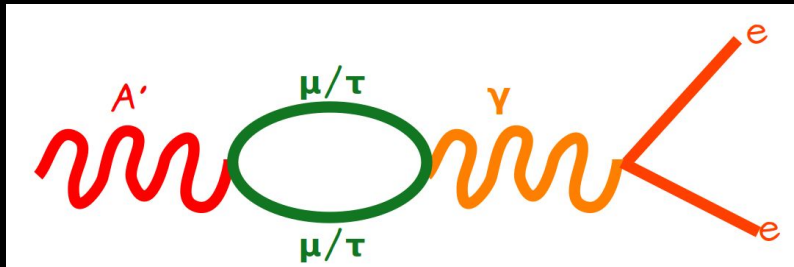
Symmetry: from global to gauge



U(1) broken gauge: dark photon



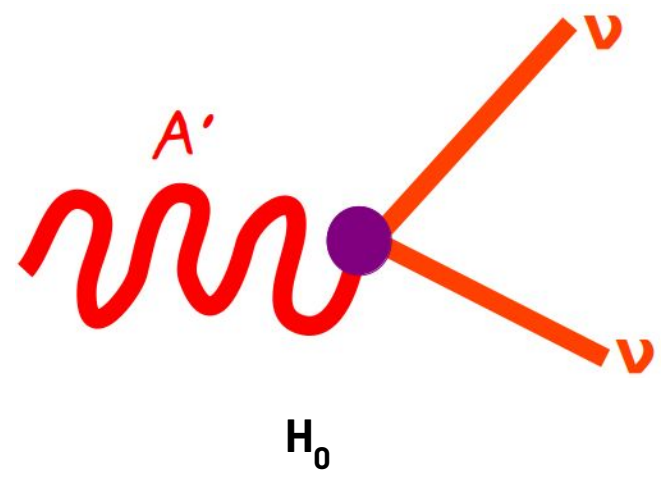
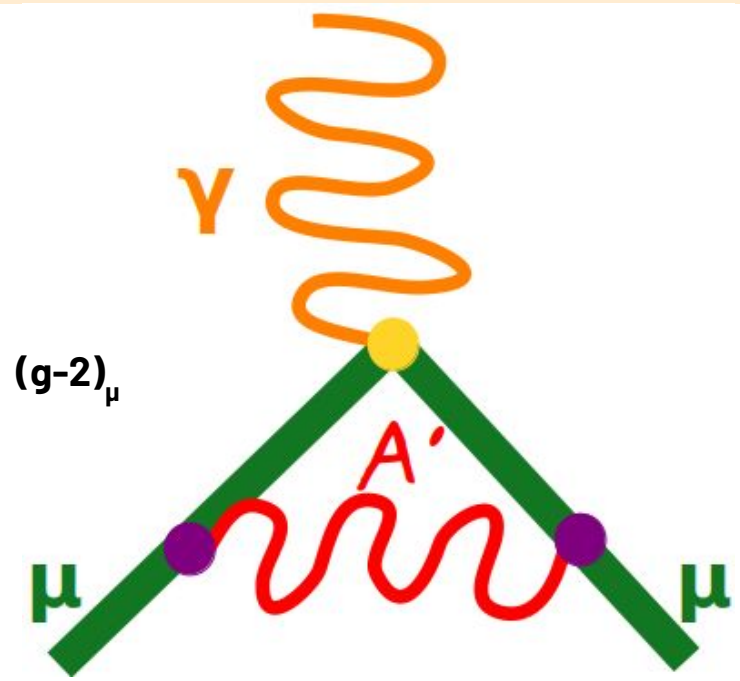
Kinetic mixing with 1st gen.



It could explain anomalies...



# Solving $(g-2)_\mu$ and $H_0$ tension



**CMB vs standard candles**  
(type-Ia supernovae and cepheid variable stars)

02

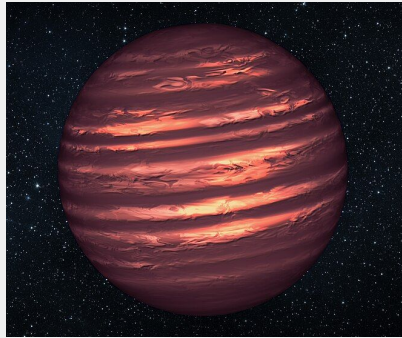
White dwarfs

# End of life of stars

## Compact objects

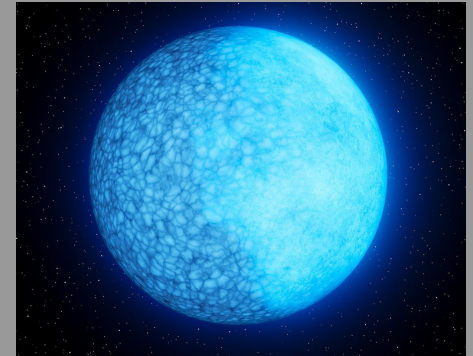
Brown dwarf

13 - 80  $M_J$



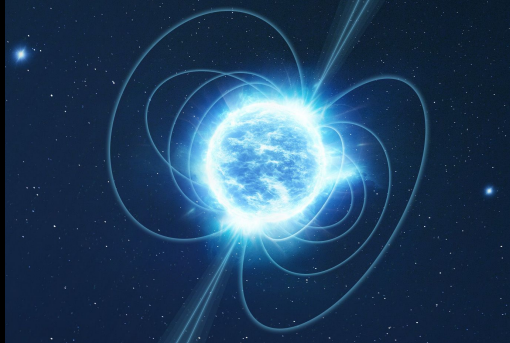
White dwarf

0.17 - 1.33  $M_{\odot}$

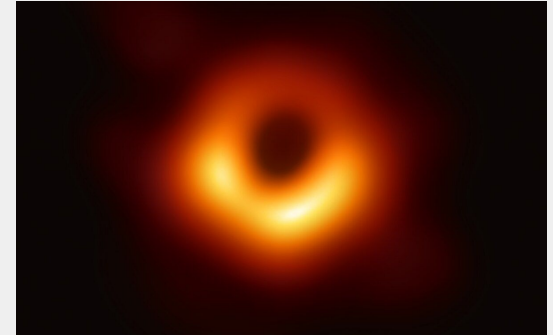


Neutron star

1.1 - 2.3  $M_{\odot}$



Black hole



# Main characteristics of White Dwarfs

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## Density

- Between  $10^6 - 10^9 \text{ kg/m}^3$
- Mainly composed by C or O.

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## Forces

- Gravitational force
- Degenerate pressure of  $e^-$
- Coulomb forces

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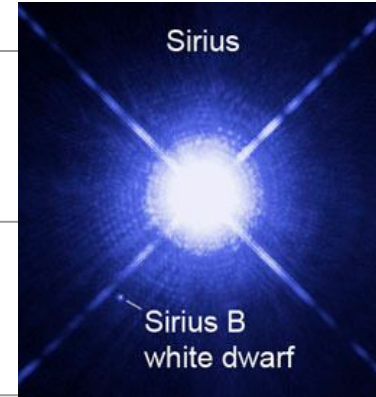
## Mass

- Less than  $\sim 1.4 M$  (Chandrasekhar limit)

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## Eq. of state

- Salpeter + TOV equations  
(Tolman-Oppenheimer-Volkoff)
- 



# WD cooling

$$C_V \frac{dT_{\text{WD}}}{dt} = -L_\nu - L_\gamma + L_H$$

## Hot WDs:

Neutrino emission  
(plasmon decay)



Credits:  
Symmetry  
magazine

## Cold WDs:

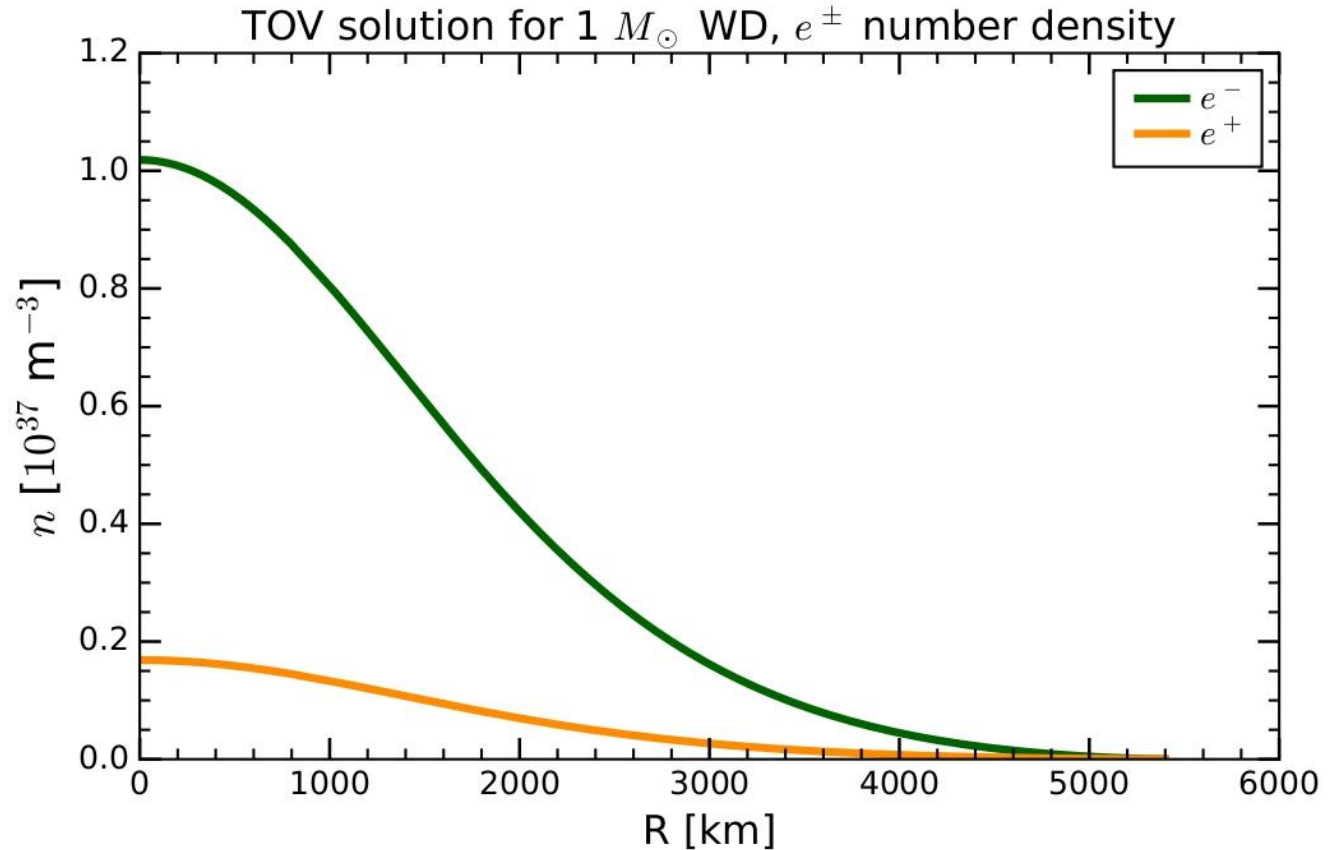
Photon surface  
emission



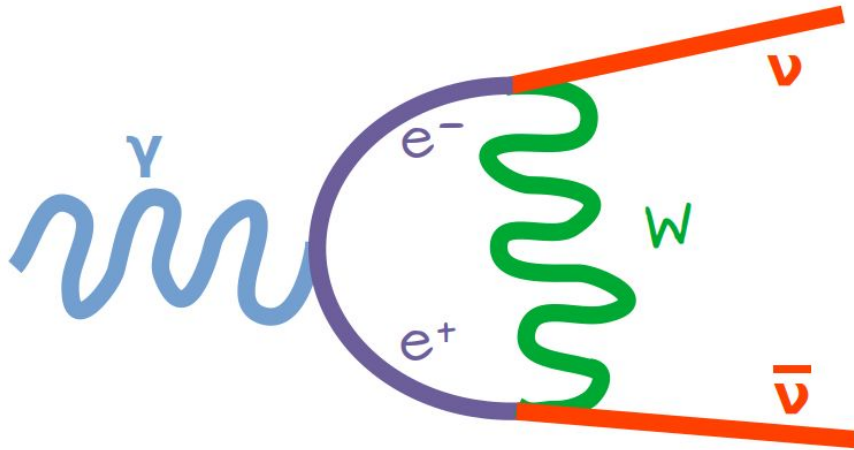
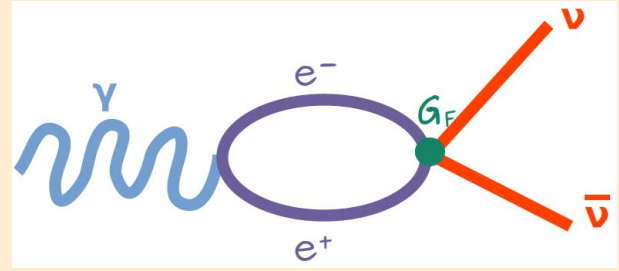
Credits:  
Live  
Science



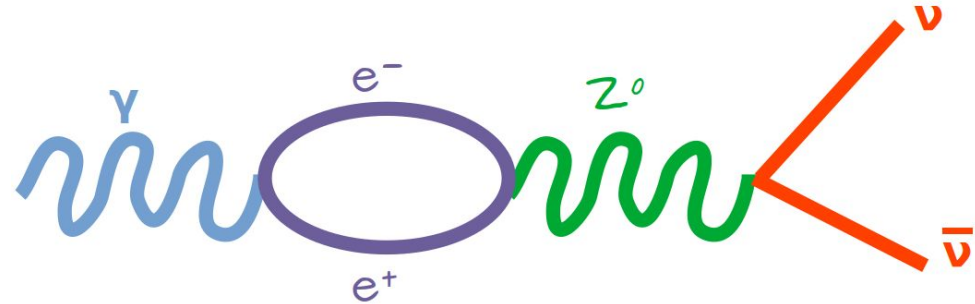
Number  
densities for  
our  $1 M_{\odot}$  WD



# Plasmon decay



**Charged  
current**



**Neutral  
current**

# Plasmon decay

## Expressions

$$\begin{aligned}
 \mathcal{M} = & \frac{G_F}{\sqrt{2}} \frac{1}{\sqrt{4\pi\alpha}} \left[ \varepsilon_\mu(\omega_l, q) C_V \left( \Pi_L(\omega_l, q) \left( 1, \frac{\omega_l}{q} \hat{q} \right)^\mu \left( 1, \frac{\omega_l}{q} \hat{q} \right)^\nu \right) \right. \\
 & + \varepsilon_\mu(\omega_t, q) g^{\mu i} \left( C_V \Pi_T(\omega_t, q) (\delta^{ij} - \hat{q}^i \hat{q}^j) \right. \\
 & \left. \left. + C_A \Pi_A(\omega_t, q) (i\varepsilon^{ijm} \hat{q}^m) \right) g^{\nu j} \right] \bar{u}(p_1) \gamma_\nu (1 - \gamma_5) v(p_2)
 \end{aligned}$$

# Plasmon decay

## Expressions

$$Q_\lambda \equiv \int d^3\vec{q} \Gamma_\lambda(q) \omega_\lambda(q) n_B(\omega_\lambda(q), T)$$

$$Q_T = 2 \left( \sum_\nu C_V^2 \right) \frac{G_F^2}{96\pi^4 \alpha} \int_0^\infty dq q^2 Z_t(q) \left( \omega_t(q)^2 - q^2 \right)^3 n_B(\omega_t(q))$$

$$Q_A = 2 \left( \sum_\nu C_A^2 \right) \frac{G_F^2}{96\pi^4 \alpha} \int_0^\infty dq q^2 Z_t(q) \left( \omega_t(q)^2 - q^2 \right) \Pi_A(\omega_t(q), q)^2 n_B(\omega_t(q))$$

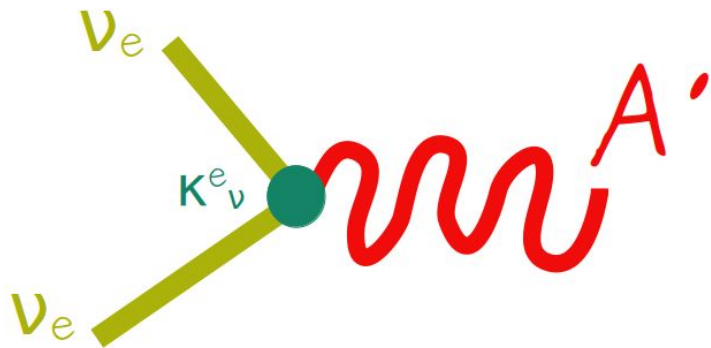
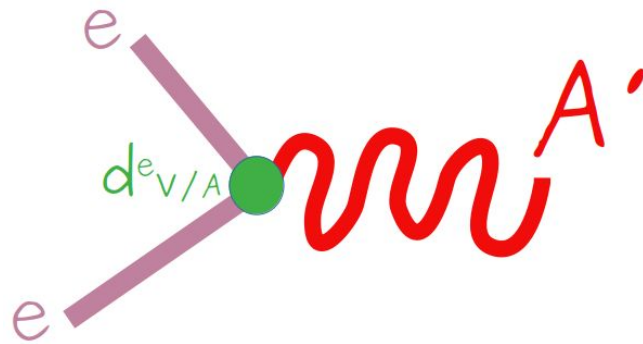
$$Q_L = \left( \sum_\nu C_V^2 \right) \frac{G_F^2}{96\pi^4 \alpha} \int_0^\infty dq q^2 Z_l(q) \omega_l(q)^2 \left( \omega_l(q)^2 - q^2 \right)^2 n_B(\omega_l(q))$$

$$L_\nu = 4\pi \int_0^{R_{\text{WD}}} Q(r) r^2 dr$$

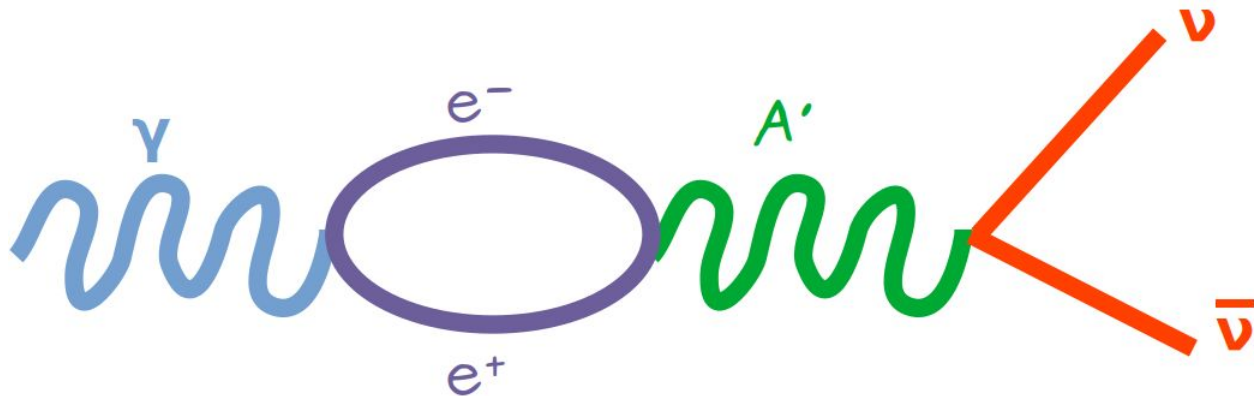
03

BSM in WDs

# Contribution from $A'$



# Plasmon decay through $A'$



$$C_a^{\alpha, \text{SM+BSM}}(Q) \rightarrow C_a^{\alpha} + b_a \frac{\sqrt{2}}{G_F} \frac{k_\nu^\alpha d_a^e}{Q^2 - m_{A'}^2}$$

a: V,A,  $b_V=1$ ,  $b_A=-1$ ,  $\alpha$ : flavor

$$F_{\text{DS}} = \frac{\mathcal{L}_{\text{DS+SM}} - \mathcal{L}_{\text{SM}}}{\mathcal{L}_{\text{SM}}}$$

Regimes  
and  
subtleties

01

Heavy case

$$m_{A'}^2 \gg Q^2$$

$$F_{\text{DS}} = \sum_{\alpha} \left( C_V^{\alpha, \text{SM}+\text{BSM}} \right)^2 / \sum_{\alpha} \left( C_V^{\alpha, \text{SM}} \right)^2 - 1$$

02

Ultra light case

$$m_{A'}^2 \ll Q^2$$

$$\Pi_{A'}^{\mu\nu} = F_{A'} P_L^{\mu\nu} + G_{A'} P_T^{\mu\nu}$$

$$D_{A'}^{\mu\nu} = \frac{-i g^{\mu\lambda}}{Q^2 - m_{A'}^2 - F_{A'}} P_{L\lambda}^{\nu} + \frac{-i g^{\mu\lambda}}{Q^2 - m_{A'}^2 - G_{A'}} P_{T\lambda}^{\nu}$$

03

Resonant case

$$m_{A'} \sim \omega_p$$

$$G_{\text{BW}}^{\mu\nu}(Q^2) = \frac{-i(g^{\mu\lambda} - q^{\mu}q^{\lambda}/m^2)}{Q^2 - m^2 - \text{Re}(F) - i \text{Im}(F)} P_{L\lambda}^{\nu} + \frac{-i(g^{\mu\lambda} - q^{\mu}q^{\lambda}/m^2)}{Q^2 - m^2 - \text{Re}(G) - i \text{Im}(G)} P_{T\lambda}^{\nu}$$

From  $\Pi^{\mu\nu}$  at  $T=0$  with  $\mathbf{v}$



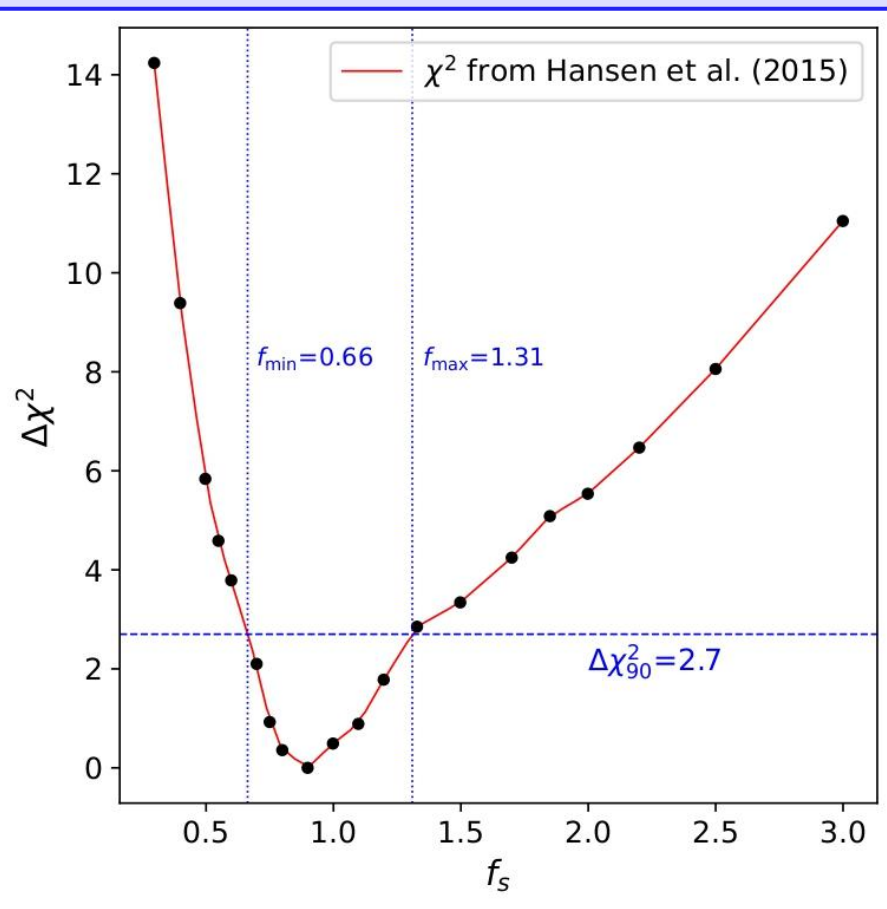
# Setting limits

## Our simulation

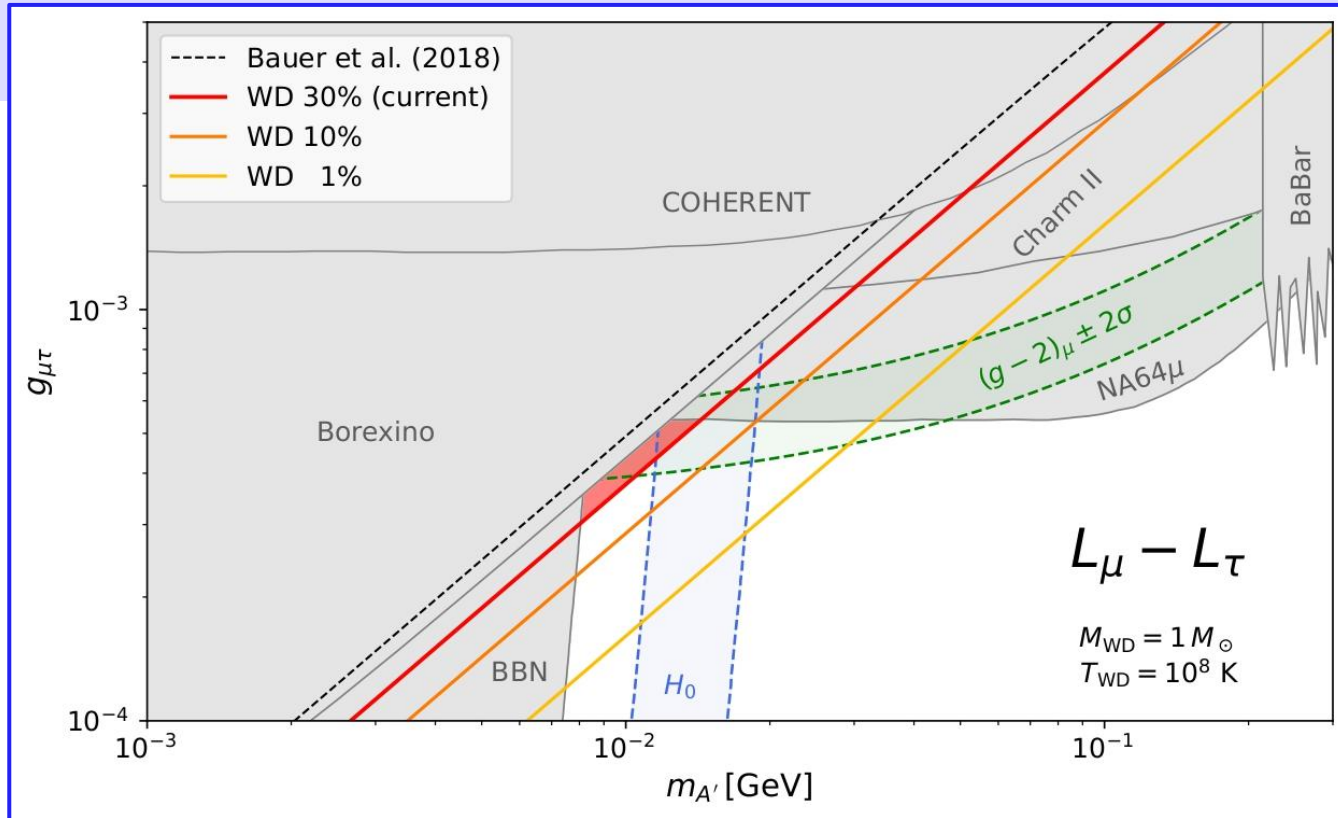
$$M_{\text{WD}} = 1 M_{\odot}$$

$$T_{\text{WD}} = 10^8 \text{ K}$$

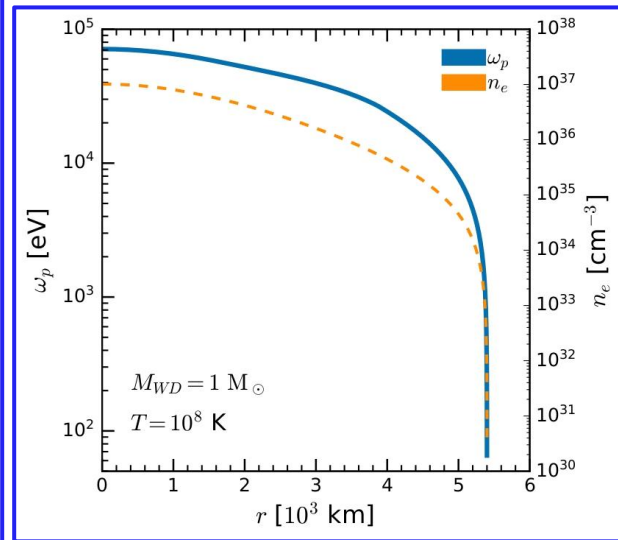
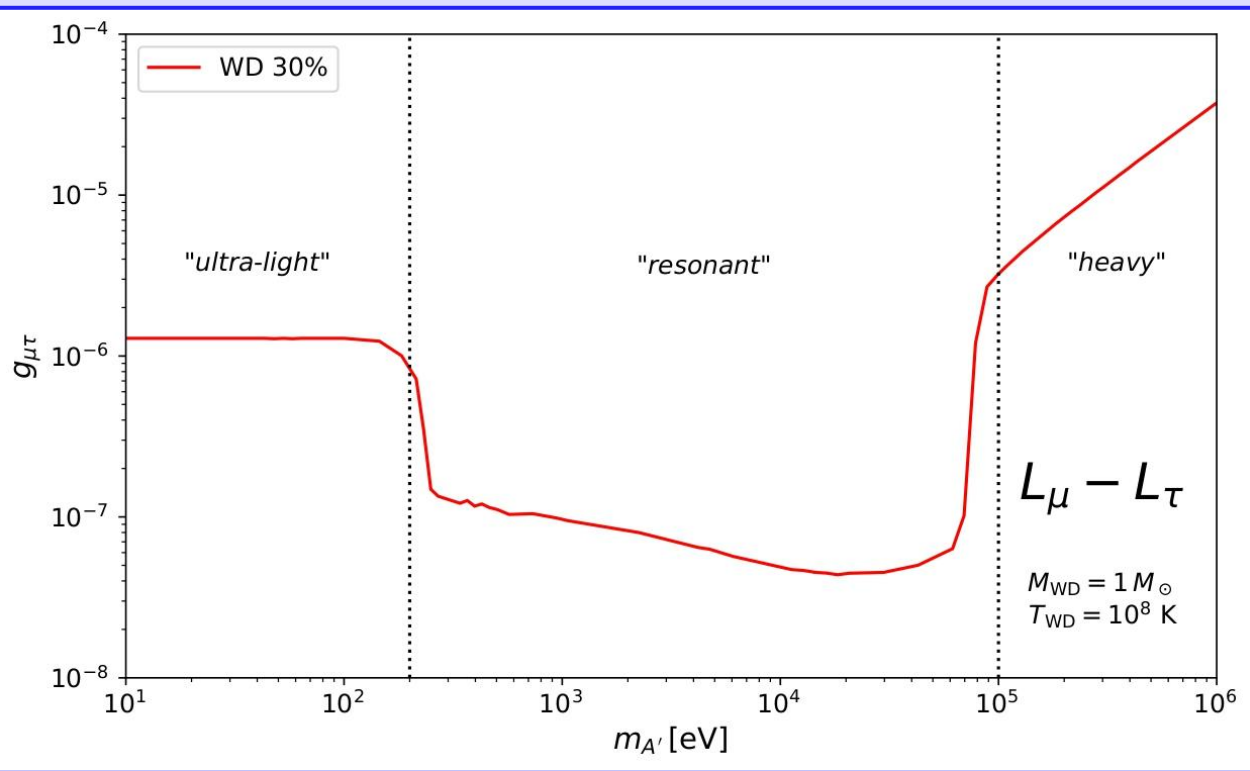
From  
observations  
of the  
Globular  
Cluster 47  
Tucanae  
**Astrophy**  
**s.J. 809 (2015)**  
**2, 141**



# Final results (1)



# Final results (2)



05

Summary

# SUMMARY

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## What was shown

- The contribution from  $L_\mu - L_\tau$  dark photon to plasmon decay in white dwarfs.
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## What we found

- White dwarfs can be used to set limits to the BSM model shown, such that part of the double solution ( $(g-2)_\mu$  and Hubble tension) is excluded.
  - There is a strong effect from the resonant region.
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## Pheno tasks

- Look for new observations from CASTOR telescope in the near future.
- 

## Future prospects

- Study these effects in SNe, red giants...
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Thank you!

Dziękuję bardzo!

06

Appendices

# Current constraints to the model

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## BBN

At masses below  $O(10)$  MeV the dark photon  $A'$  contributes significantly to the heating of the neutrino gas in the early universe leading to a too large number of neutrino degrees of freedom,  $\Delta N_{\text{eff}}$ , during BBN.

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## NA64 $\mu$

By using a missing energy-momentum technique with a high energy muon beam.

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## Borexino

From the measurement of the  ${}^7\text{Be}$  solar neutrino flux, masses of  $m_{A'} \sim 10$  MeV are excluded for  $g_{\mu\tau} \sim 0.0005$ .

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## BaBar

From resonance searches in four-muon production, high masses excluded.

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## COHERENT

From measurements of coherent elastic neutrino-nucleus scattering (CEvNS) with a CsI[Na] target, high couplings excluded.

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## CHARM-II

From the search for neutrino trident production, for masses  $\sim 100$  MeV.

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